



HEWLETT®
PACKARD

HP 39G/40G

Quick Start Guide

**Algebraic
Graphing
Calculator**



NOTICE

This manual and any examples contained herein are provided as-is and are subject to change without notice. Except to the extent prohibited by law, Hewlett-Packard Company makes no express or implied warranty of any kind with regard to this manual and specifically disclaims the implied warranties and conditions of merchantability and fitness for a particular purpose and Hewlett-Packard Company shall not be liable for any errors or for incidental or consequential damage in connection with the furnishing, performance or use of this manual and the examples herein.

© Hewlett-Packard Company 2000. All rights reserved.

The programs that control your HP 39G/40G are copyrighted and all rights are reserved. Reproduction, adaptation or translation of those programs without prior written permission of HP is also prohibited.

HP39G/40G

QUICK START GUIDE

Version 1.0





Contents

Introduction	5
Conventions	5
1 Basic Information.....	7
Hard cover.....	7
[ON] key	7
Contrast control.....	7
Batteries	7
Ports	7
Shift key.....	8
Alpha key and special characters.....	8
2 HOME	9
Tour of HOME.....	9
Entering.....	10
Deleting and clearing	10
Retrieving and editing.....	10
Showing an expression	11
Storing numbers in variables	12
3 Modes.....	13
Angle measure	13
Number format.....	14
Decimal mark.....	15
Resetting the MODES	15
4 Computational Examples	16
Arithmetic operations	16
Transcendental functions	17
Mathematical constants.....	18
Implied multiplication.....	18
5 Aplets.....	20
Built-in Aplets.....	20
Aplet Library's menu keys	20
Starting an Aplet	21
Aplet views	21
Saving an Aplet.....	21
Deleting Aplets	22

6 Working with Graphs	23
Open the applet	23
Define the function	23
Set up the plot	23
Reset all plot settings	24
Plot the function.....	25
Analyze the graph	25
Function tools.....	27
Plotting piece-wise functions	29
Plotting multiple functions.....	30
7 Working with Tables	32
Open the applet	32
Define the function	32
Set up the table.....	32
Display the table	33
8 Special Views	35
Split screen—two graphs	35
Split screen—graph and table	35
Overlaying one graph on another.....	36
Automatic scaling	36
Special preset zoom windows.....	36
9 Functions	37
Function applet's symbolic view keys	38
Deleting and clearing functions	39
10 Parametric Equations	40
11 Polar Equations.....	42
12 Sequences	44
Iterative sequences	45
Cobweb plots	46
13 Solving Equations.....	47
Analyzing an expression in one variable	47
Analyzing an equation with several variables	48
14 Statistics	50
Example: one-variable statistics	50
Example: two-variable statistics	52

Introduction

The HP 39G/40G is an algebraic-entry graphing calculator with advanced features for:

- easy retrieval of previous answers and entries
- displaying algebraic expressions in standard textbook format
- generating tables
- displaying two graphs or a graph and a table on a split-screen
- working with functions, parametric and polar equations
- working with sequences (including recursion)
- solving equations
- computing statistics
- testing hypotheses
- calculating confidence intervals based on sample data
- symbolic algebra and tools for calculus
- operating with vectors, matrices, lists, and complex numbers
- drawing and annotating diagrams
- saving and sharing settings and equations
- programming.

This guide is intended to give you an overview of the basic features of the HP 39G/40G.

Conventions

The following conventions are used in this guide to represent the keys that you press and the menu options that you choose to perform the described operations.


- Keys are represented as follows:
`SIN`, `COS`, `HOME`, etc.
- Shift keys, that is the key combinations that require you to press the `SHIFT` key first, are represented as follows:
`SHIFT` `CLEAR`, `SHIFT` `MODES`, `SHIFT` `ACOS`, etc.
- Numbers and letters are represented normally, as follows:
5, 7, A, B, etc.
- Menu options, that is, the options you select by pressing the menu keys at the top of the keypad, are represented as follows:
`STOP`, `CANCEL`, `OK`.
- Input form fields and choose list items are represented as follows:
Function, Polar, Parametric.

- Your entries as they appear on the command line or within input forms are represented as follows:

$$2 * X^2 - 3 X + 5$$

- The arrow keys are represented as follows:

   and .


-  A pointing hand appears to bring your attention to warnings, suggestions, helpful hints, shortcuts, or other important notes.

1. Basic Information


Hard cover

The cover of the HP 39G/40G slides off the front of the calculator and can be slid onto the back.




key

The  key (lower left corner of the keyboard):

- turns on the calculator
- cancels operations

If you leave your calculator on for a few minutes without pressing any keys, it will automatically turn off to save battery power. When you press  again, the screen reappears just as you left it. The memory of the calculator is maintained when the calculator is off.

Contrast control

To lighten or darken the screen to your preference, press and hold down  while pressing  or , respectively.

Batteries

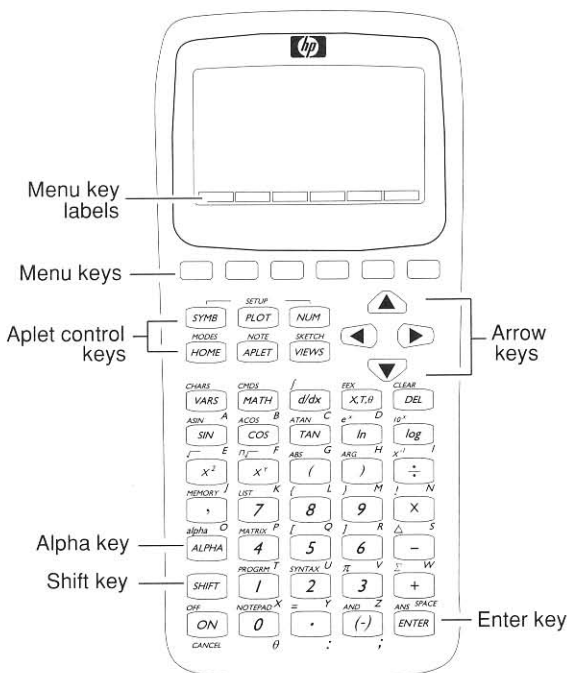
The HP 39G/40G takes three AAA batteries, which are located in the lower compartment in the back of the calculator. You should get several months' use out of a set of batteries. Even when you take the batteries out, the calculator's memory is maintained for a few minutes, giving you the opportunity to change the batteries without loss of stored information.

Ports


You will find 2 ports on the top edge of the HP 39G/40G:

- a 10-pin serial port for connecting to another calculator or a datalogger
- an infrared port for connecting to another calculator or printer.

The infrared port can be used only on the HP 39G.



Shift key

Directly above the **ON** key is the **SHIFT** key. Press **SHIFT** and another key to activate the operation or menu indicated by the blue label directly above that key. When the **SHIFT** key has been pressed, a shift symbol  is displayed at the top left of the screen.

Alpha key and special characters

The **ALPHA** key enables you to enter the characters that are displayed below the other keys. When the **ALPHA** key has been pressed, α appears at the top of the screen.

 When typing several letters in a row, simply hold **ALPHA** down as you type.

Lower case letters are obtained by pressing **ALPHA** and **SHIFT** (in either order).

Greek letters and other special symbols are found in the SPECIAL CHARACTERS menu (**SHIFT** **CHARS**).

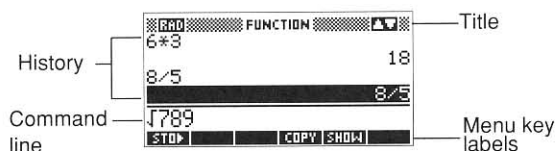
2. HOME

HOME is the primary work area for the HP 39G/40G.

Tour of HOME

To go to HOME, press **[HOME]**.

Parts of the display



Menu key or soft key labels. The labels indicating the current use of the menu keys. **STO** is the label for the first menu key. “Press **STO**” means to press the first menu key above the illustration.

Command line. The line of current entry.

History. In HOME you can see up to four lines of history: the most recent input and output. Older inputs and outputs are retained in memory, and can be displayed by pressing **[▲]** a number of times.

Title. The name of the current applet is displayed in the title bar.

RAD, GRD, DEG indicate whether Radians, Grads, or Degrees angle mode is set for HOME.

The **[H]** and **[I]** symbols indicate whether there is more history in the HOME display.

Annunciators. Annunciators are symbols that appear above the title bar and give you important status information.

Whenever an hourglass appears in the annunciator area, the HP 39G/40G is busy performing a calculation. Press **[ON]** while this annunciator is on to stop the computation.

The low battery annunciator ((•)) indicates that your batteries are getting low. (The calculator displays **Low Battery** when you first turn it on). You should change them within a few days.

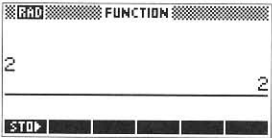
Entering

When you type, the characters appear on the command line until you press **ENTER**.

Examples:

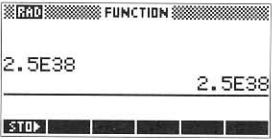
To enter 2 into the command line:

2 **ENTER**



To enter 2.5×10^{38} :

2 **□** 5 **SHIFT** *EEX* 38 **ENTER**



Deleting and clearing

To delete a character you have entered, press **▶** or **◀** until the cursor is over the character you want to delete, and press **DEL**. If the cursor is at the end of command line and you want to delete the last character, just press **DEL**.

Press **CANCEL** (**ON**) while on the command line and the entire line is deleted.

SHIFT *CLEAR* (**SHIFT** **DEL**) clears all previous inputs and outputs in HOME.

The cursor is always in insert mode in HOME. In other words, it always points to where the next character you type will be inserted.

Retrieving and editing

SHIFT *ANS* inserts the special variable *Ans* in the command line. The value of this variable is the last answer you obtained to an operation in HOME. This allows you to immediately use the result of the previous computation in a new computation without having to type it in.

In fact, until you press **SHIFT** *CLEAR*, a history of *all* your previous entries and answers is maintained on HOME. Simply press the **▲** key until you have highlighted the entry or answer you want, then press **COPY**. This copies the highlighted entry or answer into the command line.

To make changes, press the **◀** or **▶** key to position the cursor. Any characters you type are to the left of the cursor. Pressing **DEL** deletes the character underneath the flashing cursor. After you have made the changes you want, press **ENTER**.

Examples:

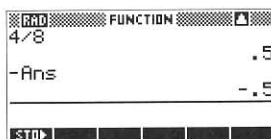
Press **[SHIFT]****CLEAR** and enter the following calculations:

3 **[X]** 2 **[ENTER]**

[(-)] **[SHIFT]****ANS** (to reverse the sign of the last answer) **[ENTER]**

4 **[÷]** 8 **[ENTER]**

[(-)] **[SHIFT]****ANS** (to reverse the sign of the last answer) **[ENTER]**



The first two computations you entered are now out of view, but they are still in HOME. Notice the **[H]** showing in the upper right of your screen. This indicates that there are more entries and answers than currently displayed. To display earlier entries, press **[▲]** to activate the highlight bar. Now you can move up and down HOME pressing the **[▲]** or **[▼]** keys. (A small **[▲]** and **[▼]** appear on screen to tell you which directions it is possible to move.) Your calculator will flash an exclamation mark—**[!]**—when you reach the top or bottom of HOME.

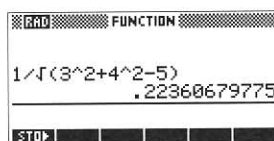
Showing an expression

If a previous entry or answer is highlighted, the **[SHOW]** menu key label is displayed. Press **[SHOW]** to display the entry or answer in standard textbook format. You can use it to check to see if you have entered an expression with the meaning that you intended.

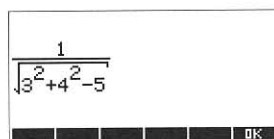
Example:

Suppose we want to evaluate the expression $1/\sqrt{3^2+4^2-5}$.

1 **[÷]** **[SHIFT]****√** (3 **[x^y]** 2 **[+]** 4 **[x^y]** 2 **[-]** 5 **)**
[ENTER]



Press **[▲]** twice to highlight the expression and press **[SHOW]** to display the expression in standard typeset version, simply press **[OK]**.



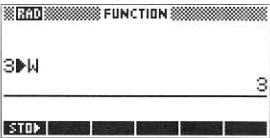
Storing numbers in variables

The letters A, B, C, . . . , X, Y, Z, and θ are reserved as variable names for real numbers. To store a number (or other object) under a variable name, enter the number or expression on the command line in HOME, press **STOP**, type the name of the variable, and press **ENTER**.

Examples:

This example stores 3 to the variable W. If a symbolic expression contains W, then the HP 39G/40G will substitute the stored value.

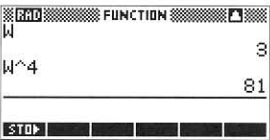
3 **STOP** **ALPHA** W **ENTER**



To recall the value, simply type the variable name and enter it.

ALPHA W **ENTER**

ALPHA W **x^y** 4 **ENTER**



3. Modes

Press **[SHIFT]MODES** to see the settings that control how the HP 39G/40G displays the HOME screen to you.

Although the number format setting affects only HOME, the angle measure setting controls HOME and the current aplet.



Angle measure

There are three angle measure modes to choose from:

- | | |
|---------|--|
| Degrees | There are 360 degrees in a full circle. |
| Radians | There are 2π radians in a full circle. |
| Grads | There are 400 grads in a full circle. |

Setting the angle measure

The following example demonstrates how to change the angle measure from the default mode, radians, to degrees for the current aplet. The procedure is the same for changing the decimal mark.

1. Press **[SHIFT]MODES** to open the HOME MODES input form.

The cursor (highlight) is in the first field, Angle Measure.



2. Press **[CHOOSE]** to display a list of choices.



3. Press **[▲]** to select Degrees, and press **[OK]**. The angle measure changes to degrees.
4. Press **[HOME]** to return to HOME.



- ☞ Instead of pressing **[CHOOSE]** and selecting an option from a menu, you can press **[+]** repeatedly until the option you want is displayed in the field.

Number format

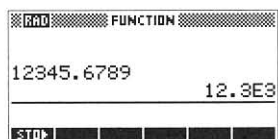
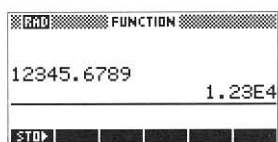
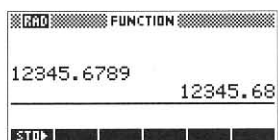
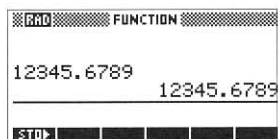
The standard numeric display mode of the HP 39G/40G is to display 12 significant digits (15 digits are used internally during computation). Your HP 39G/40G is in standard display mode if the number format reads Standard.

There are five number formats:

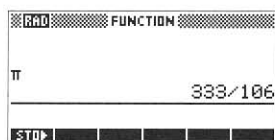
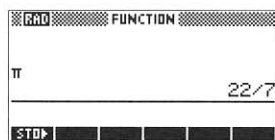
Standard	Up to 12 digits shown with a floating decimal point.
Fixed	Fixed number of decimal places, from 0 to 11.
Scientific	Exponential notation (exactly one digit to the left of the decimal point). Number of places after first significant digit can be 0 to 11.
Engineering	Exponential notation where the exponent is a multiple of 3. Number of places after first significant digit is can be 0 to 11.
Fraction	Numbers are displayed as fractions in "P/Q" format. The decimal precision of the result can be 0 to 11 places.

Examples:

- With Standard number format selected, go HOME and enter 12345.6789
- Press **[SHIFT]MODES**, **[↓]**, **[CHOOSE]** Fixed number format, specify 2 decimal places, and press **[OK]**. Press **[HOME]** and enter 12345.6789 again. The result is now displayed with 2 decimal places.
- Press **[SHIFT]MODES**, **[↓]**, **[CHOOSE]** Scientific number format (still 2 decimal places), **[OK]**. Press **[HOME]** and enter 12345.6789 again. The result is displayed with an exponent, one digit to the left of the decimal point, and the specified number of decimal places.
- Press **[SHIFT]MODES**, **[↓]**, **[CHOOSE]** Engineering number format (still 2 decimal places), **[OK]**. Press **[HOME]** and enter 12345.6789 again. The result is displayed with an exponent that is a multiple of 3, and the specified number of significant digits beyond the first one.



- e. Press SHIFT MODES , V , CHOOSE Fraction number format (with 2 digits maximum), OK . Press HOME and enter π . The result is displayed as a fraction based on 2 decimal places.
- f. Press SHIFT MODES , V , CHOOSE Fraction number format (with 3 digits maximum), OK . Press HOME and enter π . The result is displayed as a fraction based on 3 decimal places.



-  You will probably find that Standard format serves most general purposes best.

Decimal mark

You can also change the decimal mark from a period (.) to a comma (,).

Resetting the MODES

Press SHIFT CLEAR to reset all the modes to default settings.

4. Computational Examples

The HP 39G/40G uses algebraic-entry notation (*not* Reverse Polish Notation or RPN). The following examples demonstrate the use of the basic arithmetic and function operations of the HP 39G/40G. Keystrokes are shown along with the resulting calculator display. All answers shown are for Standard number format.

Arithmetic operations

Addition: 26 $+$ 82 ENTER

RAD FUNCTION	
26+82	108
86-32	54
STO>	

Subtraction: 86 $-$ 32 ENTER

Negation: $(-)$ 2 ENTER

RAD FUNCTION	
-2	-2
62*45	2790
STO>	

Multiplication: 62 \times 45 ENTER

Division: 85 \div 20 ENTER

RAD FUNCTION	
85/20	4.25
42^5	130691232
STO>	

Exponentiation: 42 x^y 5 ENTER

Square roots: SHIFT $\sqrt{}$ 20 ENTER

RAD FUNCTION	
$\sqrt{20}$	4.472135955
25^2	625
STO>	

Squares (exponent 2 is shown as a superscript):

25 x^2 ENTER

Reciprocals: 85 SHIFT x^{-1} ENTER

RAD FUNCTION	
85^{-1}	1.17647058824E-2
10^3	1000
STO>	

Powers of 10: SHIFT 10^x 3 ENTER

Absolute value: SHIFT ABS $(-)$ 5 ENTER

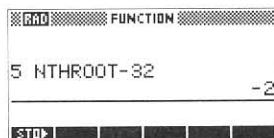
RAD FUNCTION	
$ABS(-5)$	5
$\sqrt{-4}$	(0,2)
STO>	

The square root of a negative number:

SHIFT $\sqrt{}$ $(-)$ 4 ENTER

*N*th roots: $\sqrt[n]{-32}$.

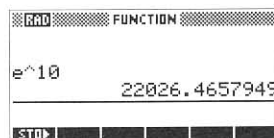
5 $\boxed{\text{SHIFT}}$ $\boxed{\sqrt[n]{}}$ $\boxed{(-)}$ $\boxed{32}$ $\boxed{)}$ $\boxed{\text{ENTER}}$



Either the subtraction key $\boxed{-}$ or the negation key $\boxed{(-)}$ can be used to obtain a negative sign in an expression.

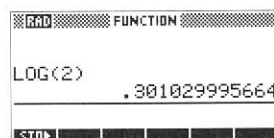
Transcendental functions

Natural exponentials: $\boxed{\text{SHIFT}}$ $\boxed{e^x}$ $\boxed{10}$ $\boxed{\text{ENTER}}$

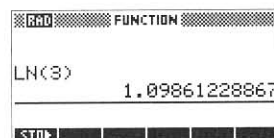


The function keys automatically insert the left parenthesis for you. Unless it is necessary to ensure the intended meaning, you do not need to insert the right parenthesis

Common (base 10) logarithms: $\boxed{\text{LOG}}$ $\boxed{2}$ $\boxed{)}$ $\boxed{\text{ENTER}}$

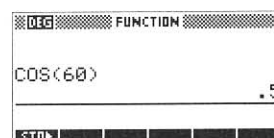


Natural (base *e*) logarithms: $\boxed{\ln}$ $\boxed{3}$ $\boxed{\text{ENTER}}$



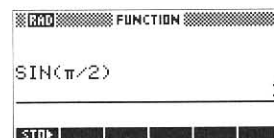
With the angle measure set to Degrees :

Trigonometric functions: $\boxed{\text{COS}}$ $\boxed{60}$ $\boxed{)}$ $\boxed{\text{ENTER}}$



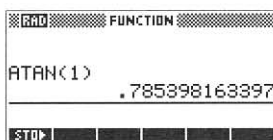
With the angle measure set to Radians :

Trigonometric functions: $\boxed{\text{SIN}}$ $\boxed{\text{SHIFT}}$ $\boxed{\pi}$ $\boxed{+}$ $\boxed{2}$ $\boxed{)}$ $\boxed{\text{ENTER}}$



Inverse trigonometric functions: $\boxed{\text{SHIFT}} \boxed{\text{ATAN}} \boxed{1} \boxed{)}$

$\boxed{\text{ENTER}}$

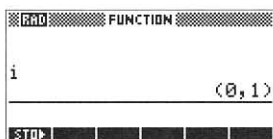
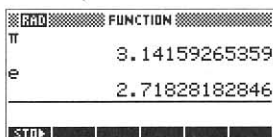


Mathematical constants

π ($\boxed{\text{SHIFT}} \boxed{\pi} \boxed{\text{ENTER}}$)

e ($\boxed{\text{ALPHA}} \boxed{\text{SHIFT}} \boxed{e}$)

i ($\boxed{\text{ALPHA}} \boxed{\text{SHIFT}} \boxed{i}$)



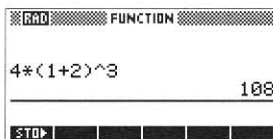
Some for you to try:

- g. A famous result. What is $e^{\pi i} + 1$?
- h. Which is larger: e^{π} or π^e ?
- i. What is $\ln(-1)$?

Implied multiplication

The juxtaposition of two number quantities implies multiplication in most cases. Here are some examples to illustrate:

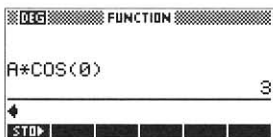
$4 \boxed{(} \boxed{1} \boxed{+} \boxed{2} \boxed{)} \boxed{x^y} \boxed{3} \boxed{\text{ENTER}}$



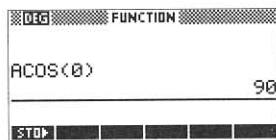
Note that a multiplication symbol is automatically entered for you.

With 3 stored in variable A and the angle measure in *MODES* set to Degrees:

$\boxed{\text{ALPHA}} \boxed{A} \boxed{\text{COS}} \boxed{0} \boxed{)} \boxed{\text{ENTER}}$ shows $A * \cos(0)$



Note the space that appears on the command line when you press `COS` immediately after typing A. This space appears because there is a chance of ambiguity in the function name. If we were to delete the space between A and `COS (0)` before pressing `ENTER`, we obtain `ACOS (θ)` not `A * COS (θ)`.



5. Aplets

Aplets are the application environments where you explore different classes of mathematical operations.

Aplets are stored in the Aplet library. Press **APLET** to display the **APLET LIBRARY**.



Built-in Aplets

Function	for working with functions, that is, equations of the form $y = f(x)$
Inference	for working with inferential statistics
Parametric	for working with parametric equations: $x(t), y(t)$
Polar	for working with polar equations: $r = f(\theta)$
Sequence	for working with sequences: $\{U_N\}$ ($N = 1, 2, \dots$)
Solve	for equations of one or more variables
Statistics	for working with descriptive statistics
Quad Explorer	a special e-lesson for investigating the characteristics of quadratic functions
Trig Explorer	a special e-lesson for investigating the characteristics of trigonometric functions

Aplet Library's menu keys

- Press **SAVE** to save an existing aplet with a new name.
- Press **RESET** to revert the aplet's default settings.
- Press **SORT** to sort the Aplet Library menu options alphabetically or chronologically.
- Press **SEND** to transmit aplet(s) to another HP 39G/40G or PC.
- Press **RECV** to receive aplet(s) from another HP 39G/40G or PC.
- Press **START** to activate an aplet.

Starting an Aplet

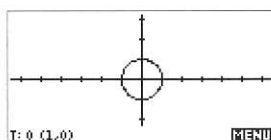
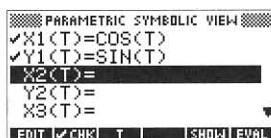
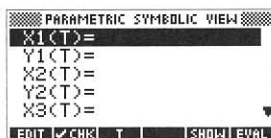
The following example illustrates how to start a Parametric aplet. The procedure is the identical for all aplets.

1. Press **APLET**.
2. Press **▼** twice to select Parametric.
3. Press **START**.

The Function, Parametric, Polar, Sequence, Inference, and Solve aplets start in the Symbolic view. The Symbolic view is used to define functions, equations, and expressions for these aplets. The Statistics aplet starts in the Numeric view and the Trig and Quad Explorer aplets start in the Plot view.

Aplet views

- In Symbolic view (**SYMB**), you specify equations, or data to work on.
- In the Plot view (**PLOT**), you draw, manipulate, and analyze graphs.
- In the Numeric view (**NUM**), you display the coordinates of the plotted points, or enter the data for statistical analysis.



T	X1	Y1
0	1	0
.1	.9950042	.0998334
.2	.9800666	.1986693
.3	.9553365	.2955202
.4	.921061	.3844183
.5	.8775826	.4744255

NUM

ZOOM **BIG** **DEFN**

Saving an Aplet

SAVE enables you to save the equations or data you have been using along with the particular settings you specified. You can even save notes (**SHIFT** **NOTE**) and sketches (**SHIFT** **SKETCH**) with the aplet.

When you press **SAVE** you are prompted for a name for the aplet. Enter a name of your choice, press **OK** or if you change your mind, press **CANCEL**.



The **ALPHA** menu key enables you to enter a string of alphabetic characters without holding down the **ALPHA** key. Press **ALPHA** to turn this feature off after you have entered a name for the aplet.

For example, if you type in **MINE** as the name of your aplet and press **ALPHA**, you will see **MINE** listed in the Aplet Library along with the built-in aplets.

At any time in the future, you can reuse the equations, data, and settings by pressing **APLET**, highlighting **MINE** and pressing **SHIFT**. If you change the equations, data, or settings, you can either **RESET** **MINE** to its original version or **SAVE** it again with the changes you have made.



APLET LIBRARY		291K
MINE	1.1KB	
Parametric	.65KB	
Function	0KB	
Inference	0KB	
Polar	0KB	
SAVE RESET SORT SEND RECV START		

Deleting Aplets

To delete a saved aplet, highlight its name in the Aplet Library and press **DEL**. If you want to delete all the saved aplets (except the built-in ones) press **SHIFT CLEAR**. The HP 39G/40G will not allow you to delete any of the built-in aplets.

When deleting aplets, you will be prompted to confirm that you want to proceed with the deletion. Press **YES** or **NO**.

6. Working with Graphs

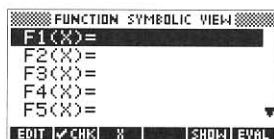
These examples illustrate some of the tools available in the Plot view (**PLOT**). All the examples are for Function, but many of the features are similar for Parametric, Polar, Sequence, Solve, and Statistics.

Open the applet

1. Open the Function applet.

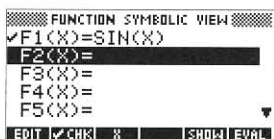
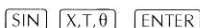



The Function Symbolic View is the starting view for the Function applet.



Define the function

2. Enter the function you want to explore.



 You can enter up to 10 functions, and plot one, some, or all of them. Those functions with a checkmark beside them will be plotted. You press **CHK** to add a checkmark, or to remove a checkmark, from a highlighted equation.

Set up the plot

3. Set up the plot.



There are two pages of plot settings, and you move between the two pages by pressing the **PAGE** and **PAGE** keys. The settings on these pages determine the dimensions and the features of the Plot view or viewing window.



Plot setup fields

The first page of the Function Plot Setup displays the following settings:

XRNG:	XMIN and XMAX
	the left and right boundaries of your viewing window
YRNG:	YMIN and YMAX
	the lower and upper boundaries of your viewing window
XTICK:	the spacing of the marks on the x -axis
YTICK:	the spacing of the marks on the y -axis
RES:	plot resolution
	(Detail for every pixel; Faster for every second pixels)

4. Change the XTICK setting to 2.



FUNCTION PLOT SETUP	
XRNG: -6.5	6.5
YRNG: -8.1	8.2
XTICK: 2	YTICK: 1
RES: Detail	
ENTER VERTICAL TICK SPACING	
EDIT	PAGE ▼

5. Move to the second page of FUNCTION PLOT SETUP.



Press **CHK** to check or uncheck any of the following plot mode settings:

SIMULT checked for simultaneous graphing of all selected equations; unchecked for sequential (F1(X) before F2(X), and so on).

CONNECT checked for connected graphing; uncheck for dot mode

AXES checked to show the axes; unchecked to hide the axes

INV. CROSS checked for inverted cursor crosshairs (shown as white on a dark background); uncheck for standard cursor crosshairs

LABELS checked to have axes labeled with their ranges; uncheck to hide labels

GRID checked to have lattice points plotted (points that line up with the tick marks on both axes); uncheck to hide lattice points

FUNCTION PLOT SETUP	
<input checked="" type="checkbox"/> SIMULT	<input type="checkbox"/> INV. CROSS
<input checked="" type="checkbox"/> CONNECT	<input type="checkbox"/> LABELS
<input checked="" type="checkbox"/> AXES	<input type="checkbox"/> GRID
PLOT FUNCTIONS SIMULTANEOUSLY?	
<input checked="" type="checkbox"/> CHK	<input type="checkbox"/> PAGE

Reset all plot settings

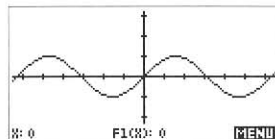
6. Reset all the plot settings so that the origin is at the center of the screen, coordinate axes are shown, each axis tick represents one unit, and each pixel represents 0.1 units.

SHIFT **CLEAR**.

To reset a field to the default value, highlight the field and press **DEL**.

Plot the function

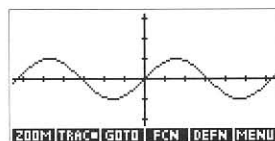
7. Press **PLOT** to see the graph of the function(s).



Analyze the graph

8. Press **MENU** and the coordinates disappear to display the Plot view menu keys.

The Plot view menu keys enable you to explore the graph in greater detail.



Plot view menu keys

- Press **ZOOM** to display the zoom menu. See “Zooming options” on page 26 for descriptions and examples of zoom options.
- **TRACE** indicates that the trace function is turned on (this is the default setting). Press **▶** or **◀** to trace along a graph. Press **▲** or **▼** to move from one function to another function. Press **TRACE** to turn the trace function off. When the trace function is off—indicated when the menu key label reads **TRACE**—the cursor can move freely across the entire viewing window.
- Press **GOTO** to specify an X value to jump to on the graph. The coordinates of the point at your chosen X value are displayed near the bottom of the screen.
- Press **FCN** to display the list of function tools. See “Function tools” on page 27 for more information. Note: The **FCN** menu key is only available in the Function aplet.
- Press **DEFN** to display the equation for the currently selected function. In the example above, the equation is $F1(X) : \sin(X)$.
- Press **MENU** to hide the menu labels. Press **MENU** again to obtain the coordinates. Press **MENU** once more to show the menu labels again.

When all of the menu labels are hidden, pressing any of the menu keys restores the trace coordinates.

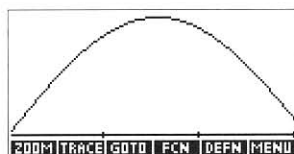
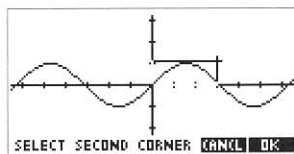
Zooming options

The **Zoom** menu key displays the following zoom methods:

Center	centers the screen at the location of the cursor.
Box...	allows you to draw a box that will become your new viewing window.
In	will <i>zoom in</i> by the horizontal and vertical zoom factors.
Out	will <i>zoom out</i> by the horizontal and vertical zoom factors.
X-Zoom In	will <i>horizontally zoom in</i> by the zoom factor.
X-Zoom Out	will <i>horizontally zoom out</i> by the zoom factor.
Y-Zoom In	will <i>vertically zoom in</i> by the zoom factor.
Y-Zoom Out	will <i>vertically zoom out</i> by the zoom factor.
Square	will <i>square up</i> the viewing window so that 1 pixel represents the same distance horizontally and vertically.
Set Factors...	allows you to set your own horizontal and vertical zoom factors (default is 4 for both factors).
Auto Scale	adjusts the scale of the <i>y</i> -axis so that as much of the graph as possible is displayed while also showing the origin, maximum, and minimum.
Decimal	returns a zoomed graph to its default plotting domain.
Integer	changes the tickmark spacing on both axes to 1 unit.
Trig	changes the tickmark spacing for the independent variable to $\pi/24$ radians, 7.5 degrees or $81\frac{1}{3}$ grads.
Un-zoom	resets the viewing window to its last settings following a zoom.

Example:

1. Graph the sine function once again using the default plot settings.
2. Press **MENU**
3. Press **ZOOM**
4. Select Box . . . and press **OK**.
5. The cursor is at the origin Press **OK** to make the origin the first corner of the zoom box.
6. Press **▶** to move the cursor to X=3.
7. Press **▲** to move the cursor to Y=1. You'll see a box being drawn.
8. Press **OK**. The viewing window has changed to encompass the area between [0,0] and [3,1].



Function tools

The menu key labeled **FCN** in the Function applet's Plot view brings up a menu list of tools to help you analyze the important characteristics of functions.

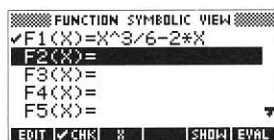
Example:

1. Open the Function applet and define the function

$$\frac{x^3}{6} - 2x$$

APLET **START**

X,T,θ **x^y** 3 **÷** 6 **-** 2 **X** **X,T,θ** **ENTER**



2. Reset plot view settings.

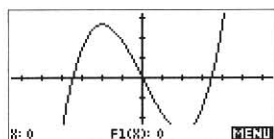
SHIFT **SETUP-PLOT**

SHIFT **CLEAR**



3. Plot the function

PLOT



4. Move the cursor along the graph until it reaches X=3.

▶ (until X: 3)

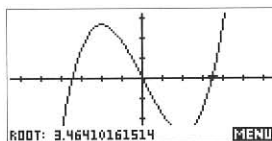
5. Display the Plot FCN menu.

MENU **FCN**



Finding roots

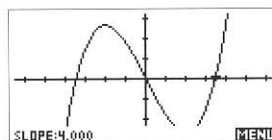
Select **Root** and press **OK**. The cursor moves to the nearest root. You should see **ROOT:** 3.46410161514 at the bottom left of the screen. This value is also recorded in a variable named **Root** that you can access from the **HOME** screen.



- ☞ Where a function has more than one root, the root closest to the cursor is returned.

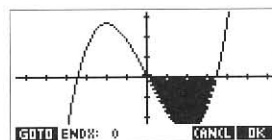
Finding slopes

Press **MENU**, **FCN**, select **Slope** and press **OK**. This calculates the derivative of the function at the x -coordinate of the cursor crosshairs location. You should see **SLOPE:** 4.000 at the bottom of the screen. This value is also recorded in a variable named **Slope**.



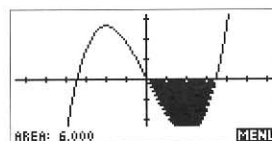
Finding integrals

Press **MENU**, **FCN** and select **Signed area...**. When you press **OK**, you are prompted for a *starting point* (lower limit of integration). Press **OK** and the starting point is $X: 3.46410161514$. Now you are prompted for an *end point* (upper limit of integration). Press **◀** to move the cursor crosshairs over to $X: 0$ and watch as the region between the graph and the x -axis is shaded.



- ☞ You can also use **GOTO**. In this case, the area is not be shaded.

Press **OK** once again to compute the definite integral of the function from the starting point to the end point. You should see **Area:** 6.000 at the bottom of the screen. This value is also recorded in a variable called **Area**.

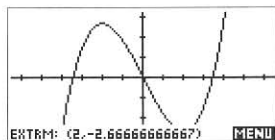


- ☞ The **Signed area...** option computes a definite integral, so if the function graph lies below the x -axis the resulting area is negative.

- ☞ To clear the shaded region created by the Signed area... option, press **PLOT** to redraw the function graph.

Finding extrema

Press **▶** to move the cursor is near $X = -2.5$. Press **MENU**, **F6**, select Extremum and press **03**. The cursor moves to the nearest extremum and displays its coordinates. You should see **EXTRM:** $(-2, 2.66666666667)$ at the bottom of the screen. This value is recorded in a variable named Extremum.



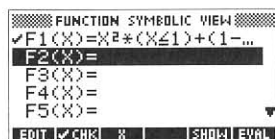
Plotting piece-wise functions

Suppose $f(x) = x^2$ if $x \leq 1$, and $f(x) = 1 - x$ if $x > 1$.

Method 1

1. Start the Function applet and enter the function.

APLET Select Function **START**
SHIFT **CLEAR**
(**X,T,θ** **)** **x²** **)** **X** **(** **X,T,θ** **)** **SHIFT** **CHARS** **≤**
03 **1** **)** **+** **(** **1** **-** **X,T,θ** **)** **X** **(** **X,T,θ** **)**
SHIFT **CHARS** **>** **03** **1** **)** **ENTER**

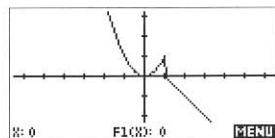


- ☞ To obtain the inequality symbols, press **SHIFT** **CHARS** menu, highlight the desired symbol using the arrow keys and press **ENTER**.

2. Plot the function.

PLOT

Note: If the plotting parameters are set so that plotted points will be connected—the default setting—the graph will connect across the jump discontinuity.



Method 2

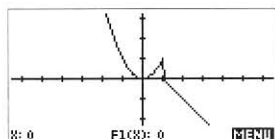
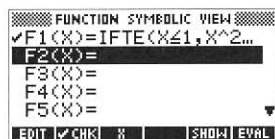
An equivalent of the above piece-wise function is IFE ($X \leq 1, X^2, 1-X$). This expression can be read as saying "if $x \leq 1$, then evaluate x^2 , else evaluate $1-x$."

- Return to the Symbolic view and enter the function.

[SYMB] [SHIFT] CLEAR
 [ALPHA] I F T E [] [X,T,θ] [SHIFT] CHARS ≤ [OK] 1
 [] [X,T,θ] [x^y] 2 [] 1 - [X,T,θ] [] [ENTER]

- Plot the function.

[PLOT]



Plotting multiple functions

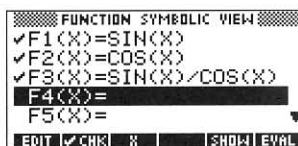
You can plot up to 10 functions at once.

- Return to the Symbolic view and enter the functions.

[SYMB] [SHIFT] CLEAR [OK]
 [SIN] [X,T,θ] [ENTER]
 [COS] [X,T,θ] [ENTER]
 [SIN] [X,T,θ] [] + [COS] [X,T,θ] [] [ENTER]

- Set up the plot.

[SHIFT] SETUP-PLOT
 [SHIFT] CLEAR



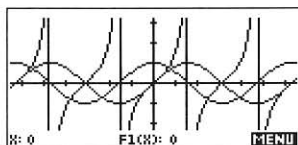
- Plot the functions

[PLOT]

Whether or not these functions are plotted simultaneously or sequentially is determined by whether or not SIMULT is checked in the FUNCTION PLOT SETUP.

Press [▲] or [▼] to move the cursor from graph to graph.

Press [F1] to see the equation of whatever function is currently being traced.

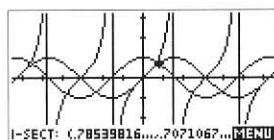


Finding intersections and areas between two graphs

If you have plotted two or more functions, an additional function tool called **Intersection** appears on the **2ND** menu.

Selecting this option uses the function currently selected and prompts you to choose either one additional function or the X-Axis.

Pressing **2ND** moves the cursor to the nearest intersection point of the two selected graphs (or the nearest root if you choose X-Axis), displays its coordinates, and records the coordinates in the variable **Isect**.



7. Working with Tables

These examples illustrate some of the tools available in the Numeric view (**NUM**). All the examples are for Function, but many of the features are similar for Parametric, Polar, Sequence, Solve, and Statistics.

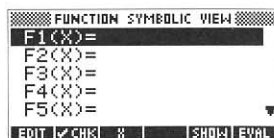
Open the applet

1. Open the Function applet.

APLET

Highlight Function

START



Define the function

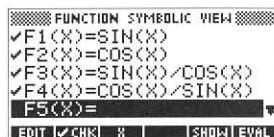
2. Enter these four functions.

SIN **(X,T,θ)** **ENTER**

COS **(X,T,θ)** **ENTER**

SIN **(X,T,θ)** **)** **÷** **COS** **(X,T,θ)** **)** **ENTER**

COS **(X,T,θ)** **)** **÷** **SIN** **(X,T,θ)** **)** **ENTER**

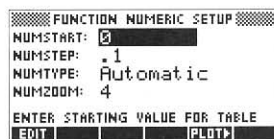


Set up the table

3. Return the numeric table settings to their default settings (where the starting value is 0 and values are automatically incremented in steps of 0.1).

SHIFT **SETUP-NUM**

SHIFT **CLEAR**



Numeric setup fields

Use the Numeric Setup to set up parameters for building a table of values for a function.

NUMSTART: the starting value for X

NUMSTEP: the step value (increment) for X

NUMTYPE: Automatic to let the HP 39G/40G generate values for X.
Build Your Own to fill in your own values for X

NUMZOOM: the zoom factor for your table

Display the table

4. Display the table.

NUM

The **▲**, **▼**, **▶**, **◀** keys enable you to move from entry to entry of the table.

5. To find the value of $F_4(X)$ when $X = 0.2$, scroll to the F_4 column.

▼ ▼ ▶ ▶ ▶ ▶

The full precision of a highlighted entry is displayed at the bottom of the screen.

6. Increase the font size in the table.

BIG

7. Decrease the font size in the table.

BIG

8. Display the equation of $F_2(X)$.

◀ ◀ DEFN

9. Display the list of zoom methods.

ZOOM

X	F1	F2	F3
0	0	1	0
.1	.0998334	.9950042	1.003347
.2	.1986693	.9800666	2.0271
.3	.2955202	.9553365	3.093362
.4	.3894183	.921061	.4227932
.5	.4794255	.8775826	.5463025

0

ZOOM **BIG** **DEFN**

X	F2	F3	F4
0	1	0	UNDEF.
.1	.9950042	1.003347	.996644
.2	.9800666	2.0271	.993155
.3	.9553365	3.093362	.987728
.4	.921061	.4227932	.965222
.5	.8775826	.5463025	1.830488

4.93315487559

ZOOM **BIG** **DEFN**

X	F3	F4
0	0	UNDEF.
.1	.100335	.996644
.2	.20271	4.933155
.3	.309336	3.23273

4.93315487559

ZOOM **BIG** **DEFN**

X	F2	F3	F4
0	1	0	UNDEF.
.1	.9950042	1.003347	.996644
.2	.9800666	2.0271	.993155
.3	.9553365	3.093362	.987728
.4	.921061	.4227932	.965222
.5	.8775826	.5463025	1.830488

COS(X)


ZOOM **BIG** **DEF**

X	F2	F3	F4
0	In		EF
.1	Out		.9644
.2	Decimal		.3155
.3	Integer		.2728
.4	Trig		.5222
.5			.0488

COS **CANCEL** **OK**

Zoom options

- In will *zoom in* by the zoom factor.
- Out will *zoom out* by the zoom factor.
- Un-zoom resets the table to its last settings.
- Decimal restores the default settings.
- Integer sets the starting value NUMSTART to 0 and the step size NUMSTEP to 1 unit.
- Trig sets the starting value NUMSTART to 0 and the step size NUMSTEP to approximately $\pi/24$ units. If the angle measure mode is *degrees*, then the NUMSTEP is 7.5 degrees.

 You can change the designated zoom factor by pressing **[SHIFT] SETUP-NUM** and editing NUMZOOM. The default zoom factor is 4.

10. Display the table using the zoom out method.

Zoom

Select Out

0.4

X	F1	F2	F3
-9	-783327	62161	-1.26016
-8	-479426	8775826	-1.546302
-7	-249833	9950042	-1.00335
-6	2455202	4553365	3093362
-5	6442177	7648422	8422884
-4	8912074	4535461	1.46476

COS(X)

Zoom **BIG** **DEF**

The table is recomputed so that .3 is still highlighted, but now the step sizes are .4 instead of .1. That is, the step size is multiplied by the zoom factor. If we had zoomed in instead of zooming out, the step size would have been divided by the zoom factor.

8. Special Views

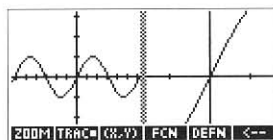
Press **[VIEWS]** to obtain a menu list of special viewing screens.



Split screen—two graphs

Plot-Detail splits the screen into two vertical panes and draws a copy of the graph in each pane. It allows you to see a before-and-after view of a graph that you modify in some way.

For example, if you press **[ZOOM]** and select a zoom option, the left graph remains unchanged but the right graph is re-plotted according to the zoom option you chose. The example at the right shows two views of the graph of $\sin(x)$. In the left pane is the graph plotted according to the default plot setup parameters; in the right is the same graph viewed by zooming in about the origin.

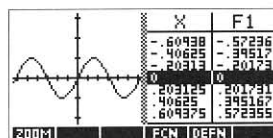


You can trace a graph and see the cursor move in both panes simultaneously.

Press **[<=>]** to copy the new graph to the left pane. You can repeat this process as many times as you wish.

Split screen—graph and table

Plot-Table splits the screen into two vertical panes and draws the graph in the left pane and the corresponding table in the right pane. It enables you to see both the **PLOT** and **NUMERIC** views of your function at the same time.



As you move the trace on the graph, the corresponding coordinates are highlighted in the table.

Overlaying one graph on another

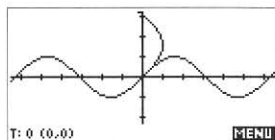
Overlay Plot enables you to plot a graph over your last graph without erasing it.

For example, suppose you plot $F1(X) = \sin(X)$ in the default window. If you switch from Function to Parametric in **[APLET]** you can use Overlay Plot (with the same window settings) to overlay the graph of

$$X1(T) = \sin(T)$$

$$Y1(T) = T$$

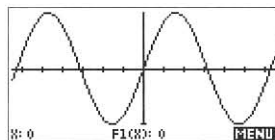
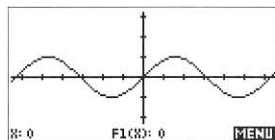
on top of the old graph to show the inverse relation.



Automatic scaling

Auto Scale will automatically scale the vertical range so as to fill as much of the screen as possible while still showing the origin, minima, and maxima.

The first example at the right shows the default display of $F1(X) = \sin(X)$. The second example shows the same function after choosing **[VIEWS]** Auto Scale.




Special preset zoom windows

Decimal sets the tick marks along the x -axis to be one unit apart (so that each pixel width = 0.1 units). Note that this effectively sets the viewing window back to its default ranges: $[-6.5, 6.5]$ by $[-3.1, 3.2]$ for functions.

Integer sets the tick marks along the x -axis to be ten units apart (so that each pixel width = 1 unit).

Trig sets the tick marks along the x -axis to be approximately $\pi/2$ units apart, and each pixel width is approximately $\pi/24$ units. If the angle measure mode is *degrees*, then Trig sets the tick marks along the x -axis to be 90 degrees apart, and each pixel width is 7.5 degrees.

 The autoscaling and special preset zoom window views are also available in the **[ZOOM]** menu when you are in Plot view.

9. Functions

1. To open the Function applet, press **[APLET]**
2. Highlight Function.
3. Press **[ENTER]**.

The FUNCTION SYMBOLIC VIEW is displayed. On this screen you define the functions that you want to plot.

You can define up to 10 functions: $F1(X)$, $F2(X)$... $F0(X)$.

Example:

1. With $F1(X)$ = highlighted, type **[SIN]** **[X,T,θ]**
[ENTER].

When Function is activated, **[X,T,θ]** inserts the variable X whenever you press it. There is also a **[$\frac{\pi}{180}$]** menu key to assist in entering formulas.

Note that the closing parenthesis is entered for you.

The **✓** indicates that $F1(X)$ is selected for graphing or making a table. An equation or automatically selected on entry.

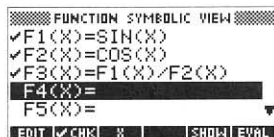
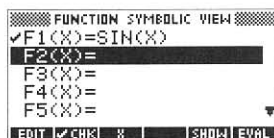
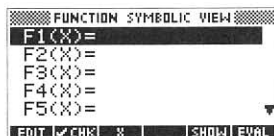
The menu keys you have access to while the FUNCTION SYMBOLIC VIEW screen is displayed are explained in "Function applet's symbolic view keys" on page 38.

2. With $F2(X)$ = highlighted, type **[COS]** **[X,T,θ]**
[ENTER].
3. With $F3(X)$ = highlighted, type
[ALPHA] **F1** **[$\left(\right)$]** **[X,T,θ]** **[$\right)$]** **[+]** **[ALPHA]** **F2** **[$\left(\right)$]** **[X,T,θ]** **[$\right)$]** **[ENTER]**.
4. Once you have defined the functions you want to plot, you can view and, if necessary, change the plot setup parameters.

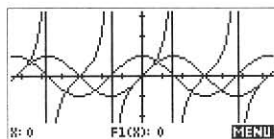
These parameters determine the plotting range, tickmark spacing, resolution, and so on.

[SHIFT] **SETUP-PLOT**.

Note that there are two pages of plot setup parameters. Press **[PAGE]** to display the second page.



5. To plot the functions, press **PLOT**.



6. To view and, if necessary, change the table setup parameters, press **SHIFT** **SETUP-NUM**.

These parameters determine the starting value for the independent variable, the increment for consecutive values of the independent variable, whether the calculator or the user determines the values of the independent variable, and the zoom factor for table zooming.

FUNCTION NUMERIC SETUP	
NUMSTART:	0
NUMSTEP:	.1
NUMTYPE:	Automatic
NUMZOOM:	4
ENTER STARTING VALUE FOR TABLE	
EDIT	PLT

7. To display the table, press **NUM**.

X	F1	F2	F3
0	0	1	0
.1	.0498334	.9950042	.1003347
.2	.1986693	.9800666	.20271
.3	.2955202	.9553365	.3093362
.4	.3844183	.921061	.4227932
.5	.4744255	.8775826	.5463025
ZOOM			
		BIG	DEFN

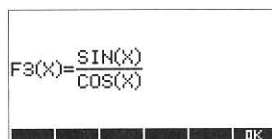
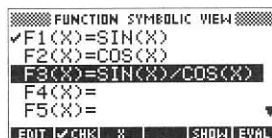
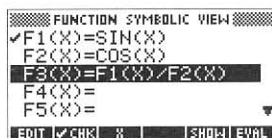
Function applet's symbolic view keys

- Press **EDIT** to copy the highlighted function to the edit line.
- Press **CHK** to select or deselect an equation. A \checkmark indicates that the equation is selected. Any or all of the functions can be selected at any time.
- Press **X** to enter the independent variable. It is another X key for typing convenience.
- Press **SHOW** to display the highlighted function in standard textbook format.
- Press **EVAL** to evaluate dependent variables or functions used in the highlighted equation.
- Press **OK** to enter the edited version.
- Press **CANCEL** to restore the original.

Example:

Press **[SYMB]** to return to the FUNCTION SYMBOLIC VIEW screen.

1. Highlight $F2(X)$ and press **[CHK]**.
2. Highlight $F3(X)$ and press **[CHK]**.
3. Highlight $F3(X) = F1(X) / F2(X)$ and press **[EVAL]**.
4. Press **[SHOW]** to see $F3(X) =$ as a fraction in vertical form.
5. Press **[OK]** to close the **[SHOW]** window.



Deleting and clearing functions

Press **[DEL]** to delete a highlighted function. Press **[SHIFT] CLEAR** to delete *all* the functions.

- ☞ When you press **[SHIFT] CLEAR**, you are asked if you really want to Clear All functions. Press **[YES]** or **[NO]**.

10. Parametric Equations

1. To open the Parametric applet, press **APLET**
2. Highlight Parametric.
3. Press **START**.

The PARAMETRIC SYMBOLIC VIEW is displayed, listing 10 pairs of parametric equation variables: $X1, Y1, X2, Y2, \dots, X9, Y9, X0, Y0$.

Parametric equations are checked in pairs. When you select or deselect one member of the pair, the other member is also automatically selected or deselected.

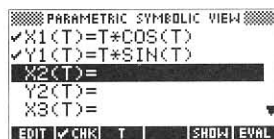
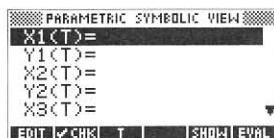
Example:

Suppose that you want to explore the following set of parametric equations:
 $x(t) = t \cos t$ and $y(t) = t \sin t$ for $0 \leq t \leq 2\pi$.

For the purposes of this example, ensure that the current angle measure mode is Radians.

1. Enter the equations.

X,T,θ **X** **COS** **X,T,θ** **ENTER**
X,T,θ **X** **SIN** **X,T,θ** **ENTER**



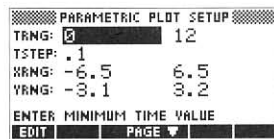
When Parametric is activated, **X,T,θ** provides the variable T whenever you press it. There is also a **⏏** menu key to assist with the entry of equations.

The **EDIT**, **CHK**, **SHOW**, and **EVAL** menu keys operate in exactly the same way as the menu keys in the Function applet. See "Function applet's symbolic view keys" on page 38 for further information.

2. Once you have defined the equations you want to plot, you can view and, if necessary, change the plot setup parameters.

These parameters determine the plotting range, and the independent variable's range and increment value.

SHIFT **SETUP-PLOT**.



Note that there are two pages of plot setup parameters. Press **PAGE** to display the second page.

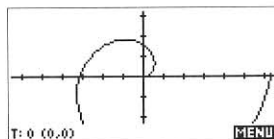
- Reset all the plot settings.

SHIFT **CLEAR**.

- Plot the equations.

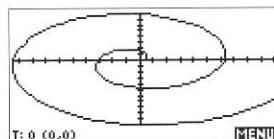
PLOT

Both the value of the independent variable T and the coordinates $(X1(T), Y1(T))$ are shown as you trace the curve. You can trace beyond the original domain in either direction.



- You can change the scale to see more or less of your graph. In this example, choose Auto Scale. See "Special Views" on page 35 for a description of Auto Scale.

VIEWS *Select Auto Scale* **0/2**



See "Zooming options" on page 26 for further information on zooming.

- Display the table of values for T , $X1(T)$, and $Y1(T)$.

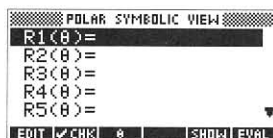
NUM

T	X1	Y1
0	0	0
.1	.0995004	.0099833
.2	.1960133	.0397339
.3	.2866009	.0886561
.4	.3684244	.1557673
.5	.4387413	.2347128

See "Working with Tables" on page 32 for further information on zooming within a table and tools for analyzing the table.

11. Polar Equations

1. To open the Polar applet, press **APLET**.
2. Highlight Polar.
3. Press **START**.



The POLAR SYMBOLIC VIEW is displayed, listing the 10 polar equation variables: R1, R2, R3, ..., R9, R0.

Example:

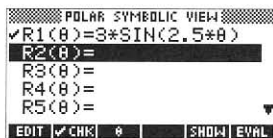
Suppose that you want to explore the equation $r(\theta) = 3 \sin(2.5\theta)$ for $0 \leq \theta \leq 4\pi$.

For the purposes of this example, ensure that the current angle measure mode is Radians.

1. Enter the equation.

3 **x** **SIN** 2.5 **X,T,θ** **ENTER**

When Polar is activated, **X,T,θ** provides the variable θ whenever you press it. There is also a **0** menu key to assist in the entry of equations.



The **EDIT**, **CHECK**, **SHOW**, and **EVAL** menu keys operate in exactly the same way as in the Function applet. See "Function applet's symbolic view keys" on page 38 for further information.

2. Display the POLAR PLOT SETUP screen.

SHIFT **SETUP-PLOT**.

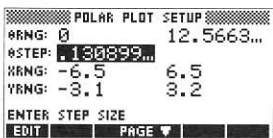
θ RNG is the plotting range of the angle θ .

θ STEP is the increment size used to determine what values for θ to plot within the plotting range.



3. Change the upper limit of θ RNG to 4π .

▶ 4 **SHIFT** **π** **ENTER**

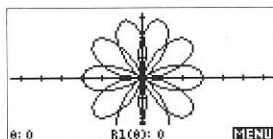


- Plot the equation

PLOT.

The values of θ and $R1(\theta)$ are shown at the bottom of the screen as you trace the curve.

- Display the table of values for θ and $R1(\theta)$ by pressing **NUM**.



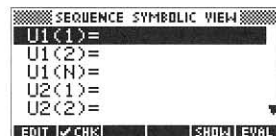
θ	$R1$		
0	0		
1	2.422114		
2	1.438277		
3	1.044916		
4	0.524413		
5	0.046454		
6			
ZOOM			
SIG DEFN			

12. Sequences

1. To open the Sequence applet, press **APLET**
2. Highlight **Sequence**.
3. Press **START**.



The **SEQUENCE SYMBOLIC VIEW** is displayed, listing the 10 sequence variables $U1(N)$, $U2(N)$, $U3(N)$... $U9(N)$, $U0(N)$.



To allow for recursive definitions of sequences, there are also variables for specifying the first one or two terms of a sequence: $U1(N1)$, $U1(2)$, $U2(1)$, $U2(2)$... $U0(1)$, $U0(2)$.

Example:

The simplest kind of sequence is one where the n th term is a function of n . An example is the geometric sequence 1, 1/2, 1/4, 1/8, ... This can be expressed as:

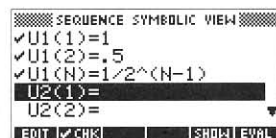
$$U_N = 1/2^{(N-1)}.$$

1. Enter the equation for the sequence against $U1(N)$.

▼ ▼ to move to $U1(N)$

1 **÷** 2 **x^y** **1/2** **ENTER**.

The values for the first two terms $U1(1)$ and $U1(2)$ are automatically computed and displayed.



When Sequence is activated, **X,T,θ** provides the variable n whenever you press it. The **1/2**, **1/4**, **1/8** and **1/16** menu keys assist in the entry of sequences.

The **EDIT**, **CHK**, **SHOW**, and **EVAL** menu keys operate in exactly the same way as in the Function applet. See "Function applet's symbolic view keys" on page 38 for further information.

2. Display the **SEQUENCE PLOT SETUP** screen.

SHIFT **SETUP-PLOT**.



- Since $1/2^{(N-1)} \leq 1$ for all positive integers, you will see more of the plot if you set the YRNG filed accordingly, such as to $[-.2, 1.06]$.

```

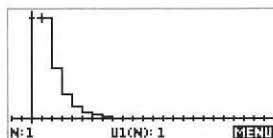
SEQUENCE PLOT SETUP
SEQPLOT: Stairstep
NRNG: 1 24
XRNG: -2 24
YRNG: -.2 1.06
CHOOSE SEQUENCE PLOT TYPE
CHOOSE PAGE

```

- Plot the sequence.

PLOT

Both the value of the index N and the value of the N th term, $U1(N)$, are shown as you trace the curve



- Display a table of values for N and $U1(N)$.

NUM

N	U1		
1	1		
2	.5		
3	.25		
4	.125		
5	.0625		
6	.03125		
1			
200M		BIG	DEFN

Iterative sequences

You can also define a sequence iteratively.

Example:

A certain sequence derived from Newton's Method can be defined iteratively.

- Press **SYMB** and uncheck $U1(1)$, $U1(2)$, or $U1(N)$.
- Highlight $U2(1)$ and enter 2.
- Highlight $U2(2)$ and enter 1.5.
- Highlight $U2(N)$ and enter:

$$U2(N-1) / 2 + 1 / U2(N-1)$$

- Ensure that the plot setup parameters are set to their default values.

SHIFT **SETUP-PLOT**

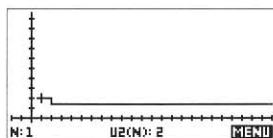
SHIFT **CLEAR**

Press **PLOT** to plot the sequence.

```

SEQUENCE SYMBOLIC VIEW
U1(2)=.5
U1(N)=1/2^(N-1)
✓U2(1)=2
✓U2(2)=1.5
✓U2(N)=U2(N-1)/2+1/U2(N-1)
EDIT ✓CHK SHOW EVAL

```



You can see how quickly this sequence converges to $\sqrt{2}$ by pressing **NUM**.

N	U2		
1	2		
2	1.5		
3	1.416667		
4	1.414216		
5	1.414214		
6	1.414214		
7	1.414214		
8	1.414214		
9	1.414214		
10	1.414214		
11	1.414214		
12	1.414214		
13	1.414214		
14	1.414214		
15	1.414214		
16	1.414214		
17	1.414214		
18	1.414214		
19	1.414214		
20	1.414214		
21	1.414214		
22	1.414214		
23	1.414214		
24	1.414214		
25	1.414214		
26	1.414214		
27	1.414214		
28	1.414214		
29	1.414214		
30	1.414214		
31	1.414214		
32	1.414214		
33	1.414214		
34	1.414214		
35	1.414214		
36	1.414214		
37	1.414214		
38	1.414214		
39	1.414214		
40	1.414214		
41	1.414214		
42	1.414214		
43	1.414214		
44	1.414214		
45	1.414214		
46	1.414214		
47	1.414214		
48	1.414214		
49	1.414214		
50	1.414214		
51	1.414214		
52	1.414214		
53	1.414214		
54	1.414214		
55	1.414214		
56	1.414214		
57	1.414214		
58	1.414214		
59	1.414214		
60	1.414214		
61	1.414214		
62	1.414214		
63	1.414214		
64	1.414214		
65	1.414214		
66	1.414214		
67	1.414214		
68	1.414214		
69	1.414214		
70	1.414214		
71	1.414214		
72	1.414214		
73	1.414214		
74	1.414214		
75	1.414214		
76	1.414214		
77	1.414214		
78	1.414214		
79	1.414214		
80	1.414214		
81	1.414214		
82	1.414214		
83	1.414214		
84	1.414214		
85	1.414214		
86	1.414214		
87	1.414214		
88	1.414214		
89	1.414214		
90	1.414214		
91	1.414214		
92	1.414214		
93	1.414214		
94	1.414214		
95	1.414214		
96	1.414214		
97	1.414214		
98	1.414214		
99	1.414214		
100	1.414214		

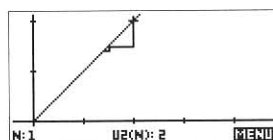
Cobweb plots

Iterative sequences are best displayed using a *cobweb* plot. In a cobweb plot, the first term of a sequence U_1 is located as the point (U_1, U_1) on the line $y = x$. This point is connected with a vertical line segment to (U_1, U_2) which in turn is connected with a horizontal line segment to (U_2, U_2) . This process is then continued to form a web of line segments connecting (U_2, U_2) to (U_3, U_3) to (U_4, U_4) and so on. If the sequence converges, one sees the web close in on a particular point.

To see a cobweb plot for the sequence we just defined:

1. Press **SYMB** to return to the SEQUENCE SYMBOLIC VIEW.
2. Select U2 in **SYMB** (and deselect any other sequences defined).
3. Press **SHIFT** **SETUP-PLOT** to bring up the SEQUENCE PLOT SETUP.
4. Highlight SEQPLOT, **CHOOSE** Cobweb, and press **OK**.
5. Set the viewing window to $[-.4, 4.8]$ by $[-.4, 2.12]$
6. Press **PLOT** to see the cobweb plot.

If you trace the cobweb plot near the point of convergence, you can **ZOOM** In to see more detail.



13. Solving Equations

The Solve applet enables you to find roots of expressions and solve equations.

1. To open the Solve applet, press **APLET**
2. Highlight Solve.
3. Press **START**.



The SOLVE SYMBOLIC VIEW is displayed, listing the 10 equation variables: E1, E2, E3 ... E9, E0.



Analyzing an expression in one variable

This example illustrates how to find a root of the expression $X^2 - 3$.

1. Enter the equation.

X,T,θ **x^y** 2 **-** 3 **ENTER**

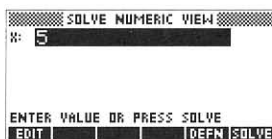
When Solve is activated, **X,T,θ** provides the variable X whenever you press it. However, you can use any real variables you wish in your equations.



The **EDIT**, **CHK**, **SHOW**, and **EVAL** menu keys operate in exactly the same way as in the Function applet. See "Function applet's symbolic view keys" on page 38 for further information.

2. Display the SOLVE NUMERIC VIEW screen and specify a value for X (in this case, 5) to act as an initial seed value.

NUM
5 **ENTER**



3. Solve for the unknown variable.

SOLVE

The root closest to the seed value is returned.
Different roots may be found by changing the seed value.



Solve aplet's numeric view menu keys

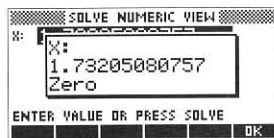
- Press **SOLVE** to edit the current value of the highlighted variable
- Press **INFO** to display a message about the solution (see below).
- Press **DEFN** to display the symbolic definition of the current expression.
- Press **SOLVE** to find a solution for the highlighted variable, based on the values of the other variables.

The following is a brief description of **INFO** messages:

Zero indicates that the displayed value X is a root (making $E1: X^2 - 3$ equal to 0) to 12 digits of precision.

Sign Reversal indicates that the value of the expression changes sign (from positive to negative or vice-versa) by a change in the last digit of the displayed solution of X . (Note: if the expression is the formula for a continuous function, the displayed value is within one digit of a root.)

Extremum generally indicates that the displayed value X minimizes the absolute value of the expression, but no sign reversal is obtained.



- When you return to the HOME screen after using the Solve aplet, any variables used will have their last values shown in the SOLVE NUMERIC VIEW.

Analyzing an equation with several variables

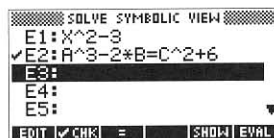
An equation can have any number of variables. Providing that you know the values of all the other variables, you can use the Solve aplet to solve the value of a specified variable. For example, if $a^3 - 2b = c^2 + 6$, you can solve for b if you know the values of a and c .

1. Return to the SOLVE SYMBOLIC VIEW and enter the equation.

SYMB

▼ to highlight E2 :

ALPHA A **x^y** 3 **=** 2 **x** **ALPHA** B **=**
ALPHA C **x^y** 2 **+** 6 **ENTER**



Note: E1: has been automatically deselected. This is because only one equation can be checked at a time in the Solve aplet.

2. Enter the known variables in the Numeric view.

NUM

3 ENTER

▼

(-) 5 ENTER

3. Solve for the variable B.

▼ to highlight B:

SOLVE

```
SOLVE NUMERIC VIEW
A: 3
B: 0
C: -5
ENTER VALUE OR PRESS SOLVE
EDIT DEFN SOLVE
```

```
SOLVE NUMERIC VIEW
A: 3
B: -1.999999999999999
C: -5
ENTER VALUE OR PRESS SOLVE
EDIT INFO DEFN SOLVE
```

14. Statistics

The Statistics applet can store up to ten separate data sets. It can do one-variable or two-variable statistical analysis of one or more sets of data.

To start Statistics, press **[APLET]**, select Statistics, and press **START**. The Statistics applet starts in Numeric view, which is used to enter data. Each column represents a variable named C1 to C9 and C0.

n	C1	C2	C3	C4
1				

EDIT INS SORT BIG EVAR STATS

After entering the data, you must define the data set in the Symbolic view (**[SYMB]**).

The values computed in the Statistics applet are saved in variables, and many of these variables are listed by the **STATS** function accessible from the Statistics applet's Numeric view screen.

Example: one-variable statistics

Suppose that a manufacturing company purchases a certain part four times a year. In the last year, the price and the number of units ordered each time was \$4.25 (250 units), \$4.60 (800 units), \$4.70 (900 units), and \$4.10 (1,000 units).

1. Open the Statistics applet.

[APLET] Select Statistics
RESET **WES**
START

APLET LIBRARY		BACK
Statistics	.07KB	
Function	0KB	
Inferential S...	.54KB	
Parametric	0KB	
Polar	0KB	
SAVE	RESET	SORT SEND RECV START

2. Enter the prices paid in column 1.

4.25 **[ENTER]**
 4.60 **[ENTER]**
 4.70 **[ENTER]**
 4.10 **[ENTER]**

n	C1	C2	C3	C4
1	4.25			
2	4.60			
3	4.70			
4	4.10			

EDIT INS SORT BIG EVAR STATS

3. Enter the corresponding frequencies (that is, number of parts purchased) in column C2.

[▶] 250 **[ENTER]**
 800 **[ENTER]**
 900 **[ENTER]**
 1000 **[ENTER]**

n	C1	C2	C3	C4
1	4.25	250		
2	4.60	800		
3	4.70	900		
4	4.10	1000		

EDIT INS SORT BIG EVAR STATS

4. Ensure the **EVAR/EVAR** menu key label reads **EVAR**.

5. Press **[SYMB]**. The STATISTICS SYMBOLIC VIEW screen is where you specify what column holds the data to be analyzed. You can also specify the corresponding frequencies. The default frequency value is 1. You can overwrite this value with a new number if the frequency for each data point is not the same. If the frequency of each data point is not the same, you need to specify a frequencies column. In our example, the data to be analyzed is in column C1 and the corresponding frequency data is stored in column C2.

1-VAR STATISTICS SYMBOLIC VIEW	
✓H1: C1	C2
H2:	1
H3:	1
H4:	1
ENTER SAMPLE	
EDIT	✓CHK C
SHOW EVAL	

[▶] [2] [OK]

6. To compute statistics about the prices, return to the numeric view (**[NUM]**) and press **[STAT]**. There are two pages of statistics. Press **[▼]** several times to scroll to the second page.

1-VAR	H1		
NΣ	2950		
TOTΣ	13072.5		
MEANΣ	4.431356		
PVARΣ	.0647371		
SVARΣ	.0647608		
PSDEV	.2640774		
2950			
			OK

1-VAR	H1		
SSDEV	.2641227		
MINΣ	4.1		
Q1	4.1		
MEDIAN	4.6		
Q3	4.7		
MAXΣ	4.7		
4.7			
			OK

7. To plot a histogram of your data you will need to change the plot setup parameters so that all your data will be plotted.

[OK] [SHIFT] SETUP-PLOT

[▶] [1] [OK]

4 [OK] 5 [OK]

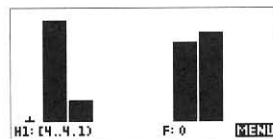
[(-)] 100 [OK] 1100 [OK]

4 [OK] 5 [OK]

1-VAR STATISTICS PLOT SETUP	
STATPLOT: Hist	HI-WIDTH: .1
X-RANG: 4	5
Y-RANG: -100	1100
X-RANG: 4	5
SELECT STATISTICS PLOT TYPE	
CROSS	PAGE

8. Plot a histogram of the data.

[PLOT]



Example: two-variable statistics

Suppose you want to explore the relationship between the temperature of a object and its volume.

1. Open the Statistics aplet.

APLET *Select Statistics*
 RESET YES
 START

APLET LIBRARY: 0000
 Statistics .07KB
 Function 0KB
 Inferential S... .54KB
 Parametric 0KB
 Polar 0KB
 SAVE RESET SORT SEND RECV START

2. Enter the temperatures in column C1.

9 ENTER
 8 ENTER
 7 ENTER
 5 ENTER
 7 ENTER

n	C1	C2	C3	C4
1	9			
2	8			
3	7			
4	5			
5	7			

EDIT INS SORT BIG LVAR=STATS

3. Move the cursor to column C2 and enter the the corresponding volumes.

▶ 7 ENTER
 8 ENTER
 4 ENTER
 8 ENTER
 6 ENTER

n	C1	C2	C3	C4
1	9	7		
2	8	8		
3	7	4		
4	5	8		
5	7	6		

EDIT INS SORT BIG 2VAR=STATS

4. Ensure the **LVAR/2VAR** menu key label reads **2VAR**.

5. To compute statistics about your data, press

STATS.

2-VAR	S1		
MEANX	7.2		
SEN	36		
SY2	668		
MEANY	6.6		
XY	33		
SY2	224		
7.2			

OK

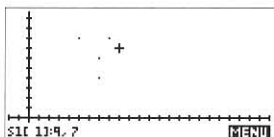
6. To view and, if necessary, change the parameters for plotting a scatter plot of your data

OK **SHIFT** *SETUP-PLT*

STATISTICS PLOT SETUP
 XRMG: -2 24
 YRMG: -2 10.6
 SIMARK: + S2MARK: x S3MARK: +
 S4MARK: :: S5MARK: x
 ENTER MINIMUM HORIZONTAL VALUE
 EDIT PAGE

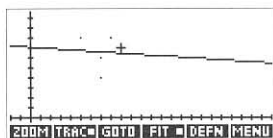
7. Draw a scatter plot of the data.

PLOT



8. To draw a regression line:

NEW FIT



9. To see the equation of the regression line:

SYMB ▼ **SHOW**

$-6.81818181818E-2X+7.1$

OK



**HEWLETT®
PACKARD**

Australian Calculator Operation
351 Burwood Highway
Forest Hill, 3131
Victoria, Australia

Printed in China

Manual p/n (ABA/ABB) F1906-90101

Scan Copyright ©
The Museum of HP Calculators
www.hpmuseum.org

Original content used with permission.

Thank you for supporting the Museum of HP
Calculators by purchasing this Scan!

Please do not make copies of this scan or
make it available on file sharing services.