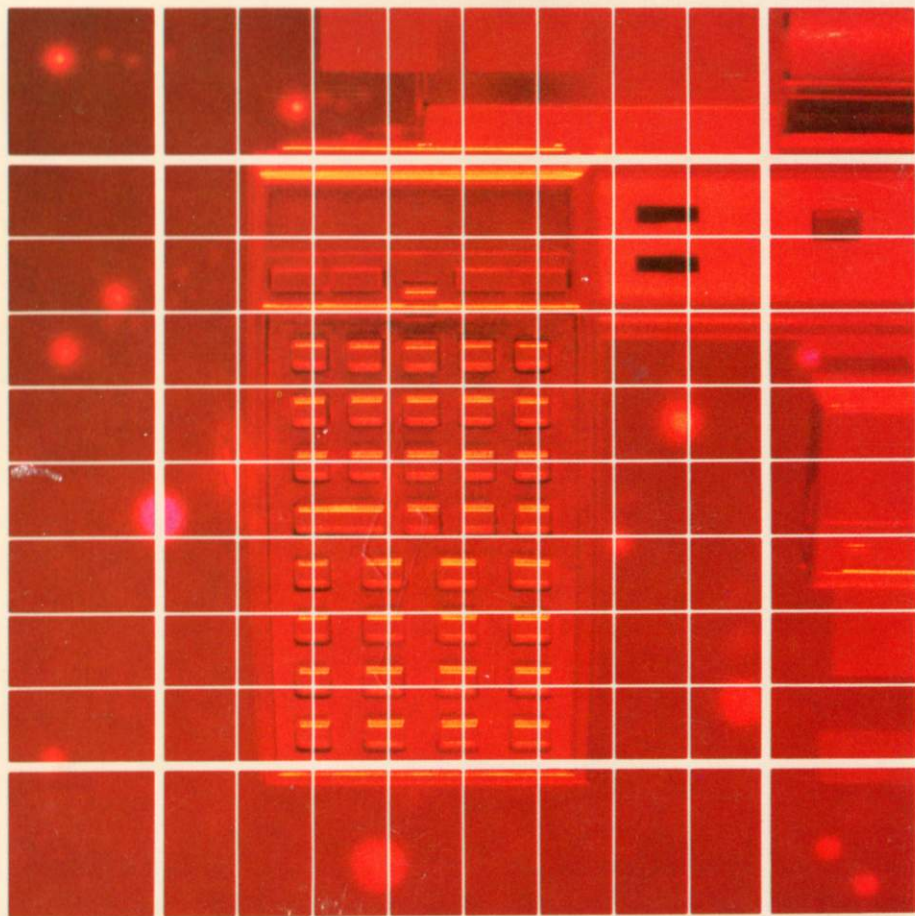


HEWLETT-PACKARD

HP-41C

STANDARD  
APPLICATIONS



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**HP-41C**

## **Standard Applications Handbook**

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## INTRODUCTION

This applications handbook contains a collection of programs that demonstrate the power and versatility of your HP-41C in programmed problem-solving. You will find the programs useful, entertaining, and fascinating. By entering and executing them, you'll get an immediate "hands-on" glimpse of the advanced capabilities of your HP-41C, and—thanks to its Continuous Memory—you'll have them available in the future ready to use.

Studying all of these professionally designed programs will help you develop your own programming expertise. The benefits of owning an HP-41C can be realized through the imaginative exploitation of its programming power and versatility, which enable you to customize your HP-41C to suit your particular needs.

For each of the 10 programs in this handbook we've included a description, instructions, one or more example problems, program highlights, and a program listing. Before entering any of the programs, take a few minutes to study the sections Reading a Program Listing and Format of User Instructions at the front of this handbook. You might understand them better and learn a lot more from them if you've first read through the *HP-41C Owner's Handbook and Programming Guide*.

When you've selected a program you'd like to execute, key it in by following the program listing, then refer to the table of instructions for detailed information on how to use the program. You'll probably need to refer to these instructions only the first few times you run the program. Afterwards, the program's prompting should provide the necessary instructions, including which data should be input, the keys to press, and the kind of output.

The Program Highlights present programming techniques of particular interest. Studying them will help you understand the operation of parts of the program, and you may find uses for them as part of programs you write yourself. For an in-depth understanding of the program's operation, and to learn more about efficient and versatile programming techniques, also study the comments included in the program listings.

Except for the blackjack game, all programs in this handbook can be keyed into the basic HP-41C. The blackjack game requires one additional memory module. As you expand your HP-41C system, you will find that some of these programs work well as a basis for larger programs of your own. You might want to modify some programs slightly to suit your individual needs—that's the beauty of programmability.



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## FORMAT OF USER INSTRUCTIONS

The User Instructions which accompany each program are your guide to operating the programs in this handbook.

The form is composed of five labeled columns. Reading from left to right, the first column, labeled STEP, gives the instruction step number.

The INSTRUCTIONS column gives instructions and comments concerning the operations to be performed.

The INPUT column specifies the input data, the units of data if applicable, or the appropriate alpha response to a prompted question. Data Input keys consist of 0 to 9 and the decimal point (the numeric keys), **EEEX** (enter exponent), and **CHS** (change sign).

The FUNCTION column specifies the keys to be pressed after keying in the corresponding input data.

Whenever a statement in the INPUT or FUNCTION column is printed in gold, the ALPHA mode must be on before the statement can be keyed in. For example, **XEQ A4C** means press the following keys: **XEQ** **ALPHA** A **4C** **ALPHA**. Of course, you could assign the function A4C to any key you chose by pressing **ASN** **ALPHA** A **4C** **ALPHA** **KEY**. Then you could simply press **KEY** in USER mode to execute the function.

The DISPLAY column specifies prompts as well as intermediate and final answers and (where applicable) their units.

Above the DISPLAY column is a box which specifies the SIZE or minimum number of data registers used by the program. Program memory should be SIZED before keying in the program or it might not fit. Refer to pages 73 and 117 in the Owner's Handbook for a complete description of how to size calculator memory.



## KEYING A PROGRAM INTO THE HP-41C

There are several things that you should keep in mind while you are keying in programs from the program listings provided in this book. The output from the HP 82143A printer provides a convenient way of listing and an easily understood method of keying in programs without showing every keystroke. This type of output is what appears in this handbook. Once you understand the procedure for keying programs in from the printed listings, you will find this method simple and fast. Here is the procedure:

1. At the end of each program listing is a listing of status information required to properly execute that program. Included is the SIZE allocation required. Before you begin keying in the program, press **XEQ** **ALPHA** **SIZE** **ALPHA** and specify the allocation (three digits; e.g., 10 should be specified as 010).

Also included in the status information is the display format and status of flags important to the program. To ensure proper execution, check to see that the display status of the HP-41C is set as specified and check to see that all applicable flags are set or clear as specified.

2. Set the HP-41C to PRGM mode (press the **PRGM** key) and press **□** **□** to prepare the calculator for the new program.
3. Begin keying in the program. Following is a list of hints that will help you when you key in your programs from the program listings in this handbook.
  - a. When you see " (quote marks) around a character or group of characters in the program listing, those characters are ALPHA. To key them in, simply press **ALPHA**, key in the characters, then press **ALPHA** again. So 06 "SAMPLE" would be keyed in as **ALPHA** **SAMPLE** **ALPHA**.
  - b. The diamond in front of each LBL instruction is only a visual aid to help you locate labels in the program listings. When you key in a program, ignore the diamond.
  - c. The printer indication of the divide sign is /. When you see / in the program listing, press **÷**.
  - d. The printer indication of the multiply sign is \*. When you see \* in the program listing, press **×**.
  - e. The † character in the program listing is an indication of the **APPEND** function. When you see †, press **APPEND** in ALPHA mode (press **□** and the K key).

- f. All operations requiring register addresses accept those addresses in these forms:
  - nn (a two-digit number)
  - IND nn (INDIRECT: **□**, followed by a two-digit number)
  - X, Y, Z, T, or L (a STACK address: **□** followed by X, Y, Z, T, or L)
  - IND X, Y, Z, T, or L (INDIRECT stack: **□** **□** followed by X, Y, Z, T, or L)

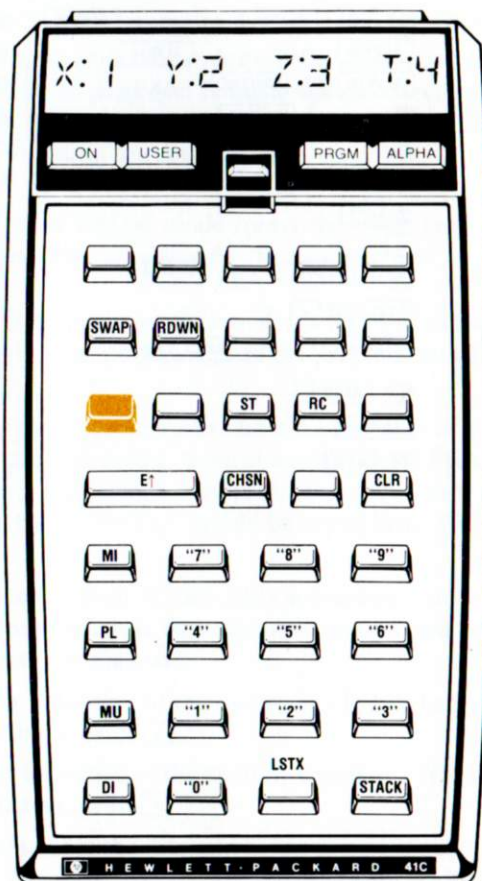
Indirect addresses are specified by pressing **□** and then the indirect address. Stack addresses are specified by pressing **□** followed by X, Y, Z, T, or L. Indirect stack addresses are specified by pressing **□** **□** and X, Y, Z, T, or L.

Printer Listing	Keystrokes	Display
01 ♦ LBL "SAMPLE"	<b>□</b> <b>LBL</b> <b>ALPHA</b> <b>SAMPLE</b> <b>ALPHA</b>	01 LBL † SAMPLE
02 "THIS IS A"	<b>ALPHA</b> <b>THIS IS A</b> <b>ALPHA</b>	02 † THIS IS A
03 "†SAMPLE"	<b>ALPHA</b> <b>APPEND</b> <b>SAMPLE</b>	03 † † SAMPLE
04 AVIEW	<b>AVIEW</b> <b>ALPHA</b>	04 AVIEW
05 6	6	05 6
06 ENTER†	<b>ENTER</b>	06 ENTER ↗
07 -2	2 <b>CHS</b>	07 -2
08 /	<b>÷</b>	08 /
09 ABS	<b>XEQ</b> <b>ALPHA</b> <b>ABS</b> <b>ALPHA</b>	09 ABS
10 STO IND	<b>STO</b> <b>□</b> <b>L</b>	10 STO IND L
11 "R3="	<b>ALPHA</b> <b>R3=</b> <b>ARCL</b> 03	11 R3=
12 ARCL 03	<b>ARCL</b> 03	12 ARCL 03
13 AVIEW	<b>AVIEW</b>	13 AVIEW
14 RTN	<b>ALPHA</b> <b>RTN</b>	14 RTN



## RPN PRIMER

This program is an aid to understanding and using RPN, the logic system used in the HP-41C. All four registers of the operational stack are visible simultaneously so that the effect of a given keystroke sequence can be seen rather than inferred. The functions provided, assigned as shown in the instructions, appear on the keyboard below. These functions all exit to a routine which displays the operational stack. It is possible to observe the effect on the stack of functions which are not included within this program. Simply execute the desired function, then press the **[R/S]** key, to which STACK is assigned. The only operational differences between this redefined calculator and the actual one are that only single-digit numbers can be keyed in and that STO/RCL address only a single register (thus requiring no address).



SIZE: 001				
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program			
2	Assign * its routines as shown and select USER mode. These suggested assignments result in the keyboard shown on the previous page.  SWAP <b>[X↔Y]</b> ST <b>[STO]</b> RDWN <b>[R*]</b> E↑ <b>[ENTER*]</b> RC <b>[RCL]</b> CLR <b>[—]</b> CHSN <b>[CHS]</b> PL <b>[+]</b> MI <b>[—]</b> MU <b>[x]</b> DI <b>[÷]</b> 9 9 8 8 7 7 6 6 5 5 4 4 3 3 2 2 1 1 0 0 LSTX <b>[LASTX]</b> STACK <b>[R/S]</b>			
3	Press desired keystroke sequence and watch stack contents change			
4	The functions RUP and CLSTK are obtained by and (or you could assign these functions as well)  *To assign a function, say FCN, to a key, say the <b>[√x]</b> key,		<b>[XEQ]</b> RUP <b>[XEQ]</b> CLSTK  <b>[ASN]</b> ALPHA <b>[FCN]</b> ALPHA <b>[√x]</b>	

### Example 1:

Evaluate the expression

$$\frac{(2 + b) b}{8 - b}$$

for b = 3

### Keystrokes:

#### Function

**[XEQ]** **[ALPHA]** CLSTK **[ALPHA]**

2

**[ENTER\*]**

### Display

X:0 Y:0 Z:0 T:0

X:2 Y:0 Z:0 T:0

X:2 Y:2 Z:0 T:0



3

+

LASTX

x

8

LASTX

-

+

X:3 Y:2 Z:0 T:0

X:5 Y:0 Z:0 T:0

X:3 Y:5 Z:0 T:0

X:15 Y:0 Z:0 T:0

X:8 T:15 Z:0 T:0

X:3 Y:8 Z:15 T:0

X:5 Y:15 Z:0 T:0

X:3 Y:0 Z:0 T:0

**Example 2:**

Without disturbing the above results, compute

$$\frac{2 + 4(9 - 7)}{6 - 4}$$

**Function**

9

ENTER

**Display**

X:9 Y:3 Z:0 T:0

X:9 Y:9 Z:3 T:0

After an **ENTER**,  
the stack does not  
lift when new data  
is keyed in

7

-

4

x

2

+

6

ENTER

4

-

+

X:7 Y:9 Z:3 T:0

X:2 Y:3 Z:0 T:0

X:4 Y:2 Z:3 T:0

X:8 Y:3 Z:0 T:0

X:2 Y:8 Z:3 T:0

X:10 Y:3 Z:0 T:0

X:6 Y:10 Z:3 T:0

X:6 Y:6 Z:10 T:3

X:4 Y:6 Z:10 T:3

X:2 Y:10 Z:3 T:3

X:5 Y:3 Z:3 T:3

Notice that the  
answer remaining  
from Example 1  
did not cause a  
difficulty in  
Example 2

**Example 3:**Convert the complex number  $3 + 4i$  to polar form.

4

ENTER

3

R-P

STACK

X:4 Y:5 Z:3 T:3

X:4 Y:4 Z:5 T:3

X:3 Y:4 Z:5 T:3

5

X:5 Y:53 Z:5 T:3

Remember that  
STACK is as-  
signed to **R/S**




**Programming Highlight**

What is especially useful in this program is the display routine STACK. You might like to keep it handy to view the entire stack from time to time as you solve your own problems.

01•LBL "CLS TK"		50 FS?C 05	
02 CLST	Clear stack.	51 CLX	Input a 0.
03 GT0 14		52 0	
04•LBL "1"		53 GT0 14	
05 FS?C 05	If lift disabled clear x first	54•LBL 13	Enable stack lift.
06 CLX		55 CF 05	
07 1	Input a 1.	56•LBL 14	
08 GT0 14		57•LBL "STR	
09•LBL "2"		CK"	
10 FS?C 05	See note	58 "X:"	Display stack.
11 CLX		59 ARCL X	
12 2	Input a 2.	60 "F Y:"	
13 GT0 14		61 ARCL Y	
14•LBL "3"		62 "F Z:"	
15 FS?C 05		63 ARCL Z	
16 CLX		64 "F T:"	
17 3	Input a 3.	65 ARCL T	
18 GT0 14		66 AVIEW	
19•LBL "4"		67 RTN	
20 FS?C 05		68•LBL "E↑"	Disable stack lift.
21 CLX		69 SF 05	
22 4	Input a 4.	70 ENTER↑	
23 GT0 14		71 GT0 14	
24•LBL "5"		72•LBL "RDW	
25 FS?C 05		N"	Roll down.
26 CLX		73 RDN	
27 5	Input a 5.	74 GT0 13	
28 GT0 14		75•LBL "SWA	
29•LBL "6"		P"	Swap x and y.
30 FS?C 05		76 X<>Y	
31 CLX		77 GT0 14	
32 6	Input a 6.	78•LBL "RUP	
33 GT0 14		"	Roll up.
34•LBL "7"		79 R↑	
35 FS?C 05		80 GT0 13	
36 CLX		81•LBL "PL"	Plus.
37 7	Input a 7.	82 +	
38 GT0 14		83 GT0 13	
39•LBL "8"		84•LBL "MI"	Minus.
40 FS?C 05		85 -	
41 CLX		86 GT0 13	
42 8	Input an 8.	87•LBL "MU"	Multiply.
43 GT0 14		88 *	
44•LBL "9"		89 GT0 13	
45 FS?C 05		90•LBL "DI"	Divide.
46 CLX		91 /	
47 9	Input a 9.	92 GT0 13	
48 GT0 14		93•LBL "CLR	
49•LBL "0"		"	
		94 SF 05	

R00 Storage

95 CLX	Disable stack lift and clear x.		
96 GT0 14			
97•LBL "CHS			
N"	Change sign.		
98 CHS			
99 GT0 14			
100•LBL "ST"	Store.		
101 ST0 00			
102 GT0 14			
103•LBL "RC"			
104 FS?C 05	If lift disabled clear x first.		
105 CLX	Recall.		
106 RCL 00			
107 GT0 14			
108•LBL "LST			
X"			
109 FS?C 05			
110 CLX			
111 LASTX			
112 GT0 14	This step need not be keyed in.		
Important Status			
Size = 001			
Fix 0			
Flags used			
F05 Set = Stack lift			
disable			
F29 Clear for no			
radix point			

**Note:** You will find it convenient to assign FS?C to some key, for example  **ASN**  FS?C  **LN** assigns FC?C to the **LN** key. You can then press **LN** once to get FS?C— in the display and a second time to create FS?C 05. Remember that you must be in USER mode or you will get two LN's instead.



## CALENDAR FUNCTIONS

This program provides an interchangeable solution of dates and days between dates. Given two dates, the program can determine the number of days between them, or it can compute a second date from a first one and a number of days. Dates are input in the form mm.ddyyyy. They are output as MONTH dd,yyyy.

Another feature of this program is that it can convert a date to its day of the week, displaying the result with the correct day name.

SIZE: 010			
STEP	INSTRUCTIONS	INPUT	FUNCTION
1	Set status, key in the program and select USER mode <b>DAY OF THE WEEK</b>		
2a	Input date and calculate day	DATE*	[E]
3a	Repeat step 2a for a new date <b>DAYS BETWEEN DATES</b>		
2b	Input two of the following: First date Second date Days between dates	D 1* D 2* D	[A] [B] [C]
3b	Calculate one of the following: First date Second date Days between dates		[A] [B] [C]
4	Repeat step 2b for new data (values which do not change need not be re-entered)  * Dates are input in the form mm.ddyyyy; they are output in the form MONTH dd,yyyy.		

### Example 1:

On what day of the week was February 19, 1946?

**Keystrokes:**

2.191946[E]

**Display:**

TUESDAY

### Example 2:

What date is 10,000 days after August 4, 1978?

**Keystrokes:**

8.041978[A] 10000[C][B]

**Display:**

DEC 20,2005

### Example 3:

A man born on December 18, 1913, is the father of a boy born on February 19, 1946. On what date will the father be twice as many days old as his son?

**Keystrokes:**

12.181913[A]

2.191946[B]

[C]

2[X][C][B]

**Display:**

DEC 18,1913

FEB 19,1946

11751

APR 23,1978

Number of days.  
Twice as many  
days after Date 1.

### Programming Highlight

This program utilizes the "selectable radix point" feature of the HP-41C to format its date display. With a date of the form mm.ddyyyy in the x-register, [XEQ] IND X executes a subroutine which places the three-letter month designation in the alpha-register. The program then multiplies the fractional part of X by 100, clears the decimal point flag, and appends the day and year to the alpha display. Thus an original x-value of 12.251978 yields a display of DEC 25,1978.

**Note:** Because of its length, this program was written using only local labels. If the program pointer should ever point to somewhere else in memory, you can move it back using CAT 1 as described on page 140 of your Owner's Handbook.

01*LBL A		52 -	
02 RCL 04	Calculate $\Delta$ days and put control 3 in display.	53 -	
03 RCL 01		54 RCL 07	
04 -		55 14	
05 3		56 /	
06 GT0 20		57 XEQ 22	
07*LBL B	Calculate $\Delta$ days and put control 4 in display.	58 RCL 09	
08 RCL 03		59 1 E6	
09 RCL 01		60 /	
10 +		61 +	
11 4		62 GT0 25	
12*LBL 20	Store control code.	63*LBL 21	Break date input into the individual com- ponents of mm,dd,yyyy.
13 ST0 02		64 RDN	
14 RDN		65 FC? 06	
15 365.25		66 ST0 IND	
16 ST0 05	Store constants.		
17 30.6001		02	
18 ST0 06		67 ENTER↑	
19 RDN	Return $\Delta$ days to display.	68 INT	
20 RDN		69 ST0 07	
21 FS?C 22		70 -	
22 GT0 21		71 1 E2	
23 ST0 IND	Store $\Delta$ days according to control code.	72 *	
02		73 ENTER↑	
24 122.1		74 INT	
25 -		75 ST0 08	
26 RCL 05		76 -	
27 /		77 1 E4	
28 INT		78 *	
29 ST0 09		79 ST0 09	
30 RCL 05		80 RCL 07	
31 *		81 1	
32 INT		82 +	
33 RCL IND		83 ENTER↑	
02		84 1/X	
34 -		85 .7	
35 CHS		86 +	
36 ST0 00		87 CHS	
37 RCL 06		88 XEQ 22	
38 /		89 RCL 06	
39 INT		90 *	
40 ST0 07		91 INT	
41 RCL 00	Calculate day of month.	92 RCL 09	
42 X<>Y		93 RCL 05	
43 RCL 06		94 *	
44 +		95 INT	
45 INT		96 +	
46 -		97 RCL 08	
47 ST0 08		98 +	
48 RCL 07		99 X<> IND	
49 1		02	
50 RCL 08		100 FS?C 06	
51 %		101 RTN	
		102*LBL 25	

R00 = Scratch  
R01 =  $\Delta$ days  
R02 = Pointer  
R03 = Day #1  
R04 = Day #2

R05 = 365.25  
R06 = 30.600  
R07 = m  
R08 = d  
R09 = y

103 ENTER↑		153*LBL 15	
104 XEQ IND		154 "SUNDAY"	
X		155 RTN	
105 FRC		156*LBL 16	
106 1 E2		157 "MONDAY"	
107 *		158 RTN	
108 CF 28		159*LBL 17	
109 FIX 4		160 "TUESDAY"	
110 ARCL X			
111 RDN		161 RTN	
112 AVIEW		162*LBL 18	
113 SF 28		163 "WEDNESDAY"	
114 RTN		164 RTN	
115*LBL 22		165*LBL 19	
116 INT		166 "THURSDAY"	
117 ST+ 09		Y"	
118 12		167 RTN	
119 *		168*LBL 01	
120 -		169 "JAN "	
121 RTN		170 RTN	
122*LBL C		171*LBL 02	
123 CF 29		172 "FEB "	
124 FIX 0		173 RTN	
125 ST0 01		174*LBL 03	
126 FS?C 22		175 "MAR "	
127 RTN		176 RTN	
128 RCL 04		177*LBL 04	
129 RCL 03		178 "APR "	
130 -		179 RTN	
131 ST0 01		180*LBL 05	
132 RTN		181 "MAY "	
133*LBL E		182 RTN	
134 SF 06	Compute day of week.	183*LBL 06	
135 SF 22		184 "JUN "	
136 RCL 05		185 RTN	
137 5		186*LBL 07	
138 XEQ 20		187 "JUL "	
139 RCL IND		188 RTN	
02		189*LBL 08	
140 7		190 "AUG "	
141 MOD		191 RTN	
142 13		192*LBL 09	
143 +		193 "SEP "	
144 XEQ IND		194 RTN	
X		195*LBL 10	
145 AVIEW		196 "OCT "	
146 RTN		197 RTN	
147*LBL 13		198*LBL 11	
148 "FRIDAY"		199 "NOV "	
149 RTN		200 RTN	
150*LBL 14		201*LBL 12	
151 "SATURDAY"		202 "DEC "	
Y"			
152 RTN			

Important Status  
Size = 010  
Fix 4  
Flags used  
F06  
F22  
F28  
F29



## WORD GUESSING GAME

This program is a version of the word game "hangman." The first player makes up a six-character word and gives it to the calculator. The second player guesses various letters until he has completed the word. After each guess, the calculator displays all correctly guessed characters in their appropriate places. When the entire word has been guessed, the number of guesses is displayed.

SIZE: 019			
STEP	INSTRUCTIONS	INPUT	FUNCTION
1	Set status and key in the program.		
2	Begin running the program		XEQ WORDS
3	First player: Key in your word	any of six characters	R/S
4	Second player: Guess a character	any character	R/S
5	Repeat step 4 to guess more characters. When word is complete, you will see DONE, WORD IS <word>, and YOU TOOK nn GUESSES.		

## Example:

Hide "HP-41C" and then guess it.

## Keystrokes:

XEQ ALPHA WORDS ALPHA  
HP-41C R/S

A R/S

P R/S

C R/S

H R/S

4 R/S

## Display:

KEY IN WORD  
LETTER?

LETTER?  
P  
LETTER?  
P C  
LETTER?  
HP C  
LETTER?  
HP 4 C  
LETTER?

(Notice that the program stops in ALPHA mode.)

1 R/S

- R/S

HP 41C  
LETTER?  
DONE  
WORD IS <HP-41C>  
YOU TOOK 7 GUESSES

## Programming Highlight

Two special routines were used while developing this program: SPEL and DESPEL. Their function was to build up a word from a collection of letters and to take apart a word into its component letters. Only DESPEL remains in the final program because the job performed by SPEL was already done by the letter-comparison portion of the program.

A code must be passed through the x-register to SPEL and DESPEL. This code tells SPEL where to find its letters, DESPEL, where to put its letters. The code is of the form

*fl.0ll* for SPEL or *ll.0ff* for DESPEL

where

*fl* = register for first letter

*ll* = register for last letter

*ff* = *fl* - 1

SPEL and DESPEL or other similar routines may be used to encode and decode many types of strings. A similar routine was used in the hexadecimal conversion program (page 28).

01+LBL "SPE	Assumes a cleared ALPHA register.	01+LBL "DES	Store the counter
02 STO 07		02 STO 07	<i>ll.0ff</i> .
03+LBL 08	Store the counter <i>fl.0ll</i> .	03 ASTO 00	Save the word.
04 ARCL IND		04+LBL 07	
07	Build the word.	05 " "	Save all but the
05 ISG 07	If not last letter,	06 ARCL 00	last letter.
06 GT0 08	then repeat loop.	07 ASTO 00	
07 RTN		08 ASHF	Save the last
		09 ASTO IND	letter.
		10 DSE 07	If not all letters,
		11 GT0 07	then repeat
		12 RTN	loop.

<pre> 01 *LBL "WORD" 02 "KEY IN" 03 AON 04 PROMPT 05 ASTO 08 06 6 07 XEQ "DES" 08 .9 09 STO 17 10 " " 11 ASTO 09 12 16.01 13 XEQ "DES" 14 *LBL "LTT" 15 CLA 16 ASTO 09 17 "LETTER?" 18 AON 19 PROMPT 20 ASTO 10 21 ISG 17 22 1.006 23 STO 18 24 *LBL 06 25 " " 26 ASTO Y 27 RCL 18 28 10 29 + 30 CLA 31 ARCL IND 32 RDN 33 ASTO X 34 X=Y? 35 GTO 00 36 CLA 37 ARCL 10 38 ASTO Y 39 CLA 40 ARCL IND 41 ASTO X 42 X=Y? </pre>	<p>Store secret word. Place letters in R01 to to R06</p> <p>Place blanks in R11 to R16.</p> <p>Ask player for letter.</p> <p>Save letter. Count # letters. Initialize counter. Begin loop 6.</p> <p>If position already has letter, then display it.</p> <p>If guess is correct</p>	<pre> 43 GTO 00 44 " " 45 ASTO X 46 *LBL 00 47 CLA 48 ARCL 09 49 ARCL X 50 ASTO 09 51 AVIEW 52 10 53 RCL 18 54 + 55 CLA 56 ARCL Y 57 ASTO IND 58 ISG 18 59 GTO 06 60 CLA 61 ARCL 08 62 ASTO Y 63 CLA 64 ARCL 09 65 ASTO X 66 X=Y? 67 GTO 00 68 PSE 69 PSE 70 GTO "LTT" 71 *LBL 00 72 "DONE" 73 AVIEW 74 "WORD IS" 75 ARCL 09 76 "F&gt;" 77 AVIEW 78 PSE 79 PSE 80 RCL 17 81 INT 82 "YOU TOO" 83 ARCL X 84 "F GUESS" 85 AVIEW 86 RTN 87 *LBL "DES" 88 PEL" </pre> <p>Then display i. Else display blank.</p> <p>Add a letter to the display.</p> <p>Repeat loop six times.</p> <p>If words are same, then done. Else ask for another guess.</p> <p>Display word.</p> <p>Display #guesses.</p>
<p>R00 = Temporary R01 = 1<sup>st</sup> letter, SW R02 = 2<sup>nd</sup> letter, SW R03 = 3<sup>rd</sup> letter, SW R04 = 4<sup>th</sup> letter, SW R05 = 5<sup>th</sup> letter, SW R06 = 6<sup>th</sup> letter, SW</p> <p>R07 = Counter R08 = Secret word, (SW) R09 = Player's word, (PW) R10 = Current letter R11 = 1<sup>st</sup> letter, PW R12 = 2<sup>nd</sup> letter, PW R13 = 3<sup>rd</sup> letter, PW</p>		

<pre> 88 STO 07 89 ASTO 00 90 *LBL 07 91 " " 92 ARCL 00 93 ASTO 00 94 ASHF 95 ASTO IND 96 DSE 07 97 GTO 07 98 RTN </pre> <p>Important Status Size = 019 Fix 0 CF 29</p> <p>Flags used F29 Clear to suppress decimal point</p>	<p>Subroutine to separate a word into its letters.</p>		
<p>R14 = 4<sup>th</sup> letter, PW R15 = 5<sup>th</sup> letter, PW R16 = 6<sup>th</sup> letter, PW R17 = Counter R18 = Counter</p>			



## ARITHMETIC TEACHER

This program generates arithmetic practice problems. You may choose the maximum values of the numbers used and whether the problems are addition, subtraction, multiplication or division. After 10 problems have been worked, a percentage score is displayed.

The program can be started by **XEQ ALPHA TEACH ALPHA**. The calculator prompts for the largest number to use in the problems. After keying in the maximum number and pressing **R/S**, you will see a display of “+, -, \*, /?” with the ALPHA annunciator turned on. Simply press the gold shift key, one of the arithmetic functions, and **R/S** to begin the exercise. ALPHA mode will be turned off automatically.

After each problem is presented, key in your answer and press **R/S**. A correct answer is rewarded with **YES** and a new problem is presented. An incorrect answer elicits an unpleasant sound and the message **NO**, and you are given a second chance. The machine tells you the answer if you make two mistakes on the same problem, then it continues with a new one. If all 10 were worked correctly the first time, a fanfare is played. The program then begins again with the “+, -, \*, /?” question.

The series of problems is determined by a seed (number) between 0 and 1 that is in the X-register when you begin the program. If you want to repeat a particular series of problems, key in the same seed each time. If no seed is keyed in, the program simply uses the number already in the X-register.

**Reference:** Knuth, *The Art of Computer Programming*, Addison Wesley, Reading, Mass., 1978.

				SIZE: 010
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program			
2	Input a seed ( $0 \leq \text{seed} < 1$ ) and begin program.	seed	<b>XEQ TEACH</b>	MAX NUMBER?
3	Input the largest number to use	N	<b>R/S</b>	+, -, *, /?
4	Select addition subtraction multiplication division	+ - * /	<b>R/S</b> <b>R/S</b> <b>R/S</b> <b>R/S</b>	equation callouts ( $n_1$ ) + ( $n_2$ ) = ? ( $n_1$ ) - ( $n_2$ ) = ? ( $n_1$ ) * ( $n_2$ ) = ? ( $n_1$ ) / ( $n_2$ ) = ?
5	Key in your answer.	answer	<b>R/S</b>	YES or NO
6	After 10 problems have been worked, your score is displayed and you may continue at step 4.			(SCORE)% RIGHT

### Example:

Using a seed of .021946, do some subtraction problems with arguments up to 14.

#### Keystrokes:

```
.021946
XEQ ALPHA TEACH ALPHA
14 R/S
- R/S
7 R/S

1 R/S

8 R/S
7 R/S

3 R/S

6 R/S
8 R/S

11 R/S

1 R/S

4 R/S

3 R/S

4 R/S
```

#### Display:

##### MAX NUMBER?

```
+, -, *, /?
12-5=?
YES
14-13=?
YES
13-6=?
NO 13-6=?
YES
14-11=?
YES
14-7=?
NO 14-7=?
NO 14-7=7
13-2=?
YES
14-13=?
YES
14-10=?
YES
12-9=?
YES
14-10=?
YES
90% RIGHT
+, -, *, /?
```

#### Programming Highlight

This program uses a combination of the HP-41C's alpha capabilities: indirect subroutine calls together with output labels consisting of user-supplied alpha characters.

At one point in the program, you are asked to key in a +, -, \*, or / symbol depending on which type of problem you wish to work. The program stores this symbol in register 06, generates two numbers, and then executes the subroutine whose name was stored in R<sub>06</sub>. That same symbol is then recalled to help create the display showing the problem you must work.

Another interesting portion of this program is the random number generator:

$$r_{n+1} = \text{FRC}(9821 \times r_n + .211327)$$

This generator was developed by Don Malm as part of an HP-65 Users' Library program. It passes the spectral test (Knuth, V.2, § 3.4) and, because its parameters satisfy Theorem A (op. cit., p. 15), it generates one million distinct random numbers between 0 and 1 regardless of the value selected for  $r_0$ .

Because the basic random number generator delivers numbers between 0 and 1, it is necessary to do further manipulation of the random numbers to get the integers required for the arithmetic problems. By multiplying the random numbers by an integer N, then taking the integer part, numbers from 0 to N-1 may be generated. This program uses your maximum desired number plus 1 to generate numbers from 0 to your desired maximum.

01*LBL "TEA CH"		42 FS?C 00	If 2nd time, get new problem else
02 CF 29	Initialize.	43 GT0 00	
03 FIX 0		44 SF 00	
04 STO 00		45 1	
05*LBL A	Ask for max number.	46 ST+ 09	count wrong answer and repeat problem
06 "MAX NUM BER?"		47 GT0 "TRY	
07 PROMPT		48*LBL 00	
08 1		49 ARCL 05	Display correct answer.
09 +		50 ARCL 06	
10 STO 04		51 ARCL 02	
11*LBL "AGN	Label to start over.	52 "I="	
"		53 ARCL 03	
12 0		54 AVIEW	
13 STO 08		55 GT0 00	
14 STO 09		56*LBL "YES	
15 10			
16 STO 07		57 CF 00	Display "YES".
17 "+, -, *	Ask which operation.	58 "YES"	
18 AON		59 AVIEW	Count right answer.
19 PROMPT		60 1	
20 AOFF		61 ST+ 08	
21 ASTO 06		62*LBL 00	If not all problems, then repeat loop.
22*LBL 09	Begin loop.	63 DSE 07	
23 XEQ "RND		64 GT0 09	
M"	Generate operands.	65 RCL 09	
24 STO 02		66 X=0?	If no wrong answers, then play tune.
25 XEQ "RND		67 XEQ "FF"	
M"		68 RCL 08	
26 STO 05		69 .1	
27 RCL 02		70 /	
28 XEQ IND	Generate problem.	71 CLA	
06		72 ARCL X	
29*LBL "TRY		73 "F% RIGH	Display %RIGHT.
"		T"	
30 ARCL 05		74 AVIEW	
31 ARCL 06		75 PSE	
32 ARCL 02		76 PSE	Start over.
33 "I=?"	Pose problem.	77 GT0 "AGN	
34 PROMPT			
35 RCL 03		78*LBL "+"	Make + problem.
36 X=Y?		79 +	
37 GT0 "YES	If correct, then "YES".	80 STO 03	
"		81 LASTX	
38 "NO "		82 -	
39 AVIEW		83 LASTX	
40 TONE 2		84 CLA	
41 TONE 2		85 RTN	
		86*LBL "--"	Make - problem.
		87 -	
<div> R00 = random number  R01 = not used  R02 = n2  R03 = answer  R04 = 1 + max number </div> <div> R05 = n1  R06 = kind of problem  R07 = counter  R08 = # right  R09 = # wrong </div>			



88 X<=0? 89 XEQ 00 90 STO 03 91 LASTX 92 + 93 LASTX 94 CLA 95 RTN 96 LBL 00 97 CHS 98 RCL 02 99 X<> 05 100 X<> 02 101 RDN 102 RTN 103 LBL "*"	Make * problem.	137 TONE 8 138 TONE 8 139 TONE 7 140 TONE 8 141 TONE 8 142 TONE 7 143 TONE 8 144 TONE 9 145 XEQ "0" 146 XEQ "0" 147 TONE 9 148 TONE 8 149 XEQ "0" 150 TONE 8 151 TONE 7 152 XEQ "0" 153 TONE 7 154 TONE 6 155 RTN 156 LBL "0"	Subroutine to use up time.
104 * 105 STO 03 106 LASTX 107 / 108 LASTX 109 CLA 110 RTN 111 LBL "/"	Make / problem.	157 X<>Y 158 X<>Y 159 X<>Y 160 X<>Y 161 X<>Y 162 X<>Y 163 RTN	
112 X<>Y 113 STO 03 114 * 115 STO 05 116 CLA 117 RTN 118 LBL "RND M"	Random number generator	Important status: Size = 010 Fix 0 CF 29	
119 RCL 00 120 9821 121 * 122 .211327 123 + 124 FRC 125 STO 00 126 SORT 127 RCL 04 128 * 129 INT 130 RTN 131 LBL "FF"	Skew and scale the numbers.	Flags used F00 set if wrong answer F 29 clear for no radix point	
132 TONE 8 133 TONE 9 134 XEQ "0" 135 XEQ "0" 136 TONE 8	Play a tune.		

## HEXADECIMAL-DECIMAL CONVERSION

This program converts numbers between the hexadecimal and decimal number systems. Decimal integers up to 1048575 and hexadecimal integers up to FFFFF can be converted by this program.

SIZE: 021				
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status, key in the program and select USER mode.			
2	Initialize		<b>A</b>	READY
3	To convert a decimal number to hexadecimal key in the number	D	<b>E</b>	H
4	To convert a hexadecimal number to decimal key in the number in ALPHA mode	H	<b>E</b>	D
5	To convert the number back, just press E again		<b>E</b>	H or D

NOTE: D represents an integer less than 1048576<sub>10</sub>  
H represents an integer less than 1000000<sub>16</sub>

### Example 1:

Convert 123<sub>10</sub> to a hexadecimal number

#### Keystrokes

**A**  
123 **E**

#### Display

READY  
7 B

#### Comments

Initialize program

### Example 2:

Convert 123<sub>16</sub> to a decimal number

#### Keystrokes

123 **E**

#### Display

291.

### Programming Highlight

This program uses the digit-entry and alpha-entry flags, flags 22 and 23, to decide whether your number is in base 10 (decimal) or 16(hexadecimal). The first line of the program checks flag 22 to see if digits were input. If so, flag 23 is cleared so that the program can continue with step 6. If flag 22 is not set, flag 23 is tested, causing a branch to LBL04 if alpha data was keyed in. At the end of the program these flags are adjusted so that reconversion can be automatic.

01 *LBL E		50 X=Y?	If character is null, then repeat loop 5.
02 FS?C 22		51 GTO 05	
03 CF 23		52 *LBL 06	
04 FS? 23		53 RCL IND	
05 GTO 04		18	
06 STO 19		54 X=Y?	Build coded hex #.
07 XEQ 08		55 GTO 07	
08 +		56 RDN	
09 *LBL 01		57 ISG 18	
10 LASTX		58 *LBL 00	
11 ISG 16		59 GTO 06	
12 *LBL 00		60 *LBL 07	
13 1 E2		61 RCL 18	
14 /		62 RCL 17	
15 INT		63 INT	
16 X*0?		64 101X	
17 GTO 01		65 *	
18 CLA		66 ST+ 19	Count up to 5 hex characters.
19 LASTX		67 ISG 17	
20 *LBL 03		68 GTO 05	
21 1 E2		69 *LBL 08	
22 *		70 16	
23 ARCL IND		71 STO 18	
24 FRC		72 1	
25 DSE 16		73 STO 17	
26 GTO 03		74 0	
27 SF 23		75 STO 16	
28 ASTO X		76 1 E2	
29 BEEP		77 STO 20	
30 RTN		78 FS? 23	
31 *LBL 04		79 GTO 09	
32 ASTO 16		80 RCL 18	
33 .00802		81 X<> 20	
34 STO 17		82 STO 18	
35 0		83 *LBL 09	
36 STO 19		84 RCL 19	
37 *LBL 05		85 *LBL 10	
38 0		86 RCL 20	
39 STO 18		87 /	
40 "		88 STO 19	
41 ASTO Y		89 FRC	
42 ARCL 16		90 RCL 20	
43 ASTO 16		91 *	
44 ASHF		92 RCL 17	
45 ASTO X		93 *	
46 X=Y?		94 ST+ 16	
47 GTO 08		95 RCL 18	
48 CLA		96 ST+ 17	
49 ASTO Y		97 RCL 19	
		98 INT	
		99 X*0?	If not done,

R00 = "0"	R06 = "6"
R01 = "1"	R07 = "7"
R02 = "2"	R08 = "8"
R03 = "3"	R09 = "9"
R04 = "4"	R10 = "A"
R05 = "5"	R11 = "B"

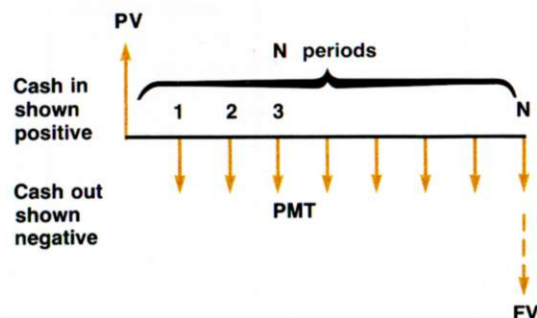


<pre> 100 GTO 10 101 X&lt;&gt; 16 102 CLA 103 FS?C 23 104 BEEP 105 RTN 106 LBL A 107 CF 22 108 CF 23 109 "0" 110 ASTO 00 111 "1" 112 ASTO 01 113 "2" 114 ASTO 02 115 "3" 116 ASTO 03 117 "4" 118 ASTO 04 119 "5" 120 ASTO 05 121 "6" 122 ASTO 06 123 "7" 124 ASTO 07 125 "8" 126 ASTO 08 127 "9" 128 ASTO 09 129 "A" 130 ASTO 10 131 "B" 132 ASTO 11 133 "C" 134 ASTO 12 135 "D" 136 ASTO 13 137 "E" 138 ASTO 14 139 "F" 140 ASTO 15 141 "READY" 142 ASTO X </pre>	<p>then repeat loop 10.</p> <p>Initialization routine.</p>		
<p>Important status:</p> <p>Size =021</p> <p>Fix 0</p> <p>Flags used</p> <p>F22 Digit entry</p> <p>F23 Alpha entry</p> <p>R12 = "C"</p> <p>R13 = "D"</p> <p>R14 = "E"</p> <p>R15 = "F"</p> <p>R16 = alpha</p> <p>R17 = loop counter, digit counter</p> <p>R18 = base constant, loop counter</p> <p>R19 = decimal-coded number built here</p> <p>R20 = base constant</p>			

Notes

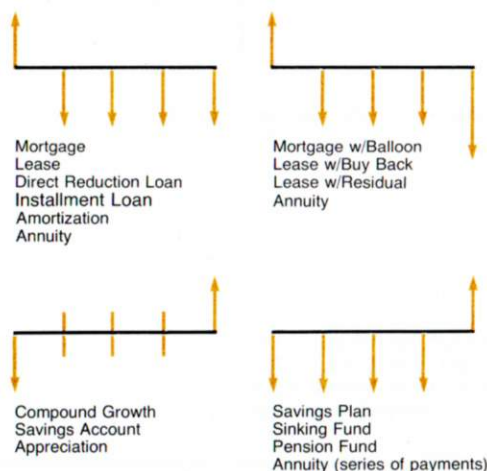
## FINANCIAL CALCULATIONS

This program converts your HP-41C into a powerful financial calculator. It has the ability to solve for any of the unknowns relating to a cash flow situation as shown below.



- PV** = Present Value: the amount loaned, borrowed, invested, etc.  
**I** = Periodic Interest rate.  
**N** = Number of periods.  
**PMT** = Payment amount: the amount paid on a loan or earned on an investment.  
**FV** = Future Value: the amount remaining, accumulated, saved, etc.

The sketch above shows a standard loan amortization cash flow from the borrower's point of view. From the lender's point of view, PV would be shown negative and the PMT stream would be positive. By changing the signs of PV, PMT, and FV, different cash flow situations may be realized. Cash flow diagrams for the four basic compound interest problems are presented below along with some of the more common terminology.



The five top-row keys (**A** through **E**) are used to enter or calculate these financial parameters. If you key in any three parameters, pressing one of the other two keys calculates the corresponding value; if you key in any four parameters, pressing the remaining key calculates its corresponding value. Previously input values can be recalled by pressing **RCL** followed by the appropriate key. The key sequence **ON** **A** may be used to clear all the registers used by this program. When the registers have been cleared in this manner, the message **N, I, PV, PMT, FV** is put into the display to remind you of the functions of the keys.

### Reference:

More information regarding cash-flow analysis may be found in Grant, E.L. and Ireson, W.G., *Principles of Engineering Economy*, Fourth Edition, The Ronald Press Company, New York, 1964.

SIZE: 010				
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in the program, check status, then place the calculator in USER mode.			
2	To clear the finance registers		<b>ON</b> <b>A</b>	N, I, PV, PMT, FV
3	Store inputs as desired number of periods periodic interest rate, percent present value of investment periodic payment future value of investment	N I PV* PMT* FV*	<b>A</b> <b>B</b> <b>C</b> <b>D</b> <b>E</b>	N I PV PMT FV
4	Compute desired output number of periods periodic interest rate present value of investment periodic payment future value of investment		<b>A</b> <b>B</b> <b>C</b> <b>D</b> <b>E</b>	N = (N) I = (I)% PV = \$(PV)* PMT = \$(PMT)* FV = \$(FV)*
5	You may return to step 4 to re-compute any of the five values or you may return to step 3 to change any or all of them.			

\*Positive for cash received, negative for cash paid out.



**Example 1:**

A couple purchases a \$50,000 house, borrowing \$40,000 at 8.5% for 30 years less one month. What is their monthly payment?

**Keystrokes**

[A] 40000 [C]  
 8.5 [ENTER] 12 [+ [B]  
 30 [ENTER] 12 [x] 1 [- [A] [D]

**Display**

40,000.00  
 0.71  
 PMT = \$-307.75

**Example 2:**

The couple in example 1 sold their house 18 months later, netting \$25,000. At what interest rate would they have had to invest their original \$10,000 and \$307.75 monthly payments to obtain \$25,000?

**Keystrokes**

18 [A]  
 25000 [E]  
 10000 [CHS] [C] [B]  
 12 [x]

**Display**

25,000.00  
 I = 3.21%  
 38.51

Monthly  
 interest rate.  
 Annual rate

**Programming Tip**

This program demonstrates a technique called an "interchangeable solution." Each of the five variables in the equation can be written in terms of the remaining four. The five top-row keys are used both for storing inputs and computing outputs using the program structure outlined below.

LBL L One of the labels A-J or a-e.

STO r Store the variable in register r.

FS?C22 Test the digit-entry flag and clear it.

RTN Stop here if this data was just keyed in.

} Compute the value of the unknown.

STO r Store the computed value in register r.

} Display the new value.

RTN

This building block may be repeated as many times as necessary depending on the number of variables.

01 *LBL A		51 ABS	
02 STO 01	Store N	52 RCL 04	
03 FS?C 22	If new data,	53 RCL 01	
04 RTN	then stop,	54 *	
05 RCL 04	else calculate	55 RCL 03	
06 RCL 09	new N.	56 +	
07 /		57 ABS	
08 STO 00		58 -	
09 RCL 05		59 RCL 04	
10 -		60 RCL 01	
11 RCL 03		61 *	
12 RCL 00		62 RCL 05	
13 +		63 +	
14 /		64 ABS	
15 LN		65 RCL 03	
16 RCL 09		66 ABS	
17 LN1+X		67 -	
18 /		68 *	
19 STO 01		69 ENTER↑	
20 "N="		70 ABS	
21 ARCL X	Display new N.	71 /	
22 AVIEW		72 1 E-9	
23 RTN		73 *	
24 *LBL B		74 STO 09	
25 STO 02	Store I and some	75 *LBL 06	Begin loop.
26 1 E2	functions of I.	76 XEQ 08	
27 /		77 RCL 04	
28 STO 09		78 *	
29 1		79 RCL 03	
30 +		80 +	
31 STO 07		81 RCL 05	
32 RCL 02		82 RCL 08	
33 FS?C 22		83 *	
34 RTN	If new data,	84 +	
35 RCL 04	then stop,	85 RCL 08	
36 X*0?	else	86 RCL 07	
37 GTO 01	if PMT=0,	87 /	
38 RCL 05	then compute	88 RCL 01	
39 RCL 03	new I by	89 *	
40 /	simple formula.	90 STO 06	
41 CHS		91 1	
42 RCL 01		92 RCL 08	
43 1/X		93 -	
44 Y↑X		94 RCL 09	
45 1		95 /	
46 -		96 -	
47 STO 09		97 RCL 04	
48 GTO 00		98 RCL 09	
49 *LBL 01		99 /	
50 RCL 05	Else compute new I	100 *	
	by Newton's method.	101 RCL 05	

R00 = used  
 R01 = n  
 R02 = i  
 R03 = PV  
 R04 = PMT  
 R05 = FV

R06 = used  
 R07 = 1 + i/100  
 R08 = used  
 R09 = i/100

<pre> 102 RCL 06 103 * 104 - 105 / 106 ST- 09 107 ABS 108 1 E-7 109 X&lt;=Y? 110 GTO 06 111 RCL 09 112 LBL 00 113 1 E2 114 * 115 STO 02 116 "I=" 117 ARCL X 118 "I%" 119 AVIEW 120 RTN 121 LBL C 122 STO 03 123 FS?C 22 124 RTN 125 RCL 04 126 XEQ 08 127 * 128 RCL 05 129 RCL 08 130 * 131 + 132 CHS 133 STO 03 134 "PV=\$" 135 ARCL X 136 AVIEW 137 RTN 138 LBL D 139 STO 04 140 FS?C 22 141 RTN 142 XEQ 08 143 1/X 144 RCL 03 145 RCL 05 146 RCL 08 147 * 148 + 149 * 150 CHS 151 STO 04 152 "PMT=\$" 153 ARCL X </pre>	<p>If I not small, then repeat loop.</p> <p>Display new I.</p> <p>Store PV. If new data, then stop, else compute new PV.</p> <p>Display new PV.</p> <p>Store PMT. If new value, then stop, else compute new PMT.</p> <p>Display new PMT.</p>	<pre> 154 AVIEW 155 RTN 156 LBL E 157 STO 05 158 FS?C 22 159 RTN 160 XEQ 08 161 RCL 04 162 * 163 RCL 03 164 + 165 RCL 08 166 / 167 CHS 168 STO 05 169 "FV=\$" 170 ARCL X 171 AVIEW 172 RTN 173 LBL 08 174 1 175 XEQ 09 176 RCL 01 177 CHS 178 Y+X 179 STO 08 180 - 181 RCL 09 182 / 183 RTN 184 LBL 09 185 RCL 09 186 1 187 + 188 STO 07 189 RTN 190 LBL a 191 CLX 192 STO 01 193 STO 02 194 STO 03 195 STO 04 196 STO 05 197 STO 09 198 "N, I, P V, PMT, F" 199 "FV" 200 AVIEW 201 RTN </pre>	<p>Store FV. If new data, then stop, else compute new FV.</p> <p>Subroutine to compute</p> $\left(1 + \frac{i}{100}\right)^{-n}$ $1 - \frac{\left(1 + \frac{i}{100}\right)^{-n}}{i/100}$ <p>Subroutine to compute <math>1 + i/100</math></p>
<p>Important status Size = 010 Fix 2</p> <p>Flags used F22 Digit entry</p>			



## ROOT FINDER

A root finder is used to find values of an independent variable,  $x$ , which cause some function  $f(x)$  of that variable to be equal to zero. These values are called the zeros of the function  $f(x)$ , or the roots of the equation  $f(x) = 0$ . For example, in the equation

$$f(x) = 2x - 6$$

$x = 3$  is a root, because

$$f(3) = 2 \times 3 - 6 = 0$$

There are many techniques that can be employed to locate the roots of an equation. Usually root-finding algorithms (procedures) begin with an initial guess and then iterate, making better and better guesses until an acceptable solution is reached. Some algorithms fail to yield an answer (converge), iterating forever. Others, even though guaranteed to converge, require a long time.

The algorithm implemented in this program will always find a root when given initial guesses straddling an odd number of roots. If the guesses do not straddle a root properly, new ones must be chosen. Thus, the price of rapid, guaranteed convergence is that you must know certain information about your function before using this program.

Before running the root finder, it is necessary to program the function whose zeros you wish to find. This is done by pressing **GTO**  $\cdot \cdot$  and keying in your program. The sequence **XEQ** **ROOT** then begins the root finding program. It requests you to key in the name you used for your function and then prompts for the two initial guesses. If both guesses yield function values on the same side of the  $x$ -axis, the message "**F1\*F2>0**" appears briefly, and you will be prompted for new guesses.

The program needs registers 01 through 07 for its own use, so register 00 and as many as are available above register 07 may be used when evaluating your function. The answer is labeled and displayed when the value of the function is less than  $10^{-10}$ . A closer tolerance can be obtained simply by keying in a different value when the program is entered.

**References:** The Illinois algorithm used here is described in M. Dowell & P. Jarratt, "A modified regula falsi method for computing the root of an equation", *BIT* 11 (1971), pp. 168-174.

A similar algorithm with slightly faster convergence was developed by the same two authors: M. Dowell & P. Jarratt, "The Pegasus method for computing the root of an equation," *BIT* 12 (1972), pp. 503-508.

Root Finder 39				
				SIZE: 008
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program.			
2	Key in your function, giving it a global name (i.e., not A-J, a-e, or 00-99).			
3	Begin executing this program		<b>XEQ</b> <b>ROOT</b>	FUNCTION NAME?
4	Key in the name of your function	Name	<b>R/S</b>	GUESS1=?
5	Key in the first guess	X1	<b>R/S</b>	GUESS2=?
6	Key in the second guess and either a root will appear or, the program will return to step 5	X2	<b>R/S</b>	X=(ROOT) F1*F2>0

### Example 1:

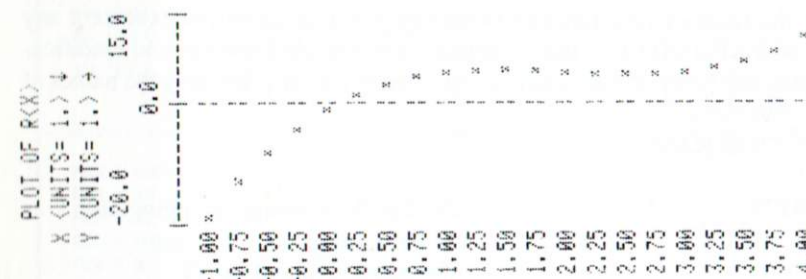
Find a value of  $x$  such that  $R(x) = x^3 - 6x^2 + 11x - 1 = 0$ . Note that a sketch of the function indicates a root between 0 and 1.

#### Keystrokes:

**GTO**  $\cdot \cdot$  **PRGM**  
**LBL** **ALPHA** **R** **ALPHA**  
**ENTER** **ENTER** **ENTER** 6 **-** **X**  
 11 **+** **X** 1 **-** **RTN**  
**PRGM**  
**XEQ** **ALPHA** **ROOT** **ALPHA**  
**R** **R/S**  
 0 **R/S**  
 1 **R/S**

#### Display:

FUNCTION NAME?  
 GUESS1=?  
 GUESS2=?  
 X = 0.0958



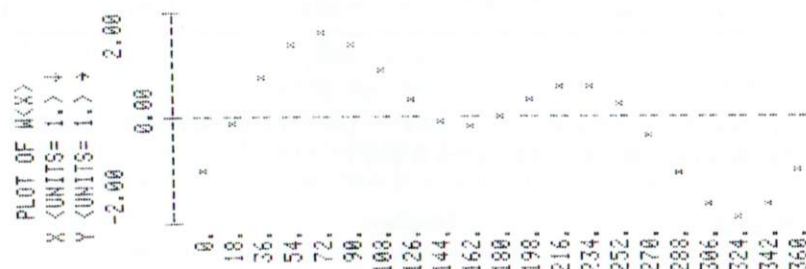
### Example 2:

Find the root of  $W(x) = \sin(x - 30) - \cos(2x + 60)$  which is between 200 and 300 degrees.



## Keystrokes:

[GTO] [•] [•] [PRGM]  
 [LBL] [ALPHA] WAVE [ALPHA]  
 30 [SIN] [RCL] 04  
 2 [X] 60 [COS] [—] [RTN]  
 [PRGM]  
 [XEQ] [ALPHA] ROOT [ALPHA]  
 WAVE [R/S]  
 200 [R/S]  
 300 [R/S]



## Programming Highlight

The root finder program asks you to key in the name of your function. It stores that name and then executes that function indirectly as needed. Note that the function AON is executed before PROMPT so that the HP-41C will stop in ALPHA mode. The function AOFF must be executed before the next PROMPT, however, or ALPHA mode will still be on. AON and AOFF are useful for controlling the mode in which the calculator stops as a further reminder of what sort of data you should provide.

With the name of your function in register 3, the program can execute it any time with XEQ IND 03. Thus, a program which might have required modification for each function you could have wished to use, requires only the names of those functions.

FUNCTION NAME?

AON

PROMPT

ASTO 03

.

.

.

AOFF

.

.

XEQ IND 03

## Display:

FUNCTION NAME?  
 GUESS1=?  
 GUESS2=?  
 X = 260.0000

Display the message, stopping with  
 ALPHA mode on.  
 The name is stored in R3.

Turn off ALPHA.

Execute the program whose name is in R3.

<pre> 01+LBL "ROOT T" 02 "FUNCTIO N NAME?" 03 AON 04 PROMPT 05 AOFF 06 ASTO 03 07+LBL A 08 "GUESS1= ?" 09 PROMPT 10 STO 01 11 "GUESS2= ?" 12 PROMPT 13 STO 02 14 RCL 01 15 STO 04 16 XEQ IND 03 17 STO 05 18 RCL 02 19 STO 04 20 XEQ IND 03 21 STO 06 22 RCL 05 23 * 24 X&gt;0? 25 GTO 05 26+LBL 00 27 RCL 02 28 RCL 02 29 RCL 01 30 - 31 RCL 06 32 RCL 05 33 - 34 / 35 RCL 06 36 * 37 - 38 STO 04 39 XEQ IND 03 40 STO 07 41 X=0? 42 GTO 04 43 ABS </pre>	<p>Ask user for the name of the function.</p> <p>Store guesses.</p> <p>Begin loop.</p> <p>New x.</p> <p>If f(x)=0 then done.</p>	<pre> 44 1 E-10 45 X&gt;Y? 46 GTO 04 47 RCL 07 48 RCL 06 49 * 50 X&gt;0? 51 GTO 01 52 RCL 02 53 STO 01 54 RCL 06 55 STO 05 56+LBL 02 57 RCL 04 58 STO 02 59 RCL 07 60 STO 06 61 GTO 00 62+LBL 01 63 2 64 ST/ 05 65 GTO 02 66+LBL 04 67 "X=" 68 ARCL 04 69 PROMPT 70+LBL 05 71 "F1+F2&gt;0 " 72 REVIEW 73 PSE 74 GTO A </pre> <p>Important status: Size = 008 DEG Fix 4</p>	<p>Tolerance value. If <math> f(x)  &lt; 1E - 10</math> then done.</p> <p>Select new guesses per requirements of Illinois algorithm.</p> <p>Done.</p> <p>Display answer.</p> <p>Error message.</p> <p>Return to input</p>
--	--	--	---

R00 = unused  
 R01 = X1  
 R02 = X2  
 R03 = Name  
 R04 = X  
 R05 = f(X1)  
 R06 = f(X2)  
 R07 = f(X3)



## CURVE FITTING

For a set of data points  $(x_i, y_i)$ ,  $i = 1, 2, \dots, n$ , this program can be used to fit the data to any of the following curves:

1. Straight line (linear regression):  $y = a + bx$ .
2. Exponential curve:  $y = ae^{bx}$  ( $a > 0$ ),
3. Logarithmic curve:  $y = a + b \ln x$ ,
4. Power curve:  $y = ax^b$  ( $a > 0$ ).

The regression coefficients  $a$  and  $b$  are found by solving the following equivalent system of linear equations.

$$An + B\sum X_i = \sum Y_i$$

$$A\sum X_i + B\sum X_i^2 = \sum Y_i X_i$$

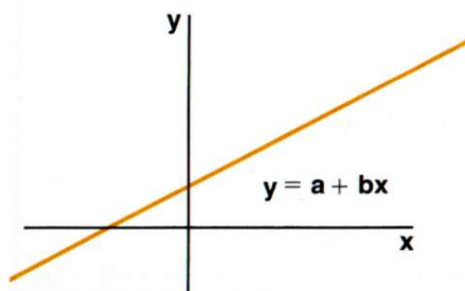
The relations of the variables are defined by the following:

Regression	A	B	$X_i$	$Y_i$
Linear	$a$	$b$	$x_i$	$y_i$
Exponential	$\ln a$	$b$	$x_i$	$\ln y_i$
Logarithmic	$a$	$b$	$\ln x_i$	$y_i$
Power	$\ln a$	$b$	$\ln x_i$	$\ln y_i$

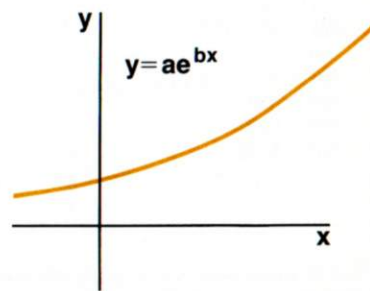
The coefficient of determination is:

$$R^2 = \frac{A\sum Y_i + b\sum X_i Y_i - \frac{1}{n} (\sum Y_i)^2}{\sum (Y_i^2) - \frac{1}{n} (\sum Y_i)^2}$$

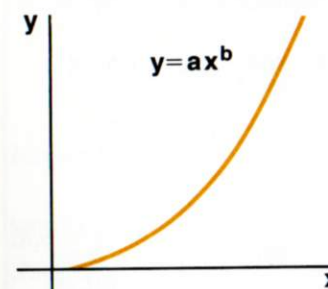
**Linear Regression**



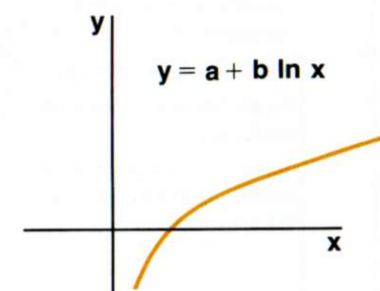
**Exponential Curve Fit**



## Power Curve Fit



## Logarithmic Curve Fit



### Remarks:

1. The program applies the least square method, either to the original equations (straight line and logarithmic curve) or to the transformed equations (exponential curve and power curve).
2. Negative and zero values of  $x_i$  will cause a calculator error for logarithmic curve fits. Negative and zero values of  $y_i$  will cause a machine error for exponential curve fits. For power curve fits both  $x_i$  and  $y_i$  must be positive, non-zero values.
3. As the differences between  $x$  and/or  $y$  values become small, the accuracy of the regression coefficients will decrease.

				SIZE: 016
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Set status and key in the program			
2	Initialize the program for STRAIGHT LINE or for EXPONENTIAL CURVE or for LOGARITHMIC CURVE or for POWER CURVE		<div style="display: flex; flex-direction: column; gap: 5px;"> <span>[XEQ] LIN</span> <span>[XEQ] EXP</span> <span>[XEQ] LOG</span> <span>[XEQ] POW</span> </div>	<div style="display: flex; flex-direction: column; gap: 5px;"> LIN EXP LOG POW </div>
3	Repeat step 3 and 4 for $i=1,2,\dots,n$ input: $x_i$ $y_i$	$x_i$ $y_i$	<div style="display: flex; flex-direction: column; gap: 5px;"> [ENTER] [A] </div>	(i)
4	If you made a mistake in inputting $x_k$ and $y_k$ , then correct by→	$x_k$ $y_k$	<div style="display: flex; flex-direction: column; gap: 5px;"> [ENTER] [C] </div>	(k-1)
5	Calculate $R^2$ and regression coefficients $a$ and $b$		<div style="display: flex; flex-direction: column; gap: 5px;"> [E] [R/S] [R/S] </div>	$R^2 = (R^2)$ $a = (a)$ $b = (b)$

STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
6	Calculate estimated y from regression, input x	x	<b>R/S</b>	$Y. = (\hat{y})$
7	Repeat step 5 for different x's			
8	Repeat step 4 if you want the results again			
9	To use the same program for another set of data, initialize the program by →		<b>■ A</b>	LIN or EXP or LOG or POW
	then go to step 3			
10	To use another program, go to step 2			

**Example 1:**

Fit a straight line to the following set of data and compute  $\hat{y}$  for  $x = 37$  and  $x = 35$ .

$x_i$	40.5	38.6	37.9	36.2	35.1	34.6
$y_i$	104.5	102	100	97.5	95.5	94

**Keystrokes:**

**XEQ** **ALPHA** **LIN** **ALPHA**  
 40.5 **ENTER** 104.5 **A**  
 38.6 **ENTER** 102 **A**  
 37.9 **ENTER** 100 **A**  
 36.2 **ENTER** 97.5 **A**  
 35.2 **ENTER** 95.5 **A**  
 35.2 **ENTER** 95.5 **C**  
 35.1 **ENTER** 95.5 **A**  
 34.6 **ENTER** 94 **A**  
**E**  
**R/S**  
**R/S**  
 37 **R/S**  
 35 **R/S**

**Display:**

**LIN**  
 1.00  
 2.00  
 3.00  
 4.00  
 5.00  
 4.00  
 5.00  
 6.00  
**R2 = 0.99**  
**a = 33.53**  
**b = 1.76**  
**Y. = 98.65**  
**Y. = 95.13**

Oops!  
 Correct error.  
 Use proper values.

**Example 2:**

Fit an exponential curve to the following set of data and compute  $\hat{y}$  for  $x = 1.5$  and  $x = 2$ .

$x_i$	.72	1.31	1.95	2.58	3.14
$y_i$	2.16	1.61	1.16	.85	0.5

**Keystrokes:**

**XEQ** **ALPHA** **EXP** **ALPHA**  
 .72 **ENTER** 2.16 **A**  
 1.31 **ENTER** 1.61 **A**  
 1.95 **ENTER** 1.16 **A**  
 2.58 **ENTER** .85 **A**  
 3.15 **ENTER** .05 **A**  
 3.15 **ENTER** .05 **C**  
 3.14 **ENTER** 0.5 **A**  
**E**  
**R/S**  
**R/S**  
 1.5 **R/S**  
 2.0 **R/S**

**Display**

**EXP**  
 1.00  
 2.00  
 3.00  
 4.00  
 5.00  
 4.00  
 5.00  
**R2 = 0.98**  
**a = 3.45**  
**b = -0.58**  
**Y. = 1.44**  
**Y. = 1.08**

If you don't  
 make a mistake  
 you can skip  
 two steps.

**Example 3:**

Fit a logarithmic curve to the following set of data and compute  $\hat{y}$  for  $x = 8$  and  $x = 14.5$ .

$x_i$	3	4	6	10	12
$y_i$	1.5	9.3	23.4	45.8	60.1

**Keystrokes:**

**XEQ** **ALPHA** **LOG** **ALPHA**  
 3 **ENTER** 1.5 **A**  
 4 **ENTER** 9.3 **A**  
 6 **ENTER** 23.4 **A**  
 10 **ENTER** 45.8 **A**  
 12 **ENTER** 60.1 **A**  
 12 **ENTER** 60.1 **C**  
 12 **ENTER** 60.1 **A**  
**E**  
**R/S**  
**R/S**  
 8 **R/S**  
 14.5 **R/S**

**Display:**

**LOG**  
 1.00  
 2.00  
 3.00  
 4.00  
 5.00  
 4.00  
 5.00  
**R2 = 0.98**  
**a = -47.02**  
**b = 41.39**  
**Y. = 39.06**  
**Y. = 63.67**

Another mistake!



## Example 4:

Fit a power curve to the following set of data and compute  $\hat{y}$  for  $x = 18$  and  $x = 23$ .

$x_i$	10	12	15	17	20	22	25	27	30	32	35
$y_i$	0.95	1.05	1.25	1.41	1.73	2.00	2.53	2.98	3.85	4.59	6.02

Keystrokes:

Display:

XEQ ALPHA POW ALPHA

10 ENTER+ 0.95 A

12 ENTER+ 1.05 A

15 ENTER+ 1.25 A

17 ENTER+ 1.41 A

20 ENTER+ 1.73 A

22 ENTER+ 2.00 A

25 ENTER+ 2.53 A

27 ENTER+ 2.98 A

30 ENTER+ 3.85 A

32 ENTER+ 4.59 A

35 ENTER+ 60.2 A

35 ENTER+ 60.2 C

35 ENTER+ 6.02 A

E

R/S

R/S

18 R/S

23 R/S

POW

1.00

2.00

3.00

4.00

5.00

6.00

7.00

8.00

9.00

10.00

11.00

10.00

11.00

R2 = 0.94

a = 0.03

b = 1.46

Y. = 1.76

Y. = 2.52

Error correction again.

## Programming Highlight

This program uses a single section of code for most of the calculations it needs to do. Since each of the four types of curve fitting requires the input data to be in a different form, it would seem that a different program should be used for each curve type. Instead, each of the set-up programs, LIN, LOG, EXP, and POW, stores a code in register 00. Then the single function on line 32, XEQ IND 00, takes care of the four different ways of processing the input data by executing the function whose label is stored in register 00.

01+LBL "LIN"		45+LBL E	
02 5		46 RCL 15	
03 "LIN"	Linear.	47 RCL 11	
04 GTO 13		48 RCL 10	Calculate A, b and a, b.
05+LBL "EXP"		49 RCL 10	
06 6		50 XEQ 09	
07 "EXP"	Exponential.	51 STO 03	
08 GTO 13		52 RCL 12	
09+LBL "LOG"		53 RCL 11	
10 7		54 RCL 10	
11 "LOG"	Logarithmic.	55 RCL 14	
12 GTO 13		56 XEQ 09	
13+LBL "POW"		57 RCL 03	
14 8		58 /	
15 "POW"	Power.	59 STO 04	
16+LBL 13		60 XEQ IND	
17 XEQ "INI"		00	
T		61 STO 06	
18 STO 00		62 RCL 15	
19 ASTO 08		63 RCL 14	
20 SREG 10		64 RCL 10	
21 CLS		65 RCL 12	
22 BEEP	Beep, display and set	66 XEQ 09	
23 AVIEW	$\Sigma$ registers.	67 RCL 03	
24 STOP		68 /	
25+LBL C		69 STO 05	
26 X<>Y		70+LBL 03	
27 XEQ IND	Correction.	71 RCL 04	
00		72 RCL 12	
28 $\Sigma^-$		73 *	
29 STOP		74 RCL 05	
30+LBL A	Input data.	75 RCL 14	
31 X<>Y		76 *	
32 XEQ IND		77 +	
00		78 RCL 12	
33 $\Sigma^+$		79 $\times 1/2$	
34 STOP		80 RCL 15	
35+LBL 07	Log.	81 /	
36 LN		82 STO 09	
37 RTN		83 -	
38+LBL 08		84 RCL 13	
39 LN	Power and exp.	85 RCL 09	
40+LBL 06		86 -	
41 X<>Y		87 /	
42 LN		88 "R2"	
43 X<>Y		89 XEQ 08	
44 RTN		90 RCL 06	
		91 "a"	
		92 XEQ 08	
		93 RCL 05	
		94 "b"	

R00 = Index  
R01 = x  
R02 = y  
R03 = det  
R04 = A

R05 = b  
R06 = a  
R07 = used  
R08 = LIN or EXP or LOG or POW  
R09 =  $(\Sigma y) 2/n$

[illegible]



## VECTOR OPERATIONS

This program enables you to add, subtract, multiply or divide two vectors. Before executing any of the routines, load the stack with the vector components as shown below.

### Initial Stack Configuration

T  $v_1$   
Z  $u_1$   
Y  $v_2$   
X  $u_2$

### Resulting Display

$U = u \quad V = v$

where the two vectors are denoted by:

$$u_1 + iv_1 \text{ and } u_2 + iv_2$$

Note that some people prefer the alternate notation of  $u + vi$ ,  $u + jv$ , or  $ui + vj$ .

				SIZE: 000
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in the program and choose a convenient display mode. You might wish to assign the routines as shown here CADD $\boxed{+}$ CSUB $\boxed{-}$ CMULT $\boxed{\times}$ CDIV $\boxed{\div}$		ASN CADD $\boxed{+}$ ASN CSUB $\boxed{-}$ ASN CMULT $\boxed{\times}$ ASN CDIV $\boxed{\div}$	
2a	Place the inputs in the operational stack Imaginary part of first vector Real part of first vector	$v_1$ $u_1$	ENTER ENTER	
2b	Imaginary part of second vector Real part of second vector	$v_2$ $u_2$	ENTER	
3	Select the desired function Vector addition Vector subtraction Vector multiplication Vector division		CADD CSUB CMULT CDIV	$U = (u), V = (v)$ $U = (u), V = (v)$ $U = (u), V = (v)$ $U = (u), V = (v)$
4	To use this answer as part of another vector calculation, it is not necessary to re-input what was just output. Simply continue with subsequent vectors at step 2b.			

### Example 1

Add  $1 + i3$  to  $4 + i6$ .

#### Keystrokes

$\boxed{\text{FIX}}$  2  
6  $\boxed{\text{ENTER}}$  4  $\boxed{\text{ENTER}}$  3  $\boxed{\text{ENTER}}$  1  
 $\boxed{\text{XEQ}}$   $\boxed{\text{ALPHA}}$  CADD  $\boxed{\text{ALPHA}}$

#### Display:

$U = 5.00, V = 9.00$

Choose a convenient display.

Set up the vectors.

### Example 2

Evaluate  $s^2 + 1$  when  $s = 3 + j2$

#### Keystrokes

2  $\boxed{\text{ENTER}}$  3  $\boxed{\text{ENTER}}$   
2  $\boxed{\text{ENTER}}$  3  $\boxed{\text{XEQ}}$   
 $\boxed{\text{ALPHA}}$  CMULT  $\boxed{\text{ALPHA}}$   
0  $\boxed{\text{ENTER}}$  1  $\boxed{\text{XEQ}}$   
 $\boxed{\text{ALPHA}}$  CADD  $\boxed{\text{ALPHA}}$

#### Display:

$U = 5.00, V = 12.00$

$U = 6.00, V = 12.00$

Add  $1 + j0$ .

### Programming Highlight

Many problems require only one number from the user, that is, you need key in only one number before executing the desired function. Vectors, however, are each described by two numbers; and two vectors must be input before the problem can be solved. Many programs can be shortened by judicious use of the stack for input data. The implementation of this program shows how short a program can become when the user is required to be careful with his input.

Notice that if the output section is replaced with LBL "UV" RTN, the four routines can be used as subroutines to any of your programs requiring vector operations. The output values  $u$  and  $v$  are returned in the X- and Y-registers respectively.

A convenient way to use this program is to assign the various routines to the  $\boxed{+}$ ,  $\boxed{-}$ ,  $\boxed{\times}$ , and  $\boxed{\div}$  keys for instant execution of the functions when in USER mode.

<pre> 01 •LBL "CSU B" 02 CHS 03 X&lt;&gt;Y 04 CHS 05 •LBL "CAD D" 06 X&lt;&gt;Y 07 RDN 08 + 09 RDN 10 + 11 R↑ 12 GTO "UV" 13 •LBL "CDI V" 14 R-P 15 1/X 16 X&lt;&gt;Y 17 CHS 18 GTO 00 19 •LBL "CMU LT" 20 R-P 21 X&lt;&gt;Y 22 •LBL 00 23 RDN 24 RDN 25 R-P 26 R↑ 27 * 28 RDN 29 + 30 R↑ 31 P-R 32 •LBL "UV" 33 "U=" 34 ARCL X 35 "F,V=" 36 ARCL Y 37 RVIEW 38 RTN </pre> <p>Important Status: Size = 000</p>	<p>Subtract.</p> <p>Change sign of second vector, then add. ADD.</p> <p>Divide.</p> <p>Invert second vector, then multiply.</p> <p>Multiply.</p> <p>Display routine.</p>		



## BLACKJACK

This program plays a simple version of the card game blackjack (twenty-one). The calculator deals (without replacement) from a 104-card deck, reshuffling when all but 13 cards have been dealt. The player may bet any amount; if he doesn't place a bet, the value of his previous one will be used.

The player and dealer each receive two cards, one of the dealer's cards being exposed. The player may then either draw additional cards (hit) or not draw (stand). The object of the game is to reach, but not exceed, a score of 21 points, counting 10 for face cards, 1 or 11 for aces, and the face value for the remaining cards. If a player's first two cards count 21, he has *blackjack* and immediately collects 1½ times his bet unless the dealer also has blackjack.

When hitting, a player who draws a card bringing his score over 21 is said to "bust" or "be busted" and he loses his bet. When the player stands on a score of 21 or less, the dealer must hit his own hand until his score exceeds 16. At that point the higher hand wins and the player's bank is updated. If the player and dealer should have the same score, the bet is a *stand-off* or a *push*.

Options allowed in casino-style blackjack such as splitting pairs, going down for double, and purchasing insurance are not included in this program.

You must have an HP-41C with one additional Memory Module to run this program.

				SIZE: 027
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Key in program, checks status, and assign DL, HT, and S as desired. A seed ( $0 \leq \text{seed} < 1$ ) may be placed on $R_{00}$ .			
2	Store your initial bank.	bank	$\boxed{\text{STO}} 21$	
3	To shuffle the deck		$\boxed{\text{XEQ}} \text{ SH}$	SHUFFLING
4	Place your bet	BET	DL	I SHOW c* YOU HAVE 1 YOU HAVE 1 2†
5a	Hit, then repeat this step or go to 5b		HT	YOU HAVE cards
5b	Stand, and the dealer will show his hand and then hit or stand as appropriate		S	I HAVE cards : : YOUR BANK IS \$ bank
6	Repeat from step 4 as desired † NOTE: If you get blackjack in step 4, the display will show BLACKJACK, and [ S (TAND) ] will be executed automatically. * c is any card, cards is a string of cards—the card numbers are linked so a 10 and a 7 will look like 107.			

### Example:

Shuffle the deck, key in a seed of  $\pi$ , and play Blackjack using a \$2 bet.

#### Keystrokes:

$\boxed{\text{ASN}} \boxed{\text{ALPHA}} \text{DL} \boxed{\text{ALPHA}} \boxed{\Sigma+}$   
 $\boxed{\text{ASN}} \boxed{\text{ALPHA}} \text{HT} \boxed{\text{ALPHA}} \boxed{1/x}$   
 $\boxed{\text{ASN}} \boxed{\text{ALPHA}} \text{S} \boxed{\text{ALPHA}} \boxed{\sqrt{x}}$   
 USER  
 $\boxed{\text{XEQ}} \boxed{\text{ALPHA}} \text{SH} \boxed{\text{ALPHA}}$   
 0  $\boxed{\text{STO}} 21$   
 $\boxed{\pi} \boxed{\text{STO}} 00$   
 2 DL

#### Display:

ASN DL 11  
 ASN HT 12  
 ASN S 13  
  
 SHUFFLING  
 104

Only FRC  
( $\pi$ ) is used.

NOTE: The DL function was assigned to  $\boxed{\Sigma+}$ . Remember, your calculator must be in user mode or you will get  $\Sigma+$ .

S

DL

HT

HT

S

I SHOW 2  
YOU HAVE 107  
I HAVE 2J  
I HAVE 2JK

BUST  
YOUR BANK IS \$2  
I SHOW 6  
YOU HAVE A5  
YOU HAVE A57  
YOU HAVE A575  
I HAVE 6K  
I HAVE 6K8  
BUST  
YOUR BANK IS \$4

NOTE: The S  
function was  
assigned to  $\sqrt{x}$

### Program Highlight

With the 11 registers left after keying in this program, you can write a program to play blackjack using simple playing and betting schemes. The routine shown checks registers and flags used by the blackjack program to determine whether to hit or stand. If the playing program loses, it doubles its bet, eventually winning. By adding still more memory modules to your HP-41C, more complicated playing strategies may be tried.

Notice that this program requires the data memory size to be increased to 28.

01•LBL "PL"		18 XEQ "HT"	
02 2	Place new bet	19 GT0 00	
03 SF 22		20•LBL 01	
04•LBL 02		21 FS? 09	If no blackjack
05 XEQ "DL"	Deal	22 XEQ "S"	Then stand
06•LBL 00		23 RCL 27	
07 RCL 24	check score	24 RCL 21	
08 12		25 ST0 27	Save last bank
09 ENTER↑	Adjustment for Ace	26 -	
10 10	If no Ace	27 X<0?	If game won,
11 FS? 07	Clear adjustment	28 GT0 "PL"	Place new bet.
12 CLX		29 X=0?	If game drawn,
13 -		30 GT0 02	Use last bet.
14 X<=Y?	If 12 ≥ score or	31 2	If game lost,
15 GT0 01	If blackjack	32 ST* 22	Double the bet.
16 FC? 09	Then stand	33 GT0 02	
17 GT0 01	Otherwise hit	34 END	

01•LBL "CRD"	Routine to get a card.	47 ARCL Y	
02 CLA		48 GT0 01	
03 AST0 19		49•LBL 00	
04 1		50 ST0 16	
05 ST0 15		51 CLX	
06 RCL 00		52 10	
07 9821	Random number generator.	53 X=Y?	
08 *		54 GT0 "10"	
09 .211327		55 1	
10 +		56 +	
11 FRC		57 X=Y?	
12 ST0 00		58 GT0 J	
13 RCL 14		59 1	
14 *		60 +	
15 INT		61 X=Y?	
16 1		62 GT0 "0"	
17 +		63 "K"	
18•LBL 02		64 GT0 01	
19 RCL IND		65•LBL A	
15		66 "A"	
20 X>Y?	If only 12 cards remain, then shuffle deck.	67 CF 07	
21 GT0 03		68 GT0 01	
22 -		69•LBL "0"	
23 ISG 15		70 "0"	
24•LBL 99		71 GT0 01	
25 GT0 02		72•LBL J	
26•LBL 03		73 "J"	
27 DSE IND		74 GT0 01	
15		75•LBL "10"	
28•LBL 99		76 "10"	
29 DSE 14		77•LBL 01	
30 12		78 AST0 19	Store card alpha.
31 RCL 14		79 RCL 16	
32 X>Y?		80 RTN	
33 GT0 04		81•LBL "SH"	Subroutine to reconstruct deck.
34 XEQ "SH"		82 "SHUFFLE"	
35•LBL 04		83 RVIEW	
36 RCL 15	Store card.	84 1.013	
37 ST0 16		85 ENTER↑	
38 10		86 8	
39 X<=Y?		87•LBL 14	
40 GT0 00		88 ST0 IND	
41 X<>Y		Y	
42 ST0 16		89 ISG Y	
43 1		90 GT0 14	
44 X=Y?		91 104	
45 GT0 A		92 ST0 14	
46 CLA		93 CLD	

R00 = Random number  
R01 = Aces  
R02 = 2's  
R03 = 3's  
R04 = 4's

R05 = 5's  
R06 = 6's  
R07 = 7's  
R08 = 8's  
R09 = 9's



94 CF 00		137 FS? 07	
95 CF 01		138 CLX	
96 CF 02		139 +	
97 CF 03		140 21	
98 CF 04		141 X*Y?	
99 RTN		142 SF 09	If no blackjack, then set
100+LBL "DL"	Blackjack. No ace.	143 FS? 09	Flag 9.
101 CF 09		144 RTN	
102 SF 07		145 21.5	
103 ABS		146 ST0 24	Blackjack.
104 INT		147 1.5	
105 FS?C 22		148 ST* 20	
106 ST0 22	Use old bet or store new	149 "BLACKJAC	Go directly to
107 RCL 22	bet.	CK"	"STAND".
108 ST0 20		150 AVIEW	
109 SF 06		151+LBL "S"	
110 CLA		152 CF 06	Player not busted. If not
111 AST0 26		153 FS? 07	blackjack, skip to 05.
112 AST0 25		154 GT0 05	
113 XEQ "CRD"	Get dealer's first card.	155 11	
"		156 RCL 24	
114 RCL 15		157 X*Y?	
115 ST0 17		158 GT0 05	
116 XEQ "CRD"	Get dealer's second	159 10	
"	card.	160 ST+ 24	
117 ST0 23		161+LBL 05	Reinstate Dealer's
118 CF 08		162 CF 07	Ace-flag.
119 FS? 07		163 FS? 08	
120 SF 08	Save dealer's A-flag.	164 SF 07	
121 CLA		165 RCL 17	
122 ARCL 19		166 ST0 15	Recover Dealer's hold
123 ARCL 25		167 XEQ 04	card.
124 AST0 25	Dealer's hand.	168 XEQ "DH"	Display Dealer's hand.
125 "I SHOW		169 FS? 07	If no dealer ace, skip
"		170 GT0 07	to LBL 07.
126 ARCL 25	Display dealer's up	171 11	
127 AVIEW	card. No ace.	172 RCL 23	
128 SF 07		173 X*Y?	
129 0		174 GT0 07	
130 ST0 24		175 21.5	
131 XEQ "CRD"	Get player's card.	176 ST0 23	
"		177 "I HAVE	
132 XEQ "PH"		BLACKJAC"	
133 XEQ "CRD"	Get player's 2nd card.	178 "HK"	
"		179 AVIEW	
134 XEQ "PH"		180 GT0 07	
135 RCL 24	Display player's hand.	181+LBL 06	
136 10			

R10 = 10's  
 R11 = J's  
 R12 = Q's  
 R13 = K's  
 R14 = # cards left in deck

R15 = counter  
 R16 = Value of current card  
 R17 = Dealer's hidden card  
 R18 = not used  
 R19 = Current card in ALPHA form

182 XEQ "CRD"	Dealer hits.	227 RCL 24	
"		228 21.5	
183 XEQ "DH"		229 X>Y?	Check for bust.
184+LBL 07	Dealer hit or stand? If	230 RTN	
185 FS? 06	player busted, then	231 "BUST"	
186 GT0 09	settle bets. If player	232 AVIEW	
187 FC? 09	blackjack set the black-	233 GT0 05	Dealer bust.
188 GT0 08	jack. If dealer's score is	234+LBL "DB"	
189 RCL 23	above 17, then settle.	235 "BUST"	
190 17	If no ace, then dealer	236 AVIEW	
191 X<=Y?	hits.	237 0	
192 GT0 08		238 RTN	
193 FS? 07		239+LBL "PH"	Display player's hand.
194 GT0 06		240 ST+ 24	
195 11		241 CLA	
196 RCL 23	If ace and score is	242 ARCL 26	
197 X>Y?	between 7 and 11, then	243 ARCL 19	
198 GT0 06	dealer hits.	244 AST0 26	
199 7		245 "YOU HAV	
200 X>Y?		E "	
201 GT0 06		246 ARCL 26	
202 10	Add 10 for ace.	247 AVIEW	
203 ST+ 23		248 RTN	
204+LBL 08		249+LBL "DH"	Display dealer's hand.
205 21.5		250 ST+ 23	
206 RCL 23	Check for dealer bust.	251 CLA	
207 X>Y?		252 ARCL 25	
208 XEQ "DB"		253 ARCL 19	
209 RCL 24		254 AST0 25	
210 -	Check for push.	255 "I HAVE	
211 X=0?		"	
212 XEQ "P"		256 ARCL 25	
213 X>0?	Set bust flag if player	257 AVIEW	
214 SF 06	loses settle bets.	258 RTN	
215+LBL 09		259+LBL "P"	Take care of push.
216 RCL 20		260 "A PUSH"	
217 FS? 06	If player loses subtract	261 AVIEW	
218 CHS	payoff.	262 ST* 20	
219 ST+ 21			
220 "YOUR BA		Important status	
NK IS \$"		Size = 028	
221 ARCL 21	Display new bank.	Fix 00	
222 AVIEW		CF 29	
223 RTN		Flag 21 Should match	
224+LBL "HT"	Player hits.	Flag 55	
225 XEQ "CRD"	Get a new card.		
"			
226 XEQ "PH"	Display new hand.		

R20 = Payoff  
 R21 = Player's bank  
 R22 =  
 R23 = Dealer's score  
 R24 = Player's score  
 R25 = Dealer's hand  
 R26 = Player's hand

Flags used  
 F00 clear  
 F01 clear  
 F02 clear  
 F03 clear  
 F04 clear  
 F06 Player busted  
 F07 Set = no Ace Clear = Ace  
 F08 Set = no dealer Ace Clear = dealer Ace  
 F09 Set = no blackjack Clear = blackjack  
 F29 Clear to suppress decimal point  
 F21 Should match the printer existence flag  
 (F55)  
 F22 Keyboard entry



1000 N.E. Circle Blvd., Corvallis, OR 97330

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