

HEWLETT-PACKARD

HP-67/HP-97

Users' Library Solutions
Energy Conservation



INTRODUCTION

In an effort to provide continued value to its customers, Hewlett-Packard is introducing a unique service for the HP fully programmable calculator user. This service is designed to save you time and programming effort. As users are aware, Programmable Calculators are capable of delivering tremendous problem solving potential in terms of power and flexibility, but the real genie in the bottle is program solutions. HP's introduction of the first handheld programmable calculator in 1974 immediately led to a request for program **solutions** — hence the beginning of the HP-65 Users' Library. In order to save HP calculator customers time, users wrote their own programs and sent them to the Library for the benefit of other program users. In a short period of time over 5,000 programs were accepted and made available. This overwhelming response indicated the value of the program library and a Users' Library was then established for the HP-67/97 users.

To extend the value of the Users' Library, Hewlett-Packard is introducing a unique service—a service designed to save you time and money. The Users' Library has collected the best programs in the most popular categories from the HP-67/97 and HP-65 Libraries. These programs have been packaged into a series of low-cost books, resulting in substantial savings for our valued HP-67/97 users.

We feel this new software service will extend the capabilities of our programmable calculators and provide a great benefit to our HP-67/97 users.

A WORD ABOUT PROGRAM USAGE

Each program contained herein is reproduced on the standard forms used by the Users' Library. Magnetic cards are not included. The Program Description I page gives a basic description of the program. The Program Description II page provides a sample problem and the keystrokes used to solve it. The User Instructions page contains a description of the keystrokes used to solve problems in general and the options which are available to the user. The Program Listing I and Program Listing II pages list the program steps necessary to operate the calculator. The comments, listed next to the steps, describe the reason for a step or group of steps. Other pertinent information about data register contents, uses of labels and flags and the initial calculator status mode is also found on these pages. Following the directions in your HP-67 or HP-97 **Owners' Handbook and Programming Guide**, "Loading a Program" (page 134, HP-67; page 119, HP-97), key in the program from the Program Listing I and Program Listing II pages. A number at the top of the Program Listing indicates on which calculator the program was written (HP-67 or HP-97). If the calculator indicated differs from the calculator you will be using, consult Appendix E of your **Owner's Handbook** for the corresponding keycodes and keystrokes converting HP-67 to HP-97 keycodes and vice versa. No program conversion is necessary. The HP-67 and HP-97 are totally compatible, but some differences do occur in the keycodes used to represent some of the functions.

A program loaded into the HP-67 or HP-97 is not permanent—once the calculator is turned off, the program will not be retained. You can, however, permanently save any program by recording it on a blank magnetic card, several of which were provided in the Standard Pac that was shipped with your calculator. Consult your **Owner's Handbook** for full instructions. A few points to remember:

The Set Status section indicates the status of flags, angular mode, and display setting. After keying in your program, review the status section and set the conditions as indicated before using or permanently recording the program.

REMEMBER! To save the program permanently, **clip** the corners of the magnetic card once you have recorded the program. This simple step will protect the magnetic card and keep the program from being inadvertently erased.

As a part of HP's continuing effort to provide value to our customers, we hope you will enjoy our newest concept.

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Program calculates one of any four quantities in the design of an air cooling system for electronic equipment. Given the ambient temperature, the power dissipation in the enclosure, and the worst case maximum temperature, the program calculates the required blower rating in cubic feet per minute.	
BLACK BODY THERMAL RADIATION	6
Calculates wave length of maximum emissive power, total emissive power, monochromatic emissive power, emissive power from zero to a specified wave length, for black radiating surfaces.	
ECONOMIC INSULATION THICKNESS	14
Can be used to determine the economic thickness of insulation given the thermal properties of the insulation, the cost of energy, hours of operation, cost of insulation, and the temperature difference.	
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Can be used to calculate the overall heat transfer coefficient for composite tubes and walls from individual section conductances and surface coefficients.	
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Computes heat duty, heat load, transfer area, logarithmic mean temperature difference, heat capacity, transfer coefficient and mass flow rate.	
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Computes sun's altitude, azimuth, and the fraction of the sun's radiation which will penetrate the surface of a solar pond given index of refraction of pond fluid, latitude, number of days after spring equinox, and number of hours before or after solar noon.	
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Computes length of day and total amount of solar radiation received by a horizontal surface of unit area as a function of latitude and declination of the sun.	
TEMPERATURE OR CONCENTRATION PROFILE FOR A SEMI-INFINITE SOLID	35
May be used to find the temperature (or concentration profile) at a specified time for a semi-infinite solid with constant surface temperature (or concentration) the profiles is assumed to be uniform when time equals zero.	

TRANSIENT TEMPERATURE DISTRIBUTION IN A SEMI-INFINITE SOLID WITH CONVECTION BOUNDARY CONDITION	40
Computes factor enabling calculation of temperature in a semi- infinite solid for data including distance from surface, time, thermal conductivity, thermal diffusivity, and heat transfer coefficient.	
CONSERVATION OF ENERGY.	44
This is a two card set which may be used to solve a variety of energy conservative flow problems (Bernoulli's equation). Card one accepts English units while card two is for metric units.	

Program Description I

1

Program Title Air Cooling System Design

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

Define: H_i = Molal enthalpy of air at T_i and P_i (BTU/LB Mole)

P_i = Power in kilowatts (3413 kW-Hr / BTU)

T_i = Temperature in degrees Rankine ($^{\circ}R$)

\dot{V}_i = Volumetric flow rate

\dot{N}_i = Molal flow rate

$i = 1$ for outside enclosure

p_i = pressure (in atmospheres)

$i = 2$ for inside enclosure

C_p = specific heat at constant pressure =
6.953 (BTU/lb-mole $^{\circ}R$)

- Molar volume for air at a temperature T and pressure p is $V = (0.35905$
 $(0.35905 \times 10^3 \text{ Ft}^3/\text{lb-mole}) (\text{Atm}/p)(T/491.7^{\circ}R) = .7302$

- Energy balance at steady state

$$H_1 \dot{N}_1 + (P_1 - P_2) = H_2 \dot{N}_2$$

- Molal volume for an ideal gas has a flow rate $\dot{V}_1 = \left(\frac{p_2}{p_1}\right) \left(\frac{T_2}{T_1}\right) \dot{V}_2$

- Specific heat equation $H_2 - H_1 = C_p (T_2 - T_1)$

- Neglect pressure difference $p_i = p_2$

Continued on next page →

Operating Limits and Warnings

1. Calculation assumes steady state, treats air as an ideal gas, neglects humidity, etc.
2. The "E" key should not be used as it contains several values needed to cram the program into the limited memory.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description I

Program Title Air Cooling System Design

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

Then $\dot{V}_2 = \frac{K(P_2 - P_1)T_2}{T_2 - T_1} = \text{Ft}^3/\text{min} = \text{Req'd flow rate}$ $k = 5.974$

or $P_2 - P_1 = \frac{\dot{V}_2}{k} \left(\frac{T_2 - T_1}{T_2} \right) = \text{kW} = \text{Power Input}$

or $T_2 = \frac{\dot{V}_2 T_1}{V_2 - k(P_2 - P_1)} = \text{Max. Enclosure Temperature}$

or $T_1 = \frac{T_2}{V_2} (V_2 - k(P_2 - P_1)) = \text{Ambient Temperature}$

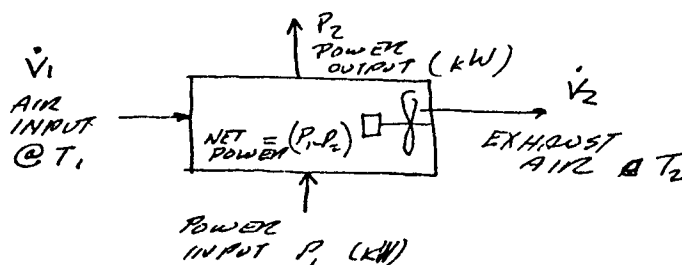
Operating Limits and Warnings

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Program Description II

Sketch(es)



Sample Problem(s)

$$t_1 = 72^\circ\text{F}$$

$$t_2 = 85^\circ\text{F}$$

$$\dot{V} = 250 \text{ ft}^3/\text{min}$$

$$\text{Calculate: } P_{1N} = 0.9982 \text{ kW}$$

Now assume you wish to change the ambient to 68°F with the same power and see what effect it has upon the blower rating. After having first pressed "D"

just key in 68 in "A" and press "C". To use the calculated P_{1N} $\dot{V}=191.1765$

Now change \dot{V} to 200 and P_{1N} to 1kW and resolve for $t_1 = 68.7209^\circ\text{F}$. Now change t_1 to 65°F and calculate t_2 for the $\dot{V}=200$ and $P_{1N} = 1$ by entering 65° in "A" and pressing "B" to obtain $t_2 = 81.1646$

If you forget one of the other three variables in using the program for optimizing just look in R_1, R_2, R_3 or R_4 For T_1, T_2, V or P_{1N} as may be of interest.

Solution(s)

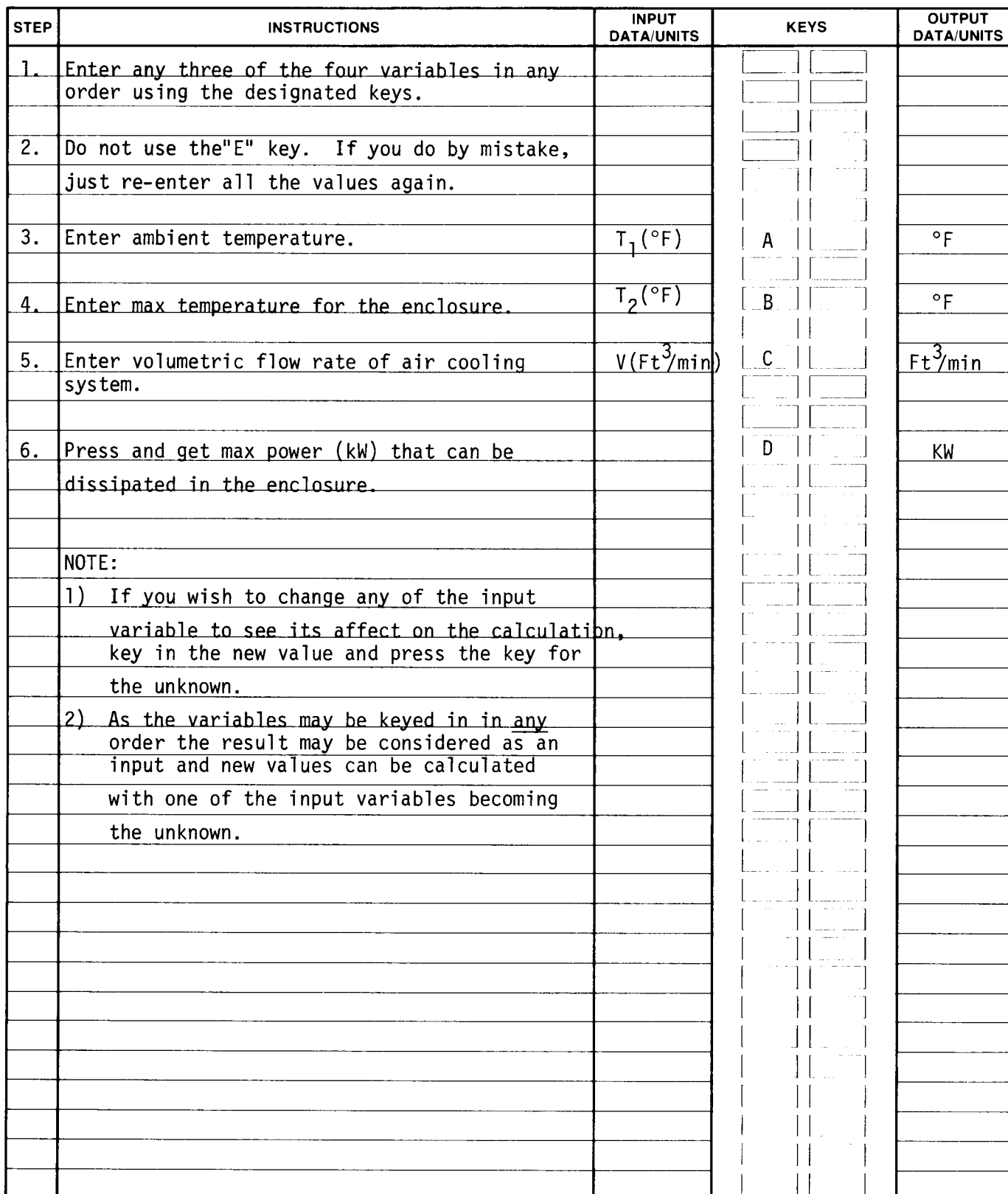
Keystrokes:

Outputs

72[A] 85[B] 250[C] [D] -----	0.9982
[D] 68[A] [C] -----	191.1765
200[C] 1[D] [A] -----	68.7209
65[A] [B] -----	81.1646

Reference(s) V.M. Faires, Thermodynamics, 5th Edition, MacMillan Co., New York, 1970; page 453.

This program is a translation of the HP-65 User's Library program #02001A submitted by Todd A.C. Heard.



Program Description I

Program Title Black Body Thermal Radiation

Contributor's Name Hewlett-Packard

Address 1000 N. E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

Bodies with finite temperatures emit thermal radiation. The higher the absolute temperature, the more thermal radiation emitted. Bodies which emit the maximum possible amount of energy at every wavelength for a specified temperature are said to be black bodies. While black bodies do not actually exist in nature, many surfaces may be assumed to be black for engineering considerations.

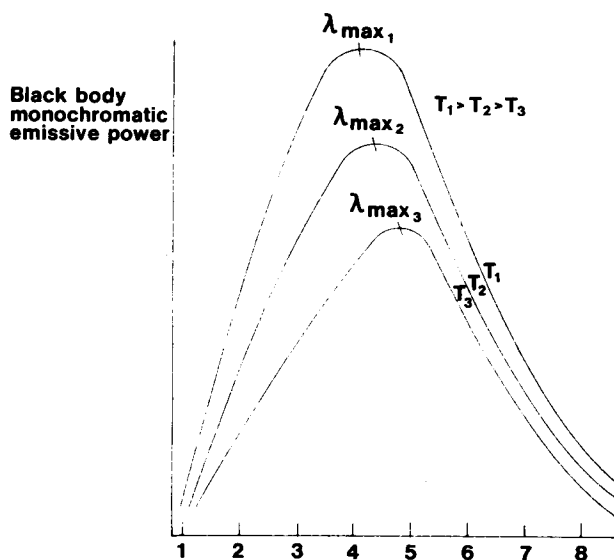


Figure 1.

(continued next page)

Operating Limits and Warnings

A minute or more may be required to obtain $E_{b(0-\lambda)}$ or $E_{b(\lambda_1-\lambda_2)}$ since the integration is numerical.

Sources differ on values for constants. This could yield small discrepancies between published tables and program outputs.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Figure 1 is a representation of black body thermal emission as a function of wavelength. Note that as temperature increases, the area under the curves (total emissive power $E_{b(0-\infty)}$) increases. Also note that the wavelength of maximum emissive power λ_{\max} shifts to the left as temperature increases.

This program calculates the wavelength of maximum emissive power for a given temperature, the temperature for which a given wavelength would be the wavelength of maximum emissive power, the total emissive power over all wavelengths, the emissive power at a particular wavelength, the emissive power from zero to a specified wavelength, and the emissive power between specified wavelengths.

Equations:

$$\lambda_{\max} T_{\lambda_{\max}} = c_3$$

$$E_{b(0-\infty)} = \sigma T^4$$

$$E_{b\lambda} = \frac{2\pi c_1}{\lambda^5 (e^{c_2/\lambda T} - 1)}$$

$$E_{b(0-\lambda)} = \int_0^\lambda E_{b\lambda} d\lambda$$

$$= 2\pi c_1 \sum_{k=1}^{\infty} \frac{-T/kc_2}{e^{-\frac{kc_2}{T\lambda}}} \left[\left(\frac{1}{\lambda} \right)^3 + \frac{3T}{\lambda^2 kc_2} + \frac{6}{\lambda} \left(\frac{T}{kc_2} \right)^2 + 6 \left(\frac{T}{kc_2} \right)^3 \right]$$

$$E_{b(\lambda_1 - \lambda_2)} = E_{b(0-\lambda_2)} - E_{b(0-\lambda_1)}$$

where

λ_{\max} is the wavelength of maximum emissivity in microns;

T is the absolute temperature in $^{\circ}\text{R}$ or K;

$E_{b(0-\infty)}$ is the total emissive power in Btu/hr-ft² or Watts/cm²;

$E_{b\lambda}$ is the emissive power at λ in Btu/hr-ft²- μm or Watts/cm²- μm ;

$E_{b(0-\lambda)}$ is the emissive power for wavelengths less than λ in Btu/hr-ft² or Watts/cm²;

$E_{b(\lambda_1-\lambda_2)}$ is the emissive power for wavelengths between λ_1 and λ_2 in Btu/hr-ft² or Watts/cm².

$$\begin{aligned} c_1 &= 1.8887982 \times 10^7 \text{ Btu-}\mu\text{m}^4/\text{hr-ft}^2 \\ &= 5.9544 \times 10^3 \text{ W}\mu\text{m}^4/\text{cm}^2 \end{aligned}$$

$$c_2 = 2.58984 \times 10^4 \mu\text{m-}^{\circ}\text{R} = 1.4388 \times 10^4 \mu\text{m-K}$$

$$c_3 = 5.216 \times 10^3 \mu\text{m-}^{\circ}\text{R} = 2.8978 \times 10^3 \mu\text{m-K}$$

$$\sigma = 1.713 \times 10^{-9} \text{ Btu/hr-ft}^2 \cdot ^{\circ}\text{R}^4 = 5.6693 \times 10^{-12} \text{ W/cm}^2 \cdot \text{K}^4$$

$$\sigma_{\text{exp}} = 1.731 \times 10^{-9} \text{ Btu/hr-ft}^2 \cdot ^{\circ}\text{R}^4 = 5.729 \times 10^{-12} \text{ W/cm}^2 \cdot \text{K}^4$$

Program Description II

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Sketch(es)

Sample Problem(s) Example 1:

What percentage of the radiant output of a lamp is in the visible range (0.4 to 0.7 microns) if the filament of the lamp is assumed to be a black body at 2400 K? What is the percentage at 2500 K?

Keystrokes:

Outputs:

[f] [B]-----→ $5.669 \times 10^{-12} \text{ W/cm}^2\text{-K}^4$

2400 [A] .4 [B] .7 [f] [E] [C] [÷] 100 [x]-----→ 2.641%

2500 [A] .7 [f] [E] [C] [÷] 100 [x]-----→ 3.337%

Example 2:

If the human eye was designed to work most efficiently is sunlight and the visible spectrum runs from about 0.4 to 0.7 microns, what is the sun's temperature in degrees Rankine? Assume that the sun is a black body. Using the temperature calculated, find the fraction of the sun's total emissive power which falls in the visible range. Find the percentage of the sun's radiation which has a wavelength less than 0.4 microns.

Keystrokes:

Outputs:

[f] [A]-----→ $1.713 \times 10^{-9} \text{ Btu/hr-ft}^2\text{-}^\circ\text{R}^4$

Compute mean of visible range.

.4 [+] .7 [+] 2 [÷]-----→ $550.0 \times 10^{-3} \mu\text{m}$

Compute temperature of sun.

[B]-----→ $9.484 \times 10^3 \text{ }^\circ\text{R}$

(continued)

Reference(s)

Robert Siegel and John R. Howell, *Thermal Radiation Heat Transfer*, Volume 1, National Aeronautics and Space Administration, 1968.

Compute percentage of power in visible range.

[A] .4 [B] .7 [E] [C] [÷] 100 [x]-----→ $33.70 \times 10^0 \%$

Compute percentage of power under 0.4 microns.

[E] [C] [÷] 100 [x]-----→ 8.433%

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Black Body Thermal Radiation

Eng SI Exp σ

$T \rightarrow \lambda_{\max} \quad \lambda \rightarrow T(\lambda_{\max}) \rightarrow E_b(0-\infty) \rightarrow E_{b\lambda} \quad \lambda' \rightarrow E_b(\lambda-\lambda') \quad E_b(0-\lambda)$

[illegible]

97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLc	21 16 11	Store English constants.	057	5	05	
002	1	01		058	.	-62	
003	8	08		059	6	06	
004	8	08		060	6	06	
005	8	08		061	9	09	
006	7	07		062	3	03	
007	9	09		063	EEX	-23	
008	8	08		064	CHS	-22	
009	2	02		065	1	01	
010	ST01	35 01		066	2	02	
011	2	02		067	ST04	35 04	Convert to experimental σ .
012	5	05		068	RTN	24	
013	8	08		069	*LBLc	21 16 13	
014	9	09		070	1	01	
015	8	08		071	.	-62	
016	.	-62		072	0	00	
017	4	04		073	1	01	
018	ST02	35 02		074	0	00	
019	5	05		075	5	05	
020	2	02		076	STX4	35-35 04	
021	1	01		077	RCL4	36 04	Store T and calculate λ_{\max} .
022	6	06		078	RTN	24	
023	ST03	35 03		079	*LBLA	21 11	
024	.	-62		080	ST05	35 05	
025	1	01		081	RCL3	36 03	
026	7	07		082	XZY	-41	
027	1	01		083	÷	-24	
028	3	03		084	RTN	24	
029	1	01		085	*LBLB	21 12	Store λ and calculate T for which λ would be λ_{\max} .
030	2	02		086	ST06	35 06	
031	EEX	-23		087	RCL3	36 03	
032	CHS	-22		088	XZY	-41	
033	8	08		089	÷	-24	
034	ST04	35 04		090	RTN	24	
035	RTN	24		091	*LBLC	21 13	Calculate $E_{b(0-\infty)}$.
036	*LBLb	21 16 12		092	RCL5	36 05	
037	5	05		093	X²	53	
038	9	09		094	X²	53	
039	5	05		095	RCL4	36 04	
040	4	04		096	x	-35	
041	.	-62		097	RTN	24	
042	4	04		098	*LBLO	21 14	Calculate $E_{b\lambda}$.
043	ST01	35 01		099	RCL1	36 01	
044	1	01		100	ENT1	-21	
045	4	04		101	+	-55	
046	3	03		102	Pi	16-24	
047	8	08		103	x	-35	
048	8	08		104	RCL6	36 06	
049	ST02	35 02		105	5	05	
050	2	02		106	Y*	31	
051	8	08		107	÷	-24	
052	9	09		108	RCL2	36 02	
053	7	07		109	RCL6	36 06	
054	.	-62		110	÷	-24	
055	8	08		111	RCL5	36 05	
056	ST03	35 03		112	÷	-24	

REGISTERS

0	1	2	3	4	5	6	7	8	9
λ	c_1	c_2	c_3	σ	T	λ, λ'	sum	kc_2/T	
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

97 Program Listing II

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STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
113	e ^x	33		169	XZV	16-35	
114	.	01		170	GT01	22 01	
115	-	-45		171	R↓	-31	
116	÷	-24		172	CLX	-51	
117	RTN	24		173	RCL7	36 07	
118	*LBL E	21 15	Calculate E _{b(0-λ)} .	174	ENT↑	-21	
119	0	00		175	+	-55	
120	ST08	35 08		176	Pi	16-24	
121	ST07	35 07		177	×	-35	
122	*LBL1	21 01		178	RCL1	36 01	
123	R↓	-31		179	×	-35	
124	CLX	-51		180	RTN	24	
125	RCL8	36 08		181	*LBL e	21 16 15	Calculate E _{b(λ-λ')} .
126	RCL2	36 02		182	ENT↑	-21	
127	RCL5	36 05		183	ENT↑	-21	
128	÷	-24		184	GSPE	23 15	
129	-	-45		185	XZV	-41	
130	ST08	35 08		186	RCL6	36 06	
131	3	03		187	ST00	35 00	
132	XZV	-41		188	R↓	-31	
133	÷	-24		189	ST08	35 08	
134	RCL6	36 06		190	GSBE	23 15	
135	X ²	53		191	-	-45	
136	÷	-24		192	ABS	16 31	
137	LSTX	16-63		193	RCL0	36 00	
138	1/X	52		194	ST06	35 06	
139	RCL6	36 06		195	R↓	-31	
140	÷	-24		196	RTN	24	
141	-	-45					
142	E	06					
143	RCL6	36 06					
144	÷	-24		200			
145	RCL8	36 08					
146	X ²	53					
147	÷	-24					
148	-	-45					
149	6	06					
150	RCL8	36 08					
151	X ²	53					
152	÷	-24					
153	RCL8	36 08		210			
154	÷	-24					
155	+	-55					
156	RCL8	36 08					
157	RCL6	36 06					
158	÷	-24					
159	e ^x	33					
160	×	-35					
161	RCL8	36 08					
162	÷	-24					
163	ST+7	35-55 07					
164	RCL7	36 07		220			
165	÷	-24					
166	EEX	-23					
167	CHS	-22					
168	5	05					

LABELS					FLAGS	SET STATUS		
A	B	C	D	E	0	FLAGS	TRIG	DISP
T→λ _{max}	λ→T(λ _{max})	E→E _{b(0-λ)}	→E _{b λ}	E→E _{b(0-λ)}	1	ON OFF		
a Eng	SI	c Exp σ	d	e λ'→E _{b(λ-λ')}	2	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input type="checkbox"/>
0	1 E _{b(0-λ)}	2	3	4		1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5	6	7	8	9	3	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input checked="" type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n <u>3</u>

Program Description I

Program Title Economic Insulation Thickness

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

$$I = 3.46 \times 10^{-3} \sqrt{Y(\Delta T) M k/b} - 6k$$

Where:

I = thickness of insulation in inches

Y = hours per year

k = conductivity of insulation BTU/ft²°F/ft.

ΔT = temperature difference, °F

M = cost of energy \$ per 10⁶ BTU

b = cost of insulation \$ per ft² per in. thickness

Operating Limits and Warnings

Insulation is assumed to be protected from moisture saturation possibilities.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

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Sketch(es)

Sample Problem(s)

A. What thickness of insulation is economic for a prefab wall used in a structure with the following conditions?

$$k = 0.15, \Delta T = 72^{\circ}-32^{\circ}\text{F}$$

$$Y = 24 \text{ hrs per day per year}(8760),$$

$$M = \$1.00 \text{ per } 10^6 \text{ BTU}$$

$$b = \$0.20 \text{ per sq. ft. per inch thickness}$$

B. What if the energy price is \$2.50/million BTU?

Solution(s)

$$0.15 [A] 8760 [B] 40 [C] 1 [D] 0.2 [E] [A] [R/S] \text{ -----} > 0.87 \text{ inches}$$

A Ans. 0.87 inches

$$2.5 [D] [A] [R/S] \text{ -----} > 1.90$$

B Ans. 1.90 inches

Reference(s) Mechanical Engineers Handbook, L. Marks, McGraw-Hill 1941, pg 404.

This program is a translation of the HP-65 Users' Program #01621A submitted by John R. Feemster.

[illegible]

17

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11	Const. 3.46 x 10 ⁻³	057	=	-24	Calculate b
002	ST01	35 01		058	ST04	35 04	
003	3	03		059	RTN	24	
004	.	-62		060	*LBLE	21 15	
005	4	04		061	ST07	35 07	
006	6	06		062	R/S	51	
007	EEX	-23		063	RCL2	36 02	
008	3	03		064	RCL5	36 05	
009	CHS	-22		065	x	-35	
010	ST06	35 06		066	RCL4	36 04	
011	RCL1	36 01		067	x	-35	
012	R/S	51		068	RCL3	36 03	
013	RCL2	36 02		069	x	-35	
014	RCL3	36 03		070	RCL1	36 01	
015	x	-35		071	RCL5	36 05	
016	RCL4	36 04		072	6	06	
017	x	-35	073	x	-35		
018	RCL5	36 05	074	+	-55		
019	x	-35	075	RCL6	36 06		
020	RCL7	36 07	076	=	-24		
021	=	-24	077	X ²	53		
022	JX	54	078	=	-24		
023	RCL6	36 06	079	ST07	35 07		
024	x	-35	080	RTN	24		
025	6	06					
026	RCL5	36 05					
027	x	-35					
028	-	-45					
029	ST01	35 01					
030	RTN	24					
031	*LBLB	21 12					
032	ST02	35 02					
033	R↓	-31					
034	ST05	35 05	090				
035	RTN	24					
036	*LBLC	21 13					
037	ST03	35 03					
038	RTN	24					
039	*LBLD	21 14					
040	ST04	35 04					
041	R/S	51					
042	RCL1	36 01					
043	RCL5	36 05					
044	6	06	100				
045	x	-35					
046	+	-55					
047	RCL6	36 06					
048	=	-24					
049	X ²	53					
050	RCL2	36 02					
051	RCL5	36 05					
052	x	-35					
053	RCL3	36 03					
054	x	-35	110				
055	RCL7	36 07					
056	=	-24					

SET STATUS

FLAGS		TRIG	DISP
ON	OFF		
0	<input type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
1	<input type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2	<input type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3	<input type="checkbox"/>		n <u>2</u>

REGISTERS

0	1 Ins.	2 hrs/yr	3 ΔT	4 M	5 k	6 Const	7 b	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

Program Description I

Program Title Heat Transfer Through Composite Cylinders and Walls

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

This program can be used to calculate the overall heat transfer coefficient for composite tubes and walls from individual section conductances and surface coefficients.

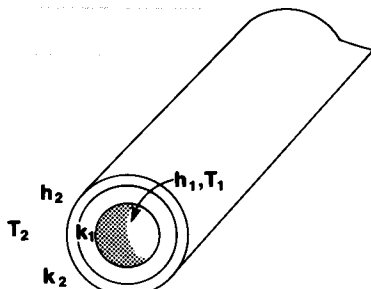


Figure 1.—Composite tube

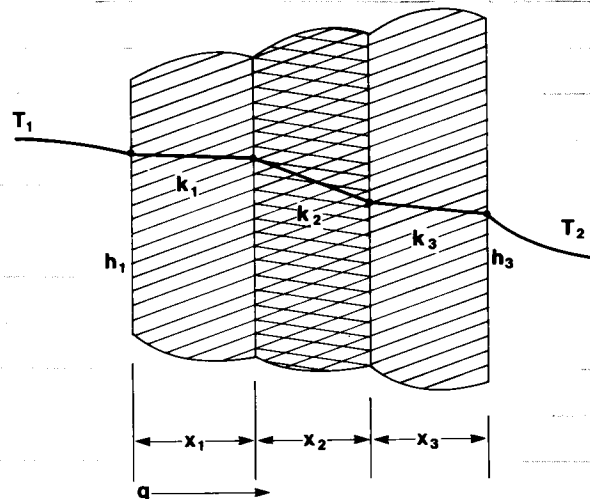


Figure 2.—Composite wall

Operating Limits and Warnings

These equations are for steady state heat transfer through materials with constant properties in all directions.

Inputs must start with the inside convective coefficient and work out in the case of composite cylinders.

Zero is an invalid input for D , k , and h .

Dimensional consistency must be maintained.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description I

Program Title Heat Transfer Through Composite Cylinders and Walls
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

The overall heat transfer coefficient U is defined by:

$$q/L = U \Delta T$$

or

$$q/A = U \Delta T$$

where ΔT is the total temperature difference ($T_2 - T_1$), q/L is the heat transfer per unit length of pipe, and q/A is the heat transfer per unit area of wall.

For cylinders

$$U = \frac{2\pi}{\frac{2}{h_1 D_1} + \frac{\ln D_2/D_1}{k_1} + \frac{\ln D_3/D_2}{k_2} + \dots + \frac{2}{h_n D_n}}$$

For walls

$$U = \frac{1}{\frac{1}{h_1} + \frac{x_1}{k_1} + \frac{x_2}{k_2} + \dots + \frac{1}{h_n}}$$

where

h is the convective surface coefficient;

D_n is the outside diameter of the annulus;

k is the conductive coefficient;

x is the thickness of a wall section.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample Problem(s)

Example 1:

A steel pipe with an inside diameter of 4 inches and a thickness of 0.5 inches has a conductivity of 25 Btu/ft-hr-°F. Two inches of asbestos ($k = 0.1$ Btu/hr-ft-°F) enclose the pipe bringing the total diameter to 9 inches. If the inside convective coefficient is 1000 Btu/hr-ft²-°F and the outside coefficient is 5 Btu/hr-ft²-°F, what is the overall heat transfer coefficient? What is the heat loss for 100 feet of pipe if ΔT is 115°F?

Keystrokes

4 \uparrow 12 \div 1000 **A** 5 \uparrow 12 \div 25 **B** 9 \uparrow 12 \div
0.1 **B** 9 \uparrow 12 \div 5 **A** **C** _____

See Displayed

0.98
Btu/hr-ft-°F

115 ☐ \longrightarrow 112.44
Btu/hr-ft

100 ☒ \longrightarrow 11244.20
Btu/hr

Solution(s)

Example 2:

A wall is composed of 1 foot of brick ($k = 0.4 \text{ Btu/hr-ft}^\circ\text{F}$), and 1 inch of wood ($k = 0.12 \text{ Btu/hr-ft}^\circ\text{F}$). The convective coefficient on one side is $23 \text{ Btu/hr-ft}^2\text{-}^\circ\text{F}$. The convective coefficient of the other side is $5 \text{ Btu/hr-ft}^2\text{-}^\circ\text{F}$. What is the overall coefficient? What is the heat flux if the temperature difference is 70°F ?

Keystrokes

RTN 1 **↑** 0.4 **E** 1 **↑** 12 **÷** .12 **E** 23 **D** 5 **D** **C** **▶** 0.29
Btu/ft²·hr·°F

See Displayed

70 x
→
 20.36
 Btu/ft²·hr

Reference(s)

User Instructions

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COMPOSITE CYLINDERS AND WALLS
 RTN-START D⇑k ⇨U h x⇑k

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Enter program		<input type="text"/> <input type="text"/>	
2	For a composite wall go to		<input type="text"/> <input type="text"/>	
	step 9.		<input type="text"/> <input type="text"/>	
3	Input the inner diameter	D_{in}	<input type="text"/> ↑ <input type="text"/>	D_{in}
4	Input the inner convective		<input type="text"/> <input type="text"/>	
	coefficient	h_{in}	<input type="text"/> A <input type="text"/>	$2/hD$
5	Input next diameter value	D	<input type="text"/> ↑ <input type="text"/>	D
	and corresponding coefficient	k or h	<input type="text"/> B <input type="text"/>	
6	Go to step 5 for next surface		<input type="text"/> <input type="text"/>	
	or go to step 3 for outside		<input type="text"/> <input type="text"/>	
	surface*		<input type="text"/> <input type="text"/>	
7	Calculate overall heat transfer		<input type="text"/> <input type="text"/>	
	coefficient		<input type="text"/> C <input type="text"/>	U
8	To calculate another overall		<input type="text"/> <input type="text"/>	
	coefficient, go to step 2		<input type="text"/> <input type="text"/>	
9	Input the coefficients for each		<input type="text"/> <input type="text"/>	
	section of the wall:		<input type="text"/> <input type="text"/>	
	Convective coefficient	h	<input type="text"/> D <input type="text"/>	$1/h$
	or length of conductive path	x	<input type="text"/> ↑ <input type="text"/>	
	and conductive coefficient	k	<input type="text"/> E <input type="text"/>	x/k
10	Go to step 9 for next input*		<input type="text"/> <input type="text"/>	
11	Calculate overall heat transfer		<input type="text"/> <input type="text"/>	
	coefficient		<input type="text"/> C <input type="text"/>	U
12	To calculate another overall		<input type="text"/> <input type="text"/>	
	coefficient, go to step 2		<input type="text"/> <input type="text"/>	

* Press **RTN** to restart a calculation.

97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11	Initialize				
002	Pi	16-24					
003	ST06	35 06		060			
004	CLX	-51					
005	ST08	35 08					
006	R↓	-31					
007	XZY	-41					
008	ST07	35 07					
009	XZY	-41					
010	GTOA	22 11	Idle				
011	*LBL1	21 01					
012	RTN	24					
013	*LBLA	21 11		070			
014	X	-35					
015	1/X	52					
016	ST+8	35-55 08					
017	RTN	24					
018	*LBLB	21 12					
019	1/X	52	Add convective factor				
020	XZY	-41					
021	RCL7	36 07					
022	XZY	-41					
023	ST07	35 07		080			
024	=	-24					
025	LN	32					
026	X	-35					
027	2	02					
028	=	-24	Add conductive factor				
029	ST-8	35-45 08					
030	GTO1	22 01					
031	*LBLC	21 13					
032	RCL8	36 08					
033	1/X	52					
034	RCL6	36 06		090			
035	X	-35					
036	ST04	35 04					
037	RTN	24	Add convective factors				
038	*LBLD	21 14					
039	1	01					
040	XZY	-41					
041	*LBLE	21 15					
042	1	01					
043	ST06	35 06					
044	CLX	-51		100			
045	ST08	35 08					
046	R↓	-31	Calculate U				
047	GTOE	22 15					
048	*LBL2	21 02					
049	RTN	24					
050	*LBLE	21 15					
051	XZY	-41					
052	=	-24					
053	*LBLD	21 14					
054	1/X	52		110			
055	ST+8	35-55 08	Add conductive factors				
056	GTO2	22 02					

REGISTERS									
0	1	2	3	4	5	6	7	8	9
				U		1 or π	Used	ΣR	
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A		B		C		D		E	
								I	

FLAGS				SET STATUS			
0				1			

Program Description I

Program Title Steady State Conductive Heat Transfer, Heat Load and Logarithmic Mean Temperature Difference

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

Given any Three variables

$$(Q, U, A\Delta t_m) \text{ OR } (Q, W, C_p\Delta t)$$

The Program Computes the Fourth Variables:

$$Q = UA\Delta t_m, \quad U = \frac{Q}{A\Delta t_m}, \dots \text{etc.}$$

$$Q = WC_p\Delta t, \quad C_p = \frac{Q}{W\Delta t}, \dots \text{etc}$$

Given Temperature Conditions

$$(T_1, T_2, t_1 \text{ \& } t_2), (t_1 \text{ \& } t_2) \text{ or } (T_1 \text{ \& } T_2)$$

The Program Computes:

$$\text{OR } \Delta t_m = \frac{\Delta_2 - \Delta_1}{\ln(\Delta_2 / \Delta_1)}$$

$$\Delta t = (t_2 - t_1), (T_2 - T_1).$$

To combine these three basic heat transfer equations will increase the flexibility and speed of heat transfer design.

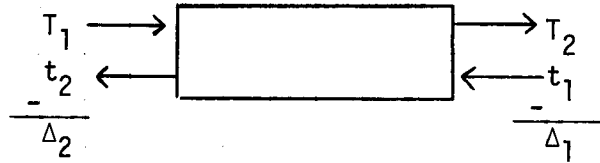
Operating Limits and Warnings

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)



Sample Problem(s) Determine U of an existing exchanger for the following data
(Represented by the Above Sketch):

$W = 247,000$ lb per hr
 $C_p = 0.585$ Btu/(lb)(°F)
 $T_1 = 410^\circ\text{F}$
 $T_2 = 150^\circ\text{F}$
 $t_1 = 100^\circ\text{F}$
 $t_2 = 347.5^\circ\text{F}$
 $A = 9390$ sq ft

Flow Rate
 Heat Capacity of the Fluid
 Hot Inlet Temperature
 Hot Outlet Temperature
 Cold Inlet Temperature
 Cold Outlet Temperature
 Heat Transfer Area

Solution(s)

$Q = 37,568,700$ Btu/hr
 $\Delta t_m = 56^\circ\text{F}$
 $U = 71.42$ Btu/(hr)(°F)(sq ft)

Duty
 Mean Temperature Difference
 Heat Transfer coefficient

Keystrokes:

247000[B] 0.585[C] 410[ENT+] 150[←] [D] 0[A]
 410[ENT+] 347.5[ENT+] 150[ENT+] 100[E]
 [D] 9390[C] 0[B]

Output:

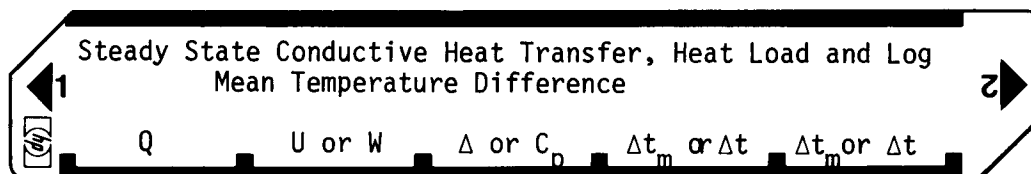
37568700(Q)
 56.02 (Δt_m)
 71.42 (U)

Reference(s) McAdams, W.H., Heat Transmission, McGraw-Hill Book Co.

This program is a translation of the HP-65 Users' Library program #00648A
 submitted by Yu Tsung Pei.

User Instructions

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STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1.	Load program		<input type="button" value="C"/> <input type="button" value="D"/>	
2.	Compute Q		<input type="button" value="C"/> <input type="button" value="D"/>	
	Input U Btu/(hr)(°F)(sq ft) or W lb/hr	U or W	<input type="button" value="B"/> <input type="button" value="C"/>	U or W
	Input A sq ft or C _p Btu/(lb)(°F)	A or C _p	<input type="button" value="C"/> <input type="button" value="D"/>	A or C _p
	Input Δt _m °F or Δt °F	Δt _m or Δt	<input type="button" value="D"/> <input type="button" value="C"/>	Δt _m or Δt
2.	Compute U or W		<input type="button" value="C"/> <input type="button" value="D"/>	
	Input Q Btu/hr	Q	<input type="button" value="A"/> <input type="button" value="B"/>	Q
	Input A sq ft or C _p Btu/(lb)(°F)	A or C _p	<input type="button" value="C"/> <input type="button" value="D"/>	A or C _p
	Input Δt _m °F or Δt °F	Δt _m or Δt	<input type="button" value="D"/> <input type="button" value="C"/>	Δt _m or Δt
2.	Compute A or C _p		<input type="button" value="O"/> <input type="button" value="B"/>	U or W
	Input Q Btu/hr	Q	<input type="button" value="A"/> <input type="button" value="B"/>	Q
	Input U Btu/(hr)(°F)(sq ft) or W lb/hr	U or W	<input type="button" value="B"/> <input type="button" value="C"/>	U or W
	Input Δt _m °F or Δt °F	Δt _m or Δt	<input type="button" value="D"/> <input type="button" value="C"/>	Δt _m or Δt
2.	Compute t _m or t		<input type="button" value="O"/> <input type="button" value="C"/>	A or C _p
	Input Q Btu/hr	Q	<input type="button" value="A"/> <input type="button" value="B"/>	Q
	Input U Btu/(hr)(°F)(sq ft) or W lb/hr	U or W	<input type="button" value="B"/> <input type="button" value="C"/>	U or W
	Input A sq ft or C _p Btu/(lb)(°F)	A or C _p	<input type="button" value="C"/> <input type="button" value="D"/>	A or C _p
3.	Compute Δt _m or Δt from T ₁ , T ₂ , t ₁ & t ₂		<input type="button" value="O"/> <input type="button" value="D"/>	Δt _m or Δt
	T ₁ T ₂	T ₁	<input type="button" value="↑"/> <input type="button" value="↓"/>	T ₁
	t ₂ t ₁	t ₂	<input type="button" value="↑"/> <input type="button" value="↓"/>	t ₂
		T ₂ or t ₂	<input type="button" value="↑"/> <input type="button" value="↓"/>	T ₂ or t ₂
		t ₁ or t ₁	<input type="button" value="E"/> <input type="button" value="C"/>	Δt _m or Δt

97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS																								
001	*LBLA	21 11	Compute the Q	057	*LBL0	21 00	$T_1 - t_2 = \Delta_2$ $T_2 - t_1 = \Delta_1$ $\Delta_2 = \Delta_1 = \Delta t_m$																								
002	0	00		058	-	-45																									
003	X \div Y	-41		059	R \uparrow	16-31																									
004	X \times Y?	16-32		060	X=Y?	16-33																									
005	GT01	22 01		061	R/S	51																									
006	RCL2	36 02		062	X \div Y?	16-35																									
007	RCL3	36 03		063	X \div Y	-41																									
008	RCL4	36 04		064	ST05	35 05																									
009	X	-35		065	ST06	35 06																									
010	X	-35		066	R \downarrow	-31																									
011	ST01	35 01	Compute the U or W	067	ST-5	35-45 05																									
012	RTN	24		068	ST-6	35-24 06																									
013	*LBLB	21 12		069	RCL5	36 05																									
014	0	00		070	RCL6	36 06																									
015	X \div Y	-41		071	LN	32																									
016	X \times Y?	16-32		072	\div	-24																									
017	GT02	22 02		073	ST04	35 04																									
018	RCL1	36 01		074	RTN	24																									
019	RCL3	36 03		075	*LBL1	21 01																									
020	RCL4	36 04		076	ST01	35 01																									
021	X	-35	Compute the A or C	077	R/S	51																									
022	\div	-24		078	*LBL2	21 02																									
023	ST02	35 02		079	ST02	35 02																									
024	RTN	24		080	R/S	51																									
025	*LBLC	21 13		081	*LBL3	21 03																									
026	0	00		082	ST03	35 03																									
027	X \div Y	-41		083	R/S	51																									
028	X \times Y?	16-32		084	*LBL4	21 04																									
029	GT03	22 03		085	ST04	35 04																									
030	RCL1	36 01		086	R/S	51																									
031	RCL2	36 02	Compute Δt_m or Δt				<div>SET STATUS</div> <table><tr><th colspan="2">FLAGS</th><th>TRIG</th><th>DISP</th></tr><tr><td>ON</td><td>OFF</td><td></td><td></td></tr><tr><td>0</td><td><input checked="" type="checkbox"/></td><td>DEG <input checked="" type="checkbox"/></td><td>FIX <input checked="" type="checkbox"/></td></tr><tr><td>1</td><td><input checked="" type="checkbox"/></td><td>GRAD <input type="checkbox"/></td><td>SCI <input type="checkbox"/></td></tr><tr><td>2</td><td><input checked="" type="checkbox"/></td><td>RAD <input type="checkbox"/></td><td>ENG <input type="checkbox"/></td></tr><tr><td>3</td><td><input checked="" type="checkbox"/></td><td></td><td>n <u>2</u></td></tr></table>	FLAGS		TRIG	DISP	ON	OFF			0	<input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>	1	<input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>	2	<input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>	3	<input checked="" type="checkbox"/>		n <u>2</u>
FLAGS		TRIG		DISP																											
ON	OFF																														
0	<input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>		FIX <input checked="" type="checkbox"/>																											
1	<input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>		SCI <input type="checkbox"/>																											
2	<input checked="" type="checkbox"/>	RAD <input type="checkbox"/>		ENG <input type="checkbox"/>																											
3	<input checked="" type="checkbox"/>			n <u>2</u>																											
032	RCL4	36 04																													
033	X	-35																													
034	\div	-24																													
035	ST03	35 03																													
036	RTN	24																													
037	*LBLD	21 14																													
038	0	00																													
039	X \div Y	-41																													
040	X \times Y?	16-32																													
041	GT04	22 04	Compute Δt_m or Δt from T_1, T_2, t_1 or t_2																												
042	RCL1	36 01																													
043	RCL2	36 02																													
044	RCL3	36 03																													
045	X	-35																													
046	\div	-24																													
047	ST04	35 04																													
048	RTN	24																													
049	*LBLE	21 15																													
050	-	-45																													
051	R \downarrow	-31																													
052	X \times Y?	16-32																													
053	GT00	22 00																													
054	R \uparrow	16-31																													
055	ST04	35 04																													
056	RTN	24																													
REGISTERS																															
0	1 Q	2 U, W	3 A, C _p	4 $\Delta t_m, \Delta t$	5 Δ_1	6 Δ_2	7	8	9																						
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9																						
A	B	C	D	E	I																										

Program Description I

Program Title Sun Altitude, Azimuth, Solar Pond Absorption

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

Given: Index of refraction of pond fluid; latitude; number of days after spring equinox, and number of hours before or after solar noon;
the program computes: the sun's altitude h.

$$h = \sin^{-1}(\cos l \cos d \cos t + \sin l \sin d)$$

l - latitude in decimal degrees

d = sun's declination = $23.45 \sin D$

D = (no. of days after spring equinox)($0.9856 \frac{\text{degrees}}{\text{day}}$)

t = (no. of hours before or after solar noon);

the sun's azimuth A.

$$A = \cos^{-1} \left(\frac{\cos i \sin l - \sin d}{\cos l \sin i} \right)$$

$i = 90 - h$;

the fraction of solar radiation striking the pond surface
which will penetrate the pond surface, E,

$$\text{Fraction } E = 2n(a^2 + b^2) \cos i \cos r$$

$$a = \frac{1}{\cos r + n \cos i} \text{ where } r = \sin^{-1} \left(\frac{\sin i}{n} \right)$$

$$b = \frac{1}{\cos i + n \cos r}$$

n = index of refraction of pond fluid

(refs: Smithsonian Physical Tables, 9th rev. Ed. & Weinberger, H., Solar energy, v8, n2,
1954 (p 729) 1964 (pp 45-56)

OPERATING LIMITS AND WARNINGS

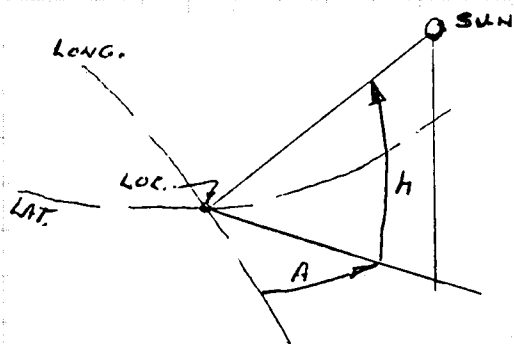
Does not compute azimuth at latitude of 90 degrees.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)



Sample Problem(s)

Find the sun's altitude, azimuth, and the fraction of the sun's radiation which will penetrate the surface of a solar pond under the following circumstances:

Index of refraction of pond fluid $n = 1.33$

Latitude $l = 46.00$

Days after spring equinox = 68

Hours before solar noon = 4

Solution(s)

$h = 35.99$ degrees

$A = 84.41$ degrees

$E = 0.96$

Keystrokes:

23.45[STO][1] .9856[STO][2] 1.33[STO][3]

46[A] 68[B] 4[C] ----->

[R/S] ----->

[R/S] ----->

Outputs:

35.99

84.41

0.96

Reference(s)

Smithsonian Physical Tables, 9th rev. Ed., 1954, (p 729)

Weinberger, H., Solar Energy, vol 8, no. 2, 1964 (pp 45-56)

This program is a translation of the HP-65 Users' Library program #00683A submitted by Robert J. Zaworski.

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[illegible]

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLE	21 11		057	GSBE	23 15	
002	COS	42		058	RCL6	36 06	
003	ST04	35 04	cos l in 4	059	RCL7	36 07	
004	LSTX	16-63		060	RCL3	36 03	
005	RTN	24		061	GSBE	23 15	
006	*LBLE	21 12	stops with latitude	062	+	-55	
007	RCL2	36 02	in x	063	RCL3	36 03	
008	X	-35		064	X	-35	
009	SIN	41		065	2	02	
010	RCL1	36 01		066	X	-35	
011	X	-35		067	RCL6	36 06	
012	ST05	35 05	d in 5	068	X	-35	
013	RTN	24		069	RCL7	36 07	
014	*LBLC	21 13	stops with decl.in x	070	X	-35	
015	1	01		071	RTN	24	
016	5	05		072	*LBLC	21 14	
017	X	-35		073	COS-	16 42	
018	COS	42		074	SIN	41	
019	ST08	35 08		075	RTN	24	
020	RCL4	36 04		076	*LBLE	21 15	
021	X	-35		077	X	-35	
022	RCL5	36 05		078	+	-55	
023	COS	42		079	ENT1	-21	
024	X	-35		080	X	-35	
025	RCL4	36 04		081	1/X	52	
026	GSBD	23 14		082	RTN	24	
027	RCL5	36 05		083	R/S	51	
028	SIN	41					
029	ST07	35 07					
030	X	-35					
031	+	-55					
032	ST06	35 06					
033	SIN-	16 41	Stops with alt. in x				
034	R/S	51					
035	RCL6	36 06					
036	RCL4	36 04					
037	GSBD	23 14					
038	X	-35					
039	RCL7	36 07					
040	-	-45					
041	RCL4	36 04					
042	=	-24					
043	RCL6	36 06					
044	GSBD	23 14					
045	=	-24					
046	COS-	16 42	Stops with azimuth				
047	R/S	51	in x				
048	RCL6	36 06					
049	GSBD	23 14					
050	RCL3	36 03					
051	=	-24					
052	SIN-	16 41					
053	COS	42					
054	ST07	35 07	cos r in 7				
055	RCL6	36 06					
056	RCL3	36 03					

SET STATUS				
FLAGS		TRIG	DISP	
ON	OFF			
0	<input type="checkbox"/>	<input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
1	<input type="checkbox"/>	<input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2	<input type="checkbox"/>	<input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3	<input type="checkbox"/>	<input checked="" type="checkbox"/>		n-2

REGISTERS								
0	1	2	3	4	5	6	7	8
	23.45	20.9856	n (index	cos l	d	cos i	sin d/cos r	cos t
		deg/day	of refrac		declination			
S0	S1	S2	S3	S4	S5	S6	S7	S8
A	B	C	D	E	I			

Program Description I

Program Title Total Daily Amount of Solar Radiation

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 9733

Program Description, Equations, Variables This program determines the total amount of solar radiation received by a horizontal surface of unit area during one calendar day. The result is expressed as equivalent hours of direct sunshine if sun were stationary and directly overhead. Also computes length of daylight and accumulates total radiation in R7 for successive calculations. Input variables are latitude, L, suns declination (from nautical almanac) in decimal degrees.

Day Length = $24 \theta / \pi$, θ expressed in radians

$\theta = \text{Arc cos } (-\sin L \sin D / \cos L \cos D)$

Total Radiation = $2 \int_0^\theta \sin H d\theta$

= $(\sin L \sin D) \theta + \cos L \cos D \sin \theta$

Operating Limits and Warnings

North latitudes and declinations are entered as positive values south as negative values.

The value $90-L+D$ must be greater than zero.

Equations assume surface level with horizon and ignores atmospheric refraction and assume cloudless sky.

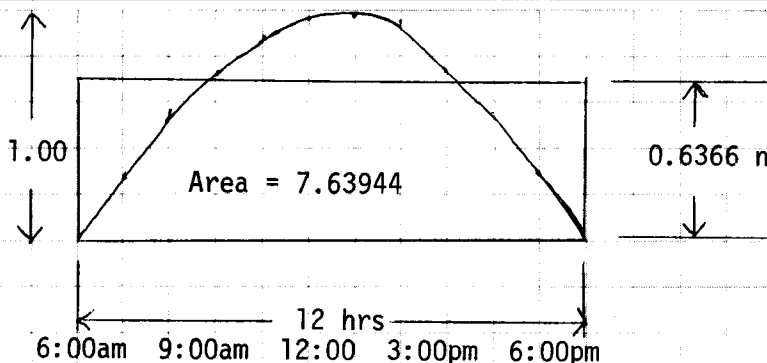
This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample (1)



Sample Problem(s)

- (1) Equator, March 21 $L = 0$, $D = 0$
- (2) North Pole, June 21, $L = 90^\circ$, $D = +23.45^\circ$
- (3) Cupertino, CA 95014, September 15, 1974
 $L = 37.32^\circ$, $Dec = +2.93^\circ$

Solution(s)

- (1) DHY length = 12.00 hrs Total Rad = 7.6394 hrs
- (2) " " = 24.00 " " " = 9.5508
- (3) " " = 12 hrs, 17 min, 53 sec. Total Rad = 6.4439

Keystrokes:

```
(1) 0[E] 0[A] 0[B] -----
    [C] -----
(2) 0[E] 90[A] 23.45[B] -----
    [C] -----
(3) 0[E] 37.32[A] 2.93[B] -----
    [C] -----
```

Outputs:

```
12.0000
 7.6394
24.0000
 9.5508
12.1753
 6.4439
```

Reference(s)

- (1) The Nautical Almanac, U.S. Naval Observatory Purchase from Superintendent of Documents, Washington D.C., 20402.
- (2) American Practical Navigation, Bowditch U.S. Naval Oceanographic Office, pg 531, Also chapter XIV.
- (3) Britannica Atlas

This program is a translation of the HP-65 Users' Library program 00996A
submitted by Robert B. Egbert.

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[illegible]

97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS		
001	*LBLA	21 11	Enter latitude & store in R-1	057	ENT↑	-21	Display sums accumulated in R-7		
002	DSP4	-63 04		058	RCL7	36 07			
003	ST01	35 01		059	+	-55			
004	R/S	51	Enter sums dec- lination and compute no. of hours of sunshine	060	ST07	35 07	Stores zero in R-7 for new series of calculations Limits of integra- tion for midnight s or case		
005	*LBLB	21 12		061	R↓	-31			
006	ST02	35 02		062	R/S	51			
007	DEG	16-21		063	*LBLD	21 14			
008	RCL1	36 01		064	RCL7	36 07			
009	SIN	41		065	R/S	51			
010	RCL2	36 02		066	*LBLE	21 15			
011	SIN	41		067	0	00			
012	X	-35		068	ST07	35 07			
013	ST03	35 03		069	R/S	51			
014	RCL1	36 01	This takes care of midnight sun	070	*LBL1	21 01			
015	COS	42		071	2	02			
016	RCL2	36 02		072	4	04			
017	COS	42		073	ST05	35 05			
018	X	-35		074	R/S	51			
019	ST04	35 04							
020	X↔Y?	16-35							
021	ST01	22 01							
022	RCL3	36 03							
023	RCL4	36 04							
024	=	-24	080						
025	CHS	-22							
026	COS↑	16 42							
027	7	07							
028	.	-62							
029	5	05	Converts degrees (θ) to length of day in hr, min,sec						
030	=	-24							
031	ST05	35 05							
032	→HMS	16 35							
033	R/S	51							
034	*LBLC	21 13		090					
035	RCL5	36 05							
036	PI	16-24							
037	X	-35							
038	2	02							
039	4	04							
040	=	-24							
041	ST06	35 06							
042	RAD	16-22							
043	RCL3	36 03							
044	RCL6	36 06	100						
045	X	-35							
046	RCL4	36 04							
047	RCL6	36 06							
048	SIN	41							
049	X	-35							
050	+	-55							
051	2	02							
052	4	04							
053	X	-35							
054	PI	16-24	110						
055	=	-24							
056	ENT↑	-21							
SET STATUS									
				FLAGS		TRIG	DISP		
				ON OFF		DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>		
				0 <input type="checkbox"/> <input checked="" type="checkbox"/>		GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>		
				1 <input type="checkbox"/> <input checked="" type="checkbox"/>		RAD <input type="checkbox"/>	ENG <input type="checkbox"/>		
				2 <input type="checkbox"/> <input checked="" type="checkbox"/>		n—2			
				3 <input type="checkbox"/> <input checked="" type="checkbox"/>					
REGISTERS									
0	1 LAT	2 DEC OF SUN	3 Sin Lx Sin D	4 cos Lx cos D	5 θ HOURS OF SUNSHINE	6 θ RADIANS	7 $\int \sin H d\theta$	8	9
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

SET STATUS		
FLAGS	TRIG	DISP
ON OFF		
0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n—2—

Program Description I

Program Title Temperature or Concentration Profile For A Semi-Infinite Solid

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

Many physical situations in heat and mass transfer may be solved within engineering tolerances by assuming an infinite geometry.

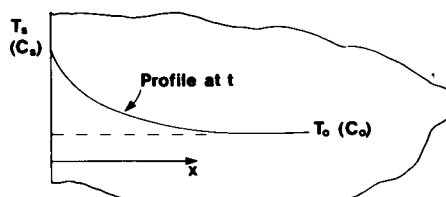


Figure 1.

In Figure 1 an infinitely thick wall initially at temperature T_0 or concentration C_0 is subject to a constant surface potential T_s or C_s . At a later time t , the internal profile will have been altered by the transport of heat or mass. This program computes values of temperature T or concentration C at time t for specified distances x from the outer surface.

Operating Limits and Warnings

This solution is exact for infinite configurations with constant cross sectional areas. However, finite geometries where the argument of the error function is greater than two will yield little or no error. This means transfer in finite bodies such as plates may be predicted until the effects of the step are felt on the far side. Also, geometries such as cylinders may be studied if the depth of penetration is small compared to the radius.

The routine used by this program will resolve error functions with arguments less than 4.5. For larger arguments, the value of the error function is set to 1.0.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description I

Program Title Temperature or Concentration Profile For A Semi- Infinite Solid

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

Equations:

$$T = (T_0 - T_s) \operatorname{erf} \left(\frac{x}{2 \sqrt{\frac{k}{\rho c_p} t}} \right) + T_s^*$$

where

k is thermal conductivity of the material;

ρ is the density of the material;

c_p is the specific heat of the material;

$k/\rho c_p$ is also known as the diffusivity of heat α .

Similarly, for mass transfer

$$C = (C_0 - C_s) \operatorname{erf} \left(\frac{x}{2 \sqrt{Dt}} \right) + C_s^*$$

where

D is the mass diffusivity.

*erf is the error function.

Operating Limits and Warnings

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

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Sketch(es)

Example 1:

A large steel transmission shaft is case hardened by diffusion of carbon. The initial carbon concentration is 0.10% and the surface concentration is brought to 1.20% almost instantly. What is the carbon concentration at 1.0 mm (1×10^{-3} m) after 15 hours (54000 seconds), if the diffusivity of carbon in steel is taken to be 1.6×10^{-11} m²/s?

Keystrokes

See Displayed

1.6 [EEX] [CHS] 11 [↑] 1 [↑] 1 [A] 1.2 [↑] .1 [B] 54000

[C] [EEX] [CHS] 3 [D] → 0.59%

Example 2:

A furnace wall is at a constant 55°F. When the furnace is turned on the inside wall temperature is raised to 2000°F. How long will it take to raise the outside wall temperature 1°F?

$$k = 0.67 \text{ Btu/hr-ft-}^\circ\text{F}$$

$$\text{Thickness} = 1.5 \text{ feet}$$

$$c = 0.2 \text{ Btu/lb } ^\circ\text{F}$$

$$\rho = 150 \text{ lb/ft}^3$$

Keystrokes

See Displayed

An iterative solution is required since t is not a program output. Guess 5.0 hours for t.

.67 [↑] 150 [↑] .2 [A] 2000 [↑] 55 [B] 5 [C] 1.5 [D] → 57.92°F

Guess 4.0

Noting that x is stored in register 8.

4.0 [C] [RCL] [8] [D] → 55.75°F

Guess 4.2

4.2 [C] [RCL] [8] [D] → 56.04°F


Guess 4.18

4.18 [C] [RCL] [8] [D] → 56.01°F

Noting that t is stored in register 7.

[RCL] [7] [f] [→H.MS] → ≈ 4 hr. 10 min.

User Instructions

SEMI-INFINITE SOLID				
	$k \leftrightarrow \rho \leftrightarrow c_p$ ($D \leftrightarrow 1 \leftrightarrow t$)	$T_s \leftrightarrow T_0$ ($c_s \leftrightarrow c_o$)	t	$x \leftrightarrow T(C) \quad a \leftrightarrow \text{erf}(a)$

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Enter program		<input type="text"/> <input type="text"/>	
2	To compute the error function		<input type="text"/> <input type="text"/>	
	of an argument go to step 8.		<input type="text"/> <input type="text"/>	
3	Input:		<input type="text"/> <input type="text"/>	
	Conductivity	k	<input type="text"/> <input type="text"/>	k
	then density	ρ	<input type="text"/> <input type="text"/>	ρ
	then specific heat	c_p	<input type="text"/> A <input type="text"/>	α
	or heat (or mass) diffusivity	α (D)	<input type="text"/> <input type="text"/>	α (D)
	then 1.00	1	<input type="text"/> <input type="text"/>	1.00
	then 1.00	1	<input type="text"/> A <input type="text"/>	α (D)
4	Input:		<input type="text"/> <input type="text"/>	
	Surface temperature (con-		<input type="text"/> <input type="text"/>	
	centration)	T_s (C_s)	<input type="text"/> <input type="text"/>	T_s (C_s)
	then initial temperature		<input type="text"/> <input type="text"/>	
	(concentration)	T_0 (C_0)	<input type="text"/> B <input type="text"/>	T_s (C_s)
5	Input time	t	<input type="text"/> C <input type="text"/>	t
6	Input distance from surface		<input type="text"/> <input type="text"/>	
	and calculate temperature		<input type="text"/> <input type="text"/>	
	or concentration	x	<input type="text"/> D <input type="text"/>	T (C)
7	For new case go to step 2, 3, or		<input type="text"/> <input type="text"/>	
	4 and change inputs. For new		<input type="text"/> <input type="text"/>	
	time go to step 5. For new x go		<input type="text"/> <input type="text"/>	
	to step 6.		<input type="text"/> <input type="text"/>	
8	Input argument and compute		<input type="text"/> <input type="text"/>	
	error function	a	<input type="text"/> E <input type="text"/>	erf(a)

97 Program Listing I

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STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11		057	+	-55	
002	x	-35		058	X*Y?	16-32	
003	=	-24	Store constants as	059	GT01	22 01	
004	ST06	35 06	α or D	060	2	02	
005	RTN	24		061	x	-35	
006	*LBLB	21 12		062	Pi	16-24	
007	ST04	35 04	Store concentrations	063	JX	54	
008	X*Y	-41	or temperatures	064	=	-24	
009	ST05	35 05		065	RCL2	36 02	
010	RTN	24		066	2	02	
011	*LBLC	21 13		067	=	-24	
012	ST07	35 07	Store time	068	e ^x	33	
013	RTN	24		069	=	-24	
014	*LBLD	21 14		070	RTN	24	
015	ST08	35 08		071	*LBL0	21 00	
016	2	02		072	1	01	
017	=	-24		073	RTN	24	
018	RCL6	36 06	Calculate temp. or				
019	RCL7	36 07	concentration given x				
020	x	-35					
021	JX	54					
022	=	-24					
023	GSBE	23 15					
024	RCL4	36 04		080			
025	RCL5	36 05					
026	-	-45					
027	x	-35					
028	RCL5	36 05					
029	+	-55					
030	RTN	24					
031	*LBLE	21 15					
032	ST01	35 01					
033	4	04					
034	.	-62		090			
035	5	05					
036	X*Y?	16-35					
037	GT06	22 00					
038	R↓	-31					
039	ENT↑	-21					
040	x	-35					
041	2	02					
042	x	-35					
043	ST02	35 02					
044	1	01		100			
045	ST03	35 03					
046	RCL1	36 01					
047	*LBL1	21 01					
048	RCL2	36 02					
049	RCL3	36 03					
050	2	02	Evaluate the error				
051	+	-55	function				
052	ST03	35 03					
053	=	-24					
054	RCL1	36 01		110			
055	x	-35					
056	ST01	35 01					

SET STATUS								
FLAGS			TRIG		DISP			
ON	OFF							
0	<input type="checkbox"/>	<input checked="" type="checkbox"/>	DEG	<input checked="" type="checkbox"/>	FIX	<input checked="" type="checkbox"/>		
1	<input type="checkbox"/>	<input checked="" type="checkbox"/>	GRAD	<input type="checkbox"/>	SCI	<input type="checkbox"/>		
2	<input type="checkbox"/>	<input checked="" type="checkbox"/>	RAD	<input type="checkbox"/>	ENG	<input type="checkbox"/>		
3	<input type="checkbox"/>	<input checked="" type="checkbox"/>			n	2		

REGISTERS									
0	1	2	3	4	5	6	7	8	9
Part. Sum	2a ²	2n + 1	T ₀ (C ₀)	T _s (C _s)	α	t	x	Used	
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

Program Description I

Program Title Transient Temperature Distribution In A Semi-Infinite Solid With Convection Boundary Condition
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

Given the data set:

x = Depth from surface

α = Thermal diffusivity

k = Thermal conductivity

h = Heat transfer coefficient

θ = Time

The program computes the following factor \bar{x}

$$\bar{x} = \text{ERF} \left(\frac{x}{2\sqrt{\alpha\theta}} \right) + \left[\text{EXP} \left(\frac{hx}{k} + \frac{h^2\alpha\theta}{k^2} \right) \right] \left[1 - \text{ERF} \left(\frac{x}{2\sqrt{\alpha\theta}} + \frac{h\sqrt{\alpha\theta}}{k} \right) \right]$$

where ERF = Error function

EXP = Exponential

The user must then manually compute the desired temperature $T(x,\theta)$, according to:

$$T(x,\theta) = T_{\infty} + (T_i - T_{\infty}) \bar{x}$$

where T_{∞} = Sink temperature

T_i = Initial solid temperature

Operating Limits and Warnings

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample Problem(s)

For the data set:

$$x = 10^{-2} \text{ cm.}$$

$$\theta = 10^{-1} \text{ cm.}$$

$$\alpha = 7.141 \times 10^{-3} \text{ cm}^2 \text{ sec}^{-1}$$

$$k = 6.322 \times 10^{-3} \text{ cal cm}^{-1} \text{ sec}^{-1} \text{ } ^\circ\text{C}^{-1}$$

$$h = 6.0 \times 10^{-1} \text{ cal cm}^{-2} \text{ sec}^{-1} \text{ } ^\circ\text{C}^{-1}$$

Solution(s) The program computes the value:

$$\bar{x} = 0.3973$$

$$\text{for } T_i = 1050^\circ\text{C and } T_\infty = 450^\circ\text{C}$$

$$T(x, \theta) = T_\infty + (T_i - T_\infty) \bar{x} = 688.40^\circ\text{C}$$

Keystrokes:

Outputs:

1[EEX][CHS] 2[STO][4] 1[EEX][CHS] 1[STO][5] 7.141[EEX][CHS] 3[STO][6]

6[EEX][CHS] 1[STO] [7] 6.322[EEX][CHS] 3[STO][8]

[A][B][C][D] -----> 0.3973

1050[ENT+] 450[-][x] 450[+] ----->688.40

Reference(s)

Hockman, J.P. Heat Transfer Third Edition pgs. 91-96 McGraw Hill, 1972

This program is a translation of the HP-65 Users' Library program #01472A submitted by John S. Wasylyr.

97 Program Listing I

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STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11		057	*LBLC	21 13	Calc
002	RCL8	36 08		058	1	01	$\text{ERFC}(\frac{x}{2\sqrt{\alpha\theta}} + \frac{h\sqrt{\alpha\theta}}{k})$
003	ST \div 7	35-24 07	Calc (h/k) Sto R-7	059	X \div Y	-41	
004	RCL6	36 06		060	-	-45	
005	ST \times 5	35-35 05	Calc ($\alpha\theta$) Sto R-5	061	ST08	35 08	Store R-8
006	RCL4	36 04		062	RCL7	36 07	
007	RCL7	36 07		063	RCL5	36 05	
008	X	-35		064	JX	54	
009	ST06	35 06	Calc (hx/k) Sto R-6	065	X	-35	
010	RCL4	36 04		066	X 2	53	Calc ($\frac{hx}{k} + \frac{h^2x\theta}{k^2}$)
011	2	02		067	RCL6	36 06	EXP
012	\div	-24		068	+	-55	
013	RCL5	36 05		069	e x	33	
014	JX	54		070	RCL8	36 08	Calc (EXP)(ERFC)
015	\div	-24		071	X	-35	Sto R-8
016	ST04	35 04	Calc ($4/2\sqrt{\alpha\theta}$) Sto R-4	072	ST08	35 08	
017	RCL7	36 07		073	RCL4	36 04	Calc. ERF ($\frac{x}{2\sqrt{\alpha\theta}}$)
018	RCL5	36 05		074	GT06	22 12	
019	JX	54		075	RTN	24	
020	X	-35		076	*LBLD	21 14	Calc
021	+	-55	Calc ($x/2\sqrt{\alpha\theta} + h\sqrt{\alpha\theta}/k$)	077	RCL8	36 08	ERF + (EXP)(ERFC)
022	RTN	24		078	+	-55	
023	*LBLB	21 12		079	RTN	24	
024	ST01	35 01	Calc	080			
025	ENT1	-21	ERF($x/2\sqrt{\alpha\theta} + h\sqrt{\alpha\theta}/k$)				
026	X	-35					
027	2	02					
028	X	-35					
029	ST02	35 02					
030	1	01					
031	ST03	35 03					
032	RCL1	36 01					
033	*LBL1	21 01					
034	RCL2	36 02		090			
035	RCL3	36 03					
036	2	02					
037	+	-55					
038	ST03	35 03					
039	\div	-24					
040	RCL1	36 01					
041	X	-35					
042	ST01	35 01					
043	+	-55					
044	X \div Y?	16-32					
045	GT01	22 01		100			
046	2	02					
047	X	-35					
048	Pi	16-24					
049	JX	54					
050	RCL2	36 02					
051	2	02					
052	\div	-24					
053	e x	33					
054	X	-35		110			
055	\div	-24					
056	RTN	24					

SET STATUS		
FLAGS	TRIG	DISP
ON OFF		
0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n _____

REGISTERS									
0	1 Used	2 Used	3 Used	4 x	5 α	6 θ	7 h	8 k	9 Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

Program Description I

Program Title Conservation of Energy
Contributor's Name Hewlett-Packard
Address 1000 N.E. Circle Blvd.
City Corvallis **State** Oregon **Zip Code** 97330

Program Description, Equations, Variables

These cards convert kinetic energy, potential energy and pressure-volume work to energy. Card 1 is for English units while Card 2 is for SI or metric units. Energy is stored as a running total. When a zero is displayed, pressing the **B**, **C**, **D** or **E** keys will cause the running total to be converted to an equivalent velocity, height, pressure or energy per unit mass. The cards may be used in a large number of fluid flow problems, where velocity, elevation and pressure change along the path of flow.

Operating Limits and Warnings

Downstream values should be input as negatives. However, when an output is called for, the calculator displays the relative value with no regard to upstream or downstream location.

Flashing zeros will result when the total energy sum stored in register 8 is negative and an attempt is made to calculate velocity.

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description I

Program Title

CONSERVATION OF ENERGY

Contributor's Name Hewlett-Packard

Address 1000 N.E. Circle Blvd.

City Corvallis

State Oregon

Zip Code 97330

Program Description, Equations, Variables

$$\frac{v_1^2}{2} + gz_1 + \frac{P_1}{\rho} + \frac{E_1}{\dot{m}} = \frac{v_2^2}{2} + gz_2 + \frac{P_2}{\rho} + \frac{E_2}{\dot{m}}$$

where

v is the fluid velocity;

z is the height above a reference datum;

P is the pressure;

E is an energy term which could represent inputs of work or friction losses (negative value);

g is the acceleration of gravity;

ρ is the fluid density;

\dot{m} is the mass flow rate (assumed to be unity);

subscripts 1 and 2 refer to upstream and downstream values respectively.

Operating Limits and Warnings

This program has been verified only with respect to the numerical example given in *Program Description II*. User accepts and uses this program material AT HIS OWN RISK, in reliance solely upon his own inspection of the program material and without reliance upon any representation or description concerning the program material.

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Program Description II

Sketch(es)

Sample Problem(s)

Example 1:

A water tower is 100 feet high. What is the zero flow rate pressure at the base? The density of water is 62.4 lb/ft³.

Keystrokes

See Displayed

Using card 1

62.4 **A** 100 **C** **D** → 43.33 psig

If water is flowing out of the tower at a velocity of 10 ft/sec, what is the static pressure?

10 **CHS** **B** **D** → 42.66 psig

What is the maximum frictionless flow velocity which could be achieved with the 100 foot tower?

62.4 **A** 100 **C** **B** → 80.21 ft/sec

If 10000 pounds of water are pumped to the top of the tower every hour, at a velocity of 20 ft/sec, with a frictional pressure drop of 2 psi, how much power is needed at the pump?

62.4 **A** 20 **B** 2 **D** 100 **C** **E** → 0.14 Btu/lb

10000 **X** → 1424.29
(Btu/hr)

Solution(s)

Reference(s)

Program Description II

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Sketch(es)

Sample Problem(s)

Example 2:

An incompressible fluid ($\rho = 735 \text{ kg/m}^3$) flows through the converging passage of Figure 1. At point 1 the velocity is 3 m/s and at point 2 the velocity is 15 m/s. The elevation difference between points 1 and 2 is 3.7 meters. Assuming frictionless flow, what is the static pressure difference between points 1 and 2?

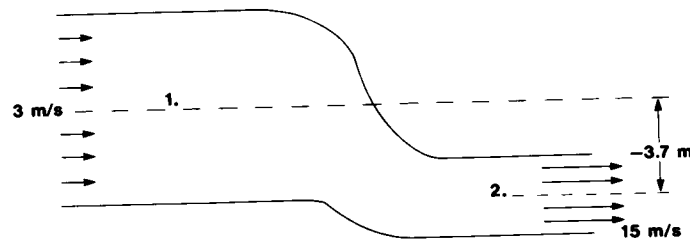


Figure 1.

Solution(s)

Keystrokes

See Displayed

Using card 2

735 **A** 3 **B** 3.7 **C** 15 **CHS** **B** **D** → -52710.82
(Nt/m²)

Reference(s)

Program Description II

Sketch(es)

Sample Problem(s)

Example 3:

A reservoir's level is 25 meters above the discharge pond. Assuming 85% power generation efficiency, how much power can be generated with a flow rate of 20 m³/s?

$$\rho = 1000 \text{ kg/m}^3$$

Keystrokes

See Displayed

Using card 2

1000	A	25	C	E	→	245.17	
							(joule/kg)
.85	X				→	208.39	
							(joule/kg)
20	↑	1000	X		→	20000	(kg/s)
X					→	4167826.25	(watts)

Solution(s)

Reference(s)

User Instructions

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CONSERVATION OF ENERGY-ENGLISH

☐ ρ (START) (lb/ft³)
 ☐ v (ft/sec)
 ☐ z (ft)
 ☐ P (psi)
 ☐ E (Btu)

CONSERVATION OF ENERGY-SI

☐ ρ (START) (kg/m³)
 ☐ v (m/s)
 ☐ z (m)
 ☐ P (N/m²)
 ☐ E (J/kg)

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	For English units (pounds, feet, seconds, Btus), enter		<input type="text"/> <input type="text"/>	
	Card 1. for SI units		<input type="text"/> <input type="text"/>	
	(kilograms, meters, seconds, watts), enter Card 2		<input type="text"/> <input type="text"/>	
2	Input fluid density	ρ	<input type="text"/> A <input type="text"/>	g
3	Input the following (negative values are downstream values):		<input type="text"/> <input type="text"/>	
	Fluid velocity	v	<input type="text"/> B <input type="text"/>	0.00
	Height from reference datum	z	<input type="text"/> C <input type="text"/>	0.00
	Pressure	P	<input type="text"/> D <input type="text"/>	0.00
	Energy input	E	<input type="text"/> E <input type="text"/>	0.00
4	Repeat step 3 for all input values		<input type="text"/> <input type="text"/>	
5	Calculate the unknown:		<input type="text"/> <input type="text"/>	
	Fluid velocity	0.00	<input type="text"/> B <input type="text"/>	v
	Height from reference datum	0.00	<input type="text"/> C <input type="text"/>	z
	Pressure	0.00	<input type="text"/> D <input type="text"/>	P
	Energy	0.00	<input type="text"/> E <input type="text"/>	E
6	For new case go to step 2, or		<input type="text"/> <input type="text"/>	
	store 0.00 in register 8 and go		<input type="text"/> <input type="text"/>	
	to step 3.		<input type="text"/> <input type="text"/>	

97 Program Listing I

STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS		
001	*LBLA	21 11	Store ρ and constants	057	GT01	22 01	Energy		
002	ST04	35 04		058	RCL8	36 08			
003	CLX	-51		059	RCL7	36 07			
004	ST08	35 08		060	=	-24			
005	7	07		061	RCL4	36 04			
006	7	07		062	X	-35			
007	8	08		063	RCL6	36 06			
008	.	-62		064	=	-24			
009	1	01		065	RTN	24			
010	6	06		066	*LBLB	21 15			
011	ST05	35 05	Velocity	067	ENT↑	-21	Summation		
012	3	03		068	RCL5	36 05			
013	2	02		069	X	-35			
014	.	-62		070	RCL6	36 06			
015	1	01		071	X	-35			
016	7	07		072	0	00			
017	ST06	35 06		073	X*Y?	16-32			
018	RTN	24		074	GT01	22 01			
019	*LBLB	21 12		075	RCL8	36 08			
020	ENT↑	-21		076	RCL5	36 05			
021	ABS	16 31	Height	077	=	-24			
022	X	-35		078	RCL6	36 06			
023	2	02		079	=	-24			
024	=	-24		080	RTN	24			
025	0	00		081	*LBL1	21 01			
026	X*Y?	16-32		082	R↓	-31			
027	GT01	22 01		083	ST+8	35-55 08			
028	RCL8	36 08		084	0	00			
029	2	02		085	RTN	24			
030	X	-35							
031	JX	54	Pressure						
032	RTN	24							
033	*LBLC	21 13							
034	ENT↑	-21		090					
035	RCL6	36 06							
036	X	-35							
037	0	00							
038	X*Y?	16-32							
039	GT01	22 01							
040	RCL8	36 08							
041	RCL6	36 06							
042	=	-24							
043	RTN	24							
044	*LBLC	21 14		100					
045	ENT↑	-21							
046	1	01							
047	4	04							
048	4	04							
049	ST07	35 07							
050	X	-35							
051	RCL4	36 04							
052	=	-24							
053	RCL6	36 06							
054	X	-35		110					
055	0	00							
056	X*Y?	16-32							
REGISTERS									
0	1	2	3	4	5	6	7	8	9
				ρ	778.16	g	144	ΣE	Used
S0	S1	S2	S3	S4	S5	S6	S7	S8	S9
A	B	C	D	E	I				

97 Program Listing II

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STEP	KEY ENTRY	KEY CODE	COMMENTS	STEP	KEY ENTRY	KEY CODE	COMMENTS
001	*LBLA	21 11	Store and gravity constant	057	R↓	-31	Summation
002	STO4	35 04		058	ST+8	35-55 08	
003	CLX	-51		059	0	00	
004	STO8	35 08		060	RTN	24	
005	9	09					
006	.	-62					
007	8	08					
008	0	00					
009	6	06					
010	6	06					
011	5	05					
012	STO6	35 06	Velocity	180			
013	RTN	24					
014	*LBLB	21 12					
015	ENT↑	-21					
016	ABS	16 31					
017	X	-35					
018	2	02					
019	=	-24					
020	0	00					
021	X=Y?	16-32		190			
022	GT01	22 01	Height				
023	RCL8	36 08					
024	2	02					
025	X	-35					
026	JX	54					
027	RTN	24					
028	*LBLC	21 13					
029	ENT↑	-21					
030	RCL6	36 06					
031	X	-35		200			
032	0	00	Pressure				
033	X=Y?	16-32					
034	GT01	22 01					
035	RCL8	36 08					
036	RCL6	36 06					
037	=	-24					
038	RTN	24					
039	*LBLD	21 14					
040	ENT↑	-21					
041	RCL4	36 04		210			
042	=	-24	Energy				
043	0	00					
044	X=Y?	16-32					
045	GT01	22 01					
046	RCL8	36 08					
047	RCL4	36 04					
048	X	-35					
049	RTN	24					
050	*LBL E	21 15					
051	ENT↑	-21					
052	0	00		220			
053	X=Y?	16-33					
054	RCL8	36 08					
055	RTN	24					
056	*LBL1	21 01					

LABELS					FLAGS	SET STATUS		
A	B	C	D	E	0	FLAGS	TRIG	DISP
ρ	V	Z	P	E		ON OFF		
a	b	c	d	e	1	0 <input type="checkbox"/> <input checked="" type="checkbox"/>	DEG <input checked="" type="checkbox"/>	FIX <input checked="" type="checkbox"/>
0	1 Σ	2	3	4	2	1 <input type="checkbox"/> <input checked="" type="checkbox"/>	GRAD <input type="checkbox"/>	SCI <input type="checkbox"/>
5	6	7	8	9	3	2 <input type="checkbox"/> <input checked="" type="checkbox"/>	RAD <input type="checkbox"/>	ENG <input type="checkbox"/>
						3 <input type="checkbox"/> <input checked="" type="checkbox"/>		n—2—

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Physics
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Aircraft Operation
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HEAT TRANSFER THROUGH COMPOSITE CYLINDERS AND
WALLS

STEADY STATE COND. HEAT TRANS., HEAT LOAD &
LOGARITHMIC MEAN

SUN ALTITUDE, AZIMUTH, SOLAR POND ABSORPTION

TOTAL DAILY AMOUNT OF SOLAR RADIATION

TEMPERATURE OR CONCENTRATION PROFILE FOR A
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TRANSIENT TEMPERATURE DISTRIBUTION IN A SEMI-
INFINITE SOLID WITH CONVECTION BOUNDARY CONDITION

CONSERVATION OF ENERGY



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