

# Programming the Personal Computer

*Wherein are revealed the functions of the keys, how problems are solved, and a bit of what goes on inside.*

by R. Kent Stockwell

THE HP-65 CALCULATOR uses the same reverse Polish keyboard language, the same four-register operational stack, and the same architecture as its predecessors, the HP-35,<sup>1</sup> the HP-45, and the HP-80.<sup>2</sup> It also has two important features that are new to hand-held calculators. One is its greatly expanded function set, and the other is programmability, complete with conditional and unconditional branching, user-definable functions, and magnetic-card program storage.

## Function Set

Thirteen HP-65 keys are for data entry. These are the digits 0 to 9, the decimal point, **CHS** (change sign), and **EEX** (enter exponent). Numbers may be entered with or without a power-of-ten exponent.

Keyed-in digits set the value of the X register, which is also the display, in the four-register operational stack.\* The **CLx** (clear x) key allows corrections. Any other key except **SST** and **R/S** terminates entry of a number.

The four arithmetic functions (+, -, ×, ÷) operate on x and y, the contents of the X and Y registers. Operands are loaded into the stack with the **ENTER↑** key; they may then be operated upon by the function keys. Operations execute immediately and results appear in X.

Thirty-three other functions derive from using three prefix keys (**f**, **f<sup>-1</sup>**, **g**) to condition eleven suffix keys (digits 0-9 and decimal point). The two gold-colored prefix keys, labeled **f** and **f<sup>-1</sup>**, access the functions printed in gold above the suffix keys and the inverses or complements of these functions. The blue prefix key, **g**, accesses the functions printed in blue on the angled lower side of the suffix keys. (The no-prefix meanings of the suffix keys appear on their top faces.) All of these functions execute immediate-

ly, operating on x, or x and y, or the entire operational stack. Thus, for example, the key sequence **f 4** obtains  $\sin x$  in the display, **f<sup>-1</sup> 4** obtains  $\sin^{-1} x$ , and **g 4** obtains  $1/x$ .

Computations requiring more data storage than is provided by the operational stack may use any of nine data storage registers. For example, pressing **STO 4** stores x into register four, leaving x unchanged. Pressing **RCL 4** recalls  $r_4$  to X, leaving  $r_4$  unchanged. Arithmetic accumulation to any storage register is accomplished by inserting the desired operation key between **STO** and the digit key that addresses the register. Thus the key sequence **STO <arithmetic operator> <digit n>** gives  $r_n <\text{arithmetic operator}> x$  in register  $R_n$  and leaves x in the display.

The user can change the display format as required by the particular problem. The key sequence **DSP <digit n>** rounds the display value to n digits after the decimal point in scientific notation,\* while **DSP . <digit n>** results in an absolute display rounded to n digits following the decimal point. For example, 12.366 gives 1.24 01 in **DSP 2** mode and 12.37 in **DSP . 2** mode. Display rounding does not affect internal values.

All functions involving angles, that is, sin, cos, tan, R→P (rectangular to polar conversion), → D.MS (conversion to degrees, minutes, seconds), and the inverses of these functions accept arguments or produce results in degrees, radians, or grads, set by the key sequence **g ENTER↑** or **g CHS** or **g EEX**, respectively. These settings remain in effect until changed.

On the theory that users should be able to correct key-sequence errors with minimal effort, any prefix key overrides any previous prefix key, and the sequence **f ENTER↑** clears any prefix keys. Thus, for example, the key sequence **STO + f g g 4** gives  $1/x$ ,

\*Capital letters are names of registers and lower-case letters are register contents.

\*One digit to the left of the decimal point with power-of-ten exponent, e.g.,  $2.54 \times 10^{12}$ .

while  $g f \text{ ENTER} \uparrow 4$  gives the value 4 in the display.

By now it must be clear how key conditioning with color-coded keys and legends has been used to provide access to many functions with a limited number of keys on a small keyboard. Although another level of conditioning would further expand the function set (e.g.,  $f g 4$  or  $f^{-1} g 4$  or  $g f 4$  could possess functional meanings), this would greatly increase keyboard complexity, keyboard busyness, and internal control programming. For these reasons, most of the key conditioning remains at the one-prefix level.

HP-65 functions are listed on page 14. Fig. 1 shows an example of a problem solution.

### Programming

All operations described so far apply when the switch in the upper right-hand corner of the HP-65 keyboard is in the RUN position. When this switch is in the W/PRGM position, the keystrokes are stored in the 100-step program memory instead of being executed. Twenty-five frequently used two-keystroke sequences merge into a single memory step; thus the program memory may actually contain more than 100 keystrokes.

#### Problem:

$$\text{Evaluate } V_B = \frac{kT}{q} \ln\left(\frac{I_D}{I_S} + 1\right) - RI_D$$

for  $V_B = 8$  volts,  $kT/q = 0.026$  volts,  $I_D = 6 \times 10^{-3}$  amperes,  $I_S = 10^{-10}$  amperes,  $R = 1200$  ohms

#### Solution:

Stack Registers					
Keystrokes	Display	X	Y	Z	T
8	8.				
$\text{ENTER} \uparrow$	$8.00 \times 10^0$	8			
.026	.026	8			
$\text{ENTER} \uparrow$	$2.60 \times 10^{-2}$	.026	8		
.006	.006	.026	8		
$\text{ENTER} \uparrow$	$6.00 \times 10^{-3}$	.006	.026	8	
$\text{EEX } 10 \text{ CHS}$	$10^{-10}$	.006	.026	8	
$\div$	$6.00 \times 10^7$	.026	8	8	
1	1	$6 \times 10^7$	.026	8	
+	$6.00 \times 10^7$	.026	8	8	
$f \ln$	$1.79 \times 10^1$	.026	8	8	
$\times$	$4.66 \times 10^{-1}$	8	8	8	
$-$	$7.53 \times 10^{-1}$	8	8	8	
1200	1200	$7.53 \times 10^{-1}$	8	8	
$\text{ENTER} \uparrow$	$1.20 \times 10^3$	1200	$7.53 \times 10^{-1}$	8	
.006	.006	1200	$7.53 \times 10^{-1}$	8	
$\times$	$7.20 \times 10^0$	$7.53 \times 10^{-1}$	8	8	
$-$	$3.34 \times 10^{-1}$	8	8	8	

Calculator in DSP 2 Mode

Fig. 1. An example of HP-65 use as a scientific calculator.

STO 1	RCL 1	g R↓
STO 2	RCL 2	g R↑
STO 3	RCL 3	g x=y
STO 4	RCL 4	g LSTx
STO 5	RCL 5	g NOP
STO 6	RCL 6	g x≠y
STO 7	RCL 7	g x≤y
STO 8	RCL 8	g x=y
		g x>y

Fig. 2. User programs may have as many as 100 steps. These twenty-five keystroke sequences merge into a single step. Thus programs may contain more than 100 keystrokes.

The memory itself contains no absolute addresses. Instead, it is a circulating shift register organized into six-bit words. One word is a marker that denotes the boundary between the beginning and the end of the memory. Another word is a pointer which denotes the last step executed in run mode, and the last step filled in program mode. As a program runs, this pointer is moved down through memory. Branching is accomplished by moving the pointer to the location of the destination label. User-defined function calls are implemented by leaving the main pointer at the call and activating a second pointer at the function location (see Fig. 3). When the return to the calling location occurs, the second pointer is deactivated and the first pointer reactivated. Neither the marker nor the pointers subtract from the 100 user steps.

Programs may contain three types of tests to allow conditional execution of all operations. These are x-y comparisons ( $x \neq y$ ,  $x \leq y$ ,  $x = y$ ,  $x > y$ ), four flag tests

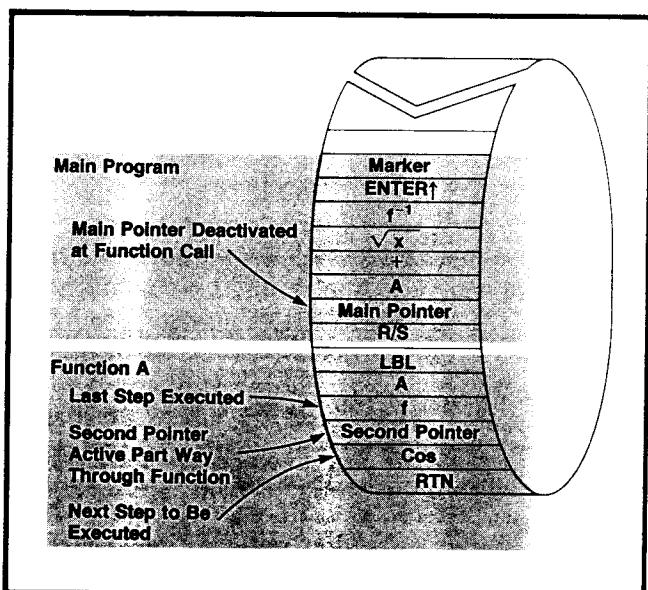
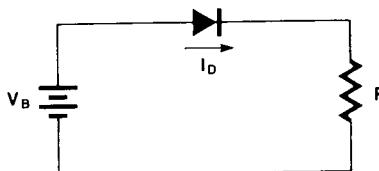


Fig. 3. The program memory circulates continuously, its beginning and end denoted by a marker. The main pointer moves as programs are entered or executed. A second pointer is activated when a user-defined function is called.

**Problem:**

Find the diode current  $I_D$  in the circuit shown. Also find its sensitivity with respect to  $V_B$  and  $R$ , i.e.,  $\partial I_D / \partial V_B$  and  $\partial I_D / \partial R$ .



**Equations:**

$$V_B = \frac{kT}{q} \ln\left(\frac{I_D}{I_S} + 1\right) + RI_D$$

$$\frac{\partial I_D}{\partial V_B} = \left[ \frac{kT}{q} \left( \frac{1}{I_D + I_S} \right) + R \right]^{-1}$$

$$\frac{\partial I_D}{\partial R} = -I_D \left[ \frac{kT}{q} \left( \frac{1}{I_D + I_S} \right) + R \right]^{-1}$$

$I_S$  = diode saturation current in amperes

$R$  = resistor value in ohms

$V_B$  = battery voltage in volts

$kT/q$  = thermal voltage in volts

**Algorithm:**

For Newton-Raphson iteration,

$$I_D(n+1) = I_D(n) - \frac{f[I_D(n)]}{f'[I_D(n)]}$$

where  $I_D(n)$  = nth guess

$f[I_D(n)]$  = function evaluated for nth guess

$f'[I_D(n)]$  = first derivative of function, evaluated for nth guess

$I_D(n+1)$  =  $(n+1)$ st guess

$$\text{Let } f[I_D] = V_B - \frac{kT}{q} \ln\left(\frac{I_D}{I_S} + 1\right) - RI_D$$

$$\text{Then } f'[I_D] = -\left[ \frac{kT}{q} \left( \frac{1}{I_D + I_S} \right) + R \right]$$

Specify convergence criterion: if  $|I_D(n+1) - I_D(n)| < C$  the algorithm halts.

Program halts after ten iterations. The user may then start ten more iterations.

**Example:**

$$I_S = 10^{-10} \text{ A}$$

Load card and follow user instructions.

$$R = 1.2 \text{ k}\Omega$$

$$V_B = 8 \text{ V}$$

$$kT/q = 0.026 \text{ V}$$

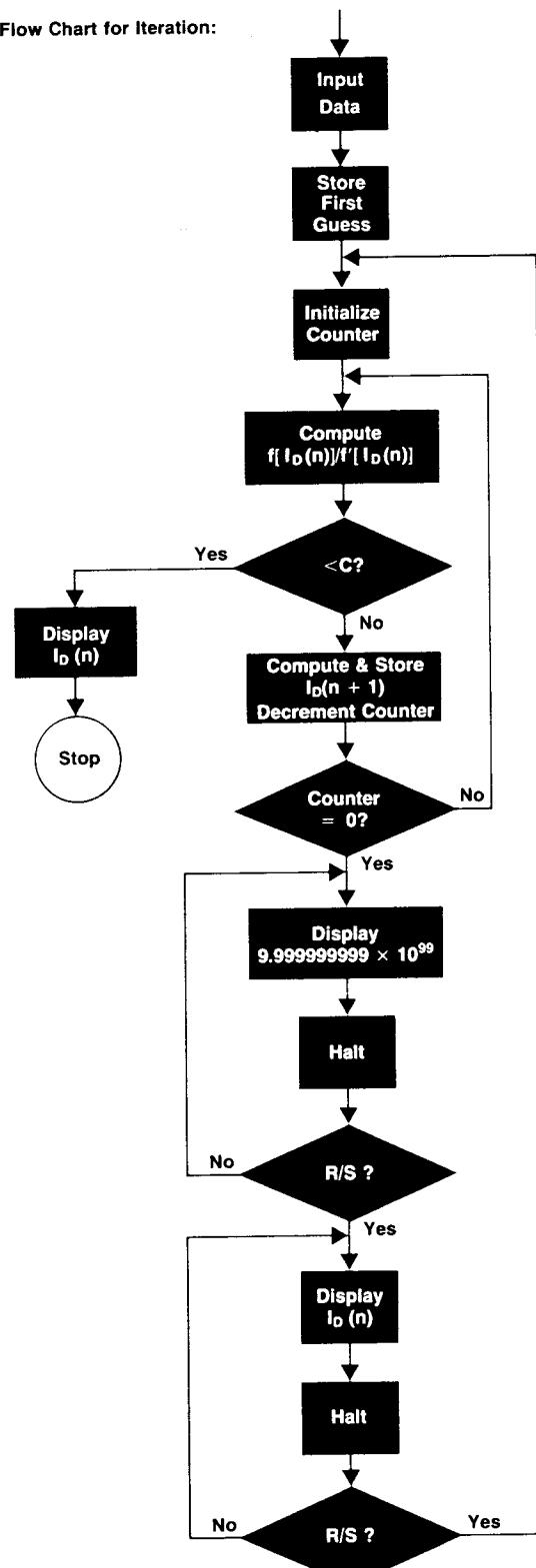
$$C = 10^{-9} \text{ A}$$

Results:

$$\begin{aligned} I_D &= 6.278 \text{ A} \\ \partial I_D / \partial V_B &= 0.8305 \text{ mA/V} \\ \partial I_D / \partial R &= -5.213 \mu\text{A}/\Omega \end{aligned}$$

Time required to compute  $I_D$  (step 3): 11 seconds.

**Flow Chart for Iteration:**



(Continued)

**Fig. 4.** An example of HP-65 programming. A common problem in many disciplines is the solution of irreducible equations, such as  $x = 5 \ln x$ . Finding the answer requires a clever first guess at the solution and, based on the results of the first guess, an even more clever second guess, and so on. The iterative procedure, tedious if done manually, can often be automated. In this example the Newton-Raphson method is used to solve an electrical engineering problem.

Program:

### HP-65 Program Form

Title: Diode Current Iteration

Page 1 of 2

KEY ENTRY	CODE	COMMENTS	REGISTERS
LBL 23	23	Compute $f(I_D)$	R1, KT1/q
D	14		R2, $I_D$ (n)
RCL 5	34 05		R3, $I_S$
RCL 2	34 01		R4, R
RCL 2	34 02		R5, VB
RCL 3	34 05		R6, C
+	81		R7, A
1	01		R8, Counter
+	61		A, B
0	31		R9, Scratch, X $\times$ Y
ln	07		LABELS
X	71		A 10
-	35		B 11
RCL 4	34 04		C 12
RCL 2	34 02		D 13
X	71		E 14
RCL 5	51	Leaves $f(I_D)$ in X	
LBL 23	23	Compute $f(I_D)$	
E	10		
RCL 1	34 01		
RCL 2	34 02		
RCL 3	34 05		
+	61		
÷	81		
RCL 4	34 04		
+	61		
CMS	42	Compute $\alpha I_D / \alpha R$	
RCL 5	24	Leaves $f(I_D)$ in X, $\alpha I_D / \alpha R$ in Y	
LBL 23	23	Compute $\alpha I_D / \alpha R$	
A	11		
EEX	43	First guess = $10^{-3}$ AMP	
CHS	42		
3	03		
STO 2	33 02		
LBL 23	23	Initialize counter	
1	71		
1	01		
0	00		
STO B	33 08		
LBL 23	23	Iterate	
2	02		
D	11		
E	15		
÷	61	$f(I_D) / f'(I_D)$ in X	
9	35		
ABS	06		
RCL 6	34 04		
9 X $\times$ Y	35 24	$ f(I_D) / f'(I_D)  < C ?$	
LBL 23	02		

Note: D+E called as functions by the iteration program. C. Thus, to define a new problem, simply redefine f(I<sub>D</sub>) and f'(I<sub>D</sub>) functions D+E and, if required, the first guess in function A.

FLAGS

1

2

### HP-65 User Instructions

Title: Diode Current Iteration  
Programmer: R.K. Stockwell

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Date 3/6/74

STEP	INSTRUCTIONS	INPUT DATA/UNITS	KEYS	OUTPUT DATA/UNITS
1	Enter Card 1			
2	Inputs (Any Order)			
	Thermal Voltage	KT, Volts	STO 1	
	Saturation Current	I <sub>S</sub> , AMPS	STO 3	
	Resistance	R, OHMS	STO 4	
	Battery Voltage	V <sub>B</sub> , Volts	STO 5	
	Convergence Criterion	C, AMPS	STO 6	
3	Compute Diode Current		A	I <sub>D</sub> , AMPS
	If display 9.999999999 $\times 10^{-9}$ ,			
	do 4 and 5,			
	Otherwise skip to 6			
4	Display Present Diode Current		R/S	I <sub>D</sub> , AMPS
5	Continue (Go to 3, iterate ten more times)		R/S	
6	Either calculate voltage sensitivity or calculate resistance sensitivity or calculate $f(I_D)$ or calculate $f'(I_D)$ or go to 2 and re-enter any or all inputs for a new problem.		B	0.1 AMPS/ 10 <sup>9</sup> Volts
			C	0.1 AMPS/ 10 <sup>9</sup> OHMS
			D	f(I <sub>D</sub> ) AMPS
			E	f'(I <sub>D</sub> ) AMPS

(there are two flags, each of which may be set or cleared and then tested for set or clear), and decrement and skip if zero (DSZ). Except for DSZ, each test, if false, causes program control to skip the next two memory steps; otherwise, execution continues normally. The DSZ operation decrements data-storage register R<sub>8</sub> by one, using integer arithmetic, and if the result is zero, program control skips the succeeding two steps.

Literal labels with the GO TO function implement branching. Thus LBL<n> is the destination for GTO <n>, where n is a digit or a key A-E in the top row.

The HP-65 user may store two types of programs in the program memory. First, he may precede a section of memory containing various functions with LBL <m>, where m is A, B, C, D, or E, and terminate the section with RTN (return). Thereafter, pressing key A, B, C, D, or E in the RUN mode causes that memory section to execute immediately. Any or all of keys A to E may be defined but the sum of memory steps for all functions cannot exceed 100. These user-defined functions behave exactly like the preprogrammed functions described earlier, yet the user may create the functions to fit his special needs.

The user's second option is to precede a block of code with a label definition and terminate it with the R/S (Run/Stop) key. In RUN mode this key stops an executing program; if no program is running, pressing the R/S key starts execution. Pressing GTO<label name>R/S then starts program execution, and the program halts at the R/S in memory. If the program starts at the beginning of memory no label is needed; in RUN mode control can be transferred to the beginning of memory by pressing RTN. Programs defined in this way may call any of the functions A through E; the desired key is simply entered into the program definition.

The SST (single step) and DEL (delete) functions implement debugging and editing. In W/PRGM mode, each depression of SST advances the memory pointer one step and displays each memory step as a two-digit key code. These codes represent digit keys by their values and all other keys by a row-column index of the key position referenced to the upper left-hand corner of the keyboard. For example, the decimal-point key is in the eighth row, third column, so its code is 83. In the RUN mode, each depression of SST advances the memory pointer one step and executes the adjacent memory step.

The key sequence g CLx in W/PRGM mode deletes the displayed memory step and moves up the next step to fill the gap. Any keys entered in W/PRGM mode are automatically inserted following the displayed memory step. Thus the replacement operation consists of a delete operation followed by the desired key.

The sequence f CLx clears the entire memory.

Programs can be stored on magnetic cards for later use. Cards can be recorded and rerecorded as many times as desired. To protect a recorded program on a card, further recording can be prevented by clipping the notched tab on the upper left corner of the card. Users may write on the card and place it in a slot above the keys **A** through **E**, thereby labeling any specially defined keys.

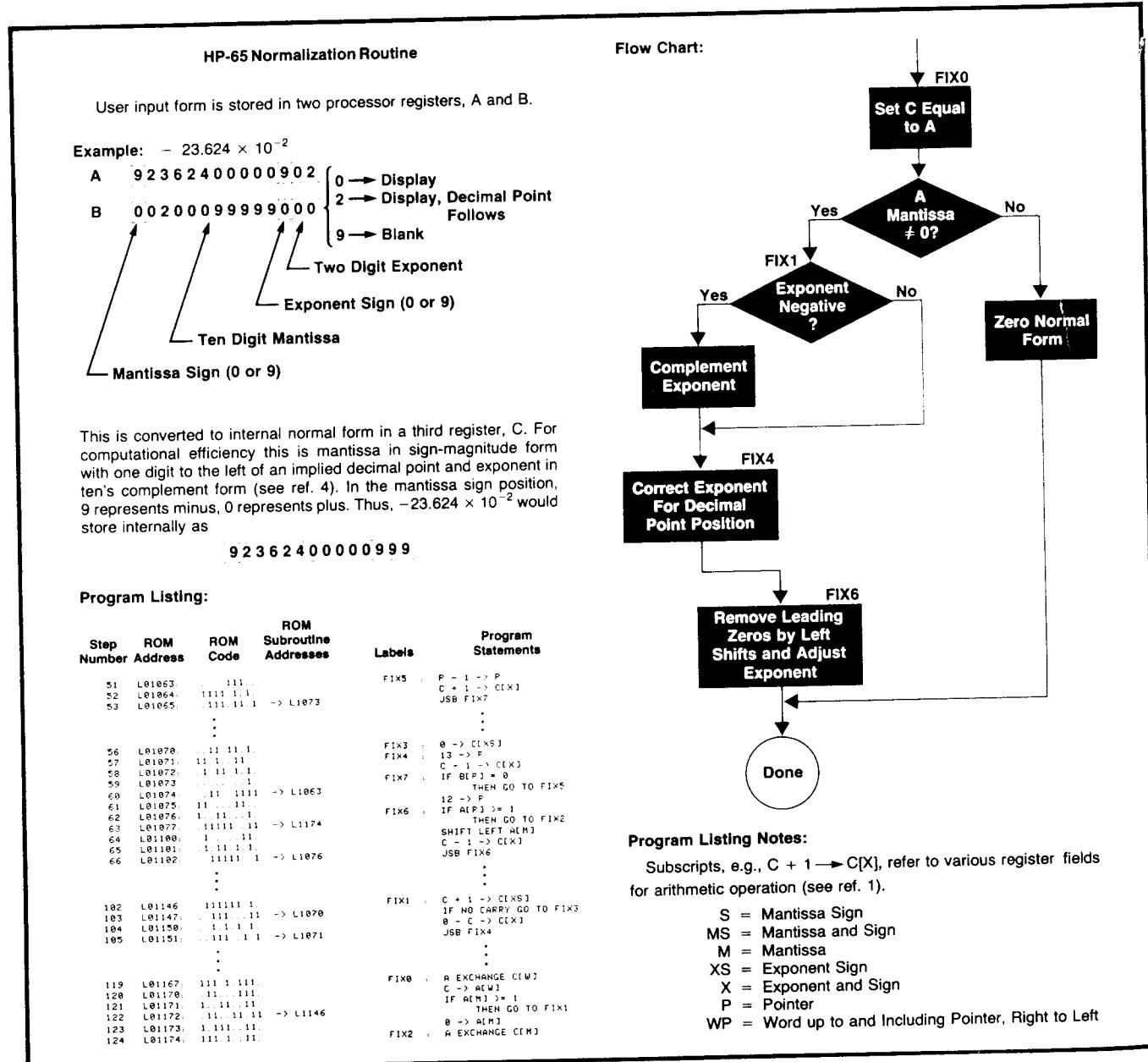
Fig. 4 shows an example of HP-65 programming.

### Firmware

To direct the various computational and control

functions of the HP-65, 3072 words of read-only memory (ROM) are used. Each ROM word contains ten bits and constitutes a calculator microinstruction. Microinstructions grouped together in blocks perform the various external functional tasks of the calculator. A task may require one block of words or several blocks woven together. For example, the CLx function requires only a few words, while the sin function uses the tan function, which uses the add function, and so on.

Although production of efficient microcode is an iterative process, the first step is the choice or design



of an algorithm. This may involve such constraints as accuracy, execution speed, microinstructions required, or even available design time. Next, a functional flow chart is drawn to outline the sequence of various operations and any conditional operations. This flow chart is then expanded to sufficient detail that it can be translated to microinstructions and implemented on a calculator simulator. More often than not there are implementation errors to correct; sometimes the entire algorithm is faulty, requiring a new design. When the design is complete, integrated-circuit read-only memories are produced.

Where possible, the HP-65 uses the proven algorithm implementations from the HP-35 and HP-45 (trigonometric, logarithmic, and exponential routines). This saved development time and reduced implementation error probabilities.

Many HP-65 algorithms would provide interesting descriptions here, but one that demonstrates appreciable complexity is the digit-entry routine. Designing this seemingly trivial function so as to seem trivial to the user required considerable patience and careful thought. Usually, any entry will produce an undesirable result unless the designer specifically accounts for it. Values must be displayed as keyed in, yet they must be normalized to some internal form. The table below lists some of the design constraints on this algorithm.

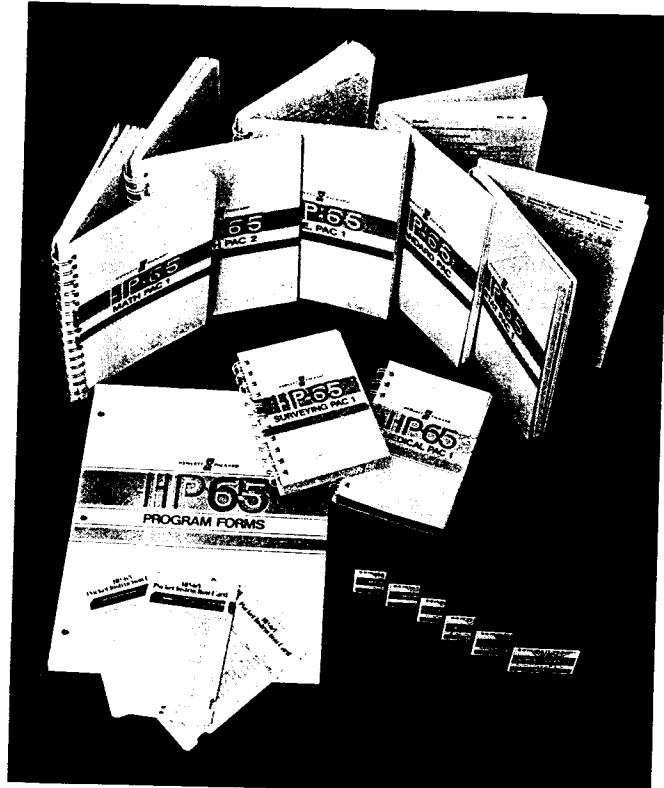
Digits before decimal point	Continue appending digits, increment internal exponent.
following	Complement exponent sign
Multiple	Complement mantissa sign, or exponent sign if has been pressed.

Such an algorithm was explained in a previous issue.<sup>3</sup> Fig. 5 shows the flow chart and ROM listing for the normalizing routine.

#### Acknowledgments

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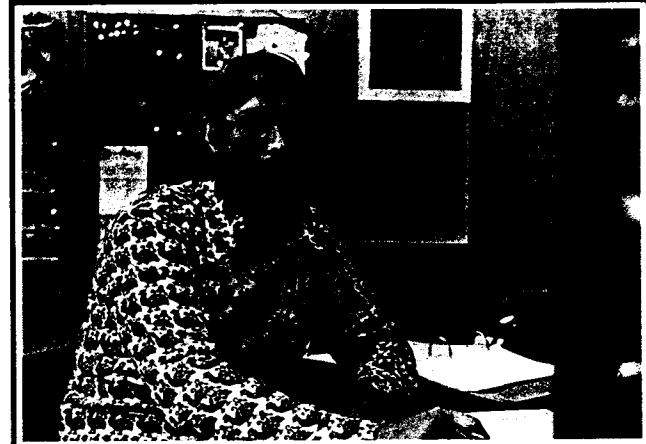
USER ACTION	DESIRED RESULT
More than ten mantissa digits	Ignore all digits after tenth
First key of new entry	Overwrite existing x if key follows <b>ENTER↑</b> or <b>CLx</b> ; otherwise do automatic <b>ENTER↑</b>
Extra digits after <b>EEX</b>	Shift exponent left; new digit becomes least significant digit of exponent.
Multiple decimal point	Ignore all decimal points after first
Decimal point after <b>EEX</b>	Ignore
Leading zeros keyed in	Accept and display leading zeros, zero normal form.
<b>EEX</b> first key of new entry	Enter one in mantissa; following digits enter exponent.
Decimal point first key of new entry	Display only decimal point; zero normal form.
Digits after decimal point	Continue appending digits; no effect on internal exponent



patiently keeping up with numerous daily changes; Steve Walther for providing the microinstruction language compiler; Darrel Lauer and Al Inholder for crystallizing the keyboard layout from a myriad of suggestions; Ed Heinsen and Lynn Tillman for extending the simulation software to accommodate the increased complexity of the HP-65. ■

#### References

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2. W.L. Crowley and F. Rodé, "A Pocket-Sized Answer Machine for Business and Finance", Hewlett-Packard Journal, May 1973.
3. D.S. Cochran, "Internal Programming of the 9100A Calculator", Hewlett-Packard Journal, September 1968.
4. M.M. Mano, "Computer Logic Design", Prentice-Hall, 1972, chapter 1.



#### R. Kent Stockwell

Kent Stockwell joined HP four years ago. As a member of HP Laboratories for most of that period, he's done program development, modeling, and numerical analysis for computer-aided circuit design and, more recently, the firmware development for the HP-65. Kent studied electrical engineering at Massachusetts Institute of Technology, graduating in 1970 with SB and SM degrees. A native of Kalamazoo, Michigan, he now lives in Palo Alto, California, where he's currently remodeling his house and putting his woodworking skills to good use. He also plays trombone and baritone horn, and enjoys backpacking in the mountains of California and Colorado.

## APPENDIX

### HP-65 Programmable Pocket Calculator

#### Functions and Operations

##### Arithmetic

add  
subtract  
multiply  
divide

##### Logarithmic

natural logarithm (base e)  
natural antilogarithm (base e)  
common logarithm (base 10)  
common antilogarithm (base 10)

##### Trigonometric

set operating mode (degrees, radians, or grads)  
sine  
arc sine  
cosine  
arc cosine  
tangent  
arc tangent  
add or subtract degrees/minutes/seconds  
convert angle from degrees, radians, or grads to degrees/minutes/seconds and vice versa  
convert polar coordinates to rectangular coordinates and vice versa

##### Exponential

square  
square root  
raising a number to a power ( $y^x$ )  
reciprocal (can be used with  $y^x$  function to extract nth roots)

##### Other Preprogrammed Functions and Operations

extract integer or decimal portion of a number  
factorial  
recall value of  $\pi$  to 10 significant digits  
convert decimal-base integers to or from octal-base integers  
"roll down" or "roll up" numbers in operational stack  
clear display  
clear operational stack  
clear all nine addressable memory registers  
recall last input argument from separate "last-x" storage register  
store or recall numbers from any of the nine addressable memory registers  
register arithmetic  
display formatting

##### Program Structure and Edit Functions

clear program memory  
user-definable keys (A-E)  
label  
go-to  
return  
run/stop  
no-operation  
set flag 1  
test flag 1  
set flag 2  
test flag 2  
 $x = y$   
 $x \neq y$   
 $x \leq y$   
 $x > y$   
decrement and skip on zero  
delete program step  
single-step

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