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Test Statistics



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PROGRAM DESCRIPTION

ONE SAMPLE TEST STATISTICS FOR THE MEAN

Suppose $(x_1, x_2, x_3, \dots, x_n)$ is a sample from a normal population with a known variance σ^2 and an unknown mean μ . A test of the null hypothesis

$$H_0: \mu = \mu_0$$

is based on the z statistic which has a standard normal distribution.

If the variance σ^2 is unknown then the t statistic, which has the t distribution with n-1 degrees of freedom, is used instead.

Equations:

$$z = \frac{\sqrt{n} (\bar{X} - \mu_0)}{\sigma}$$

$$t = \frac{\sqrt{n} (\bar{X} - \mu_0)}{S}$$

Where: $\bar{X}$ is the sample mean and S is the population estimate of the standard deviation.

SAMPLE PROBLEM

Suppose that the mean intelligence of the general population is 100 with a standard deviation of 15. Test the null hypothesis that the following sample of students is different from the population.

Student	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>
Score	109	115	125	113	103

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "ONESAM"	One Sample Test For The Mean	
		<u>E</u> to end input, <u>C</u> to correct	
1	Enter data as prompted	Enter datum 1?	109 [RTN]
		Enter datum 2?	115 [RTN]
		Enter datum 3?	125 [RTN]
	ERROR	Enter datum 4?	1 [RTN]
2	Call error correction	Enter datum 5?	C [RTN]
		Datum 4 deleted = 1	
1	Enter correct value	Enter datum 4?	113 [RTN]
1	Continue	Enter datum 5?	103 [RTN]
3	End data input	Enter datum 6?	E [RTN]
4	Enter general mean	Enter μ_0 ?	100 [RTN]
5	Enter general std (N-1)	Enter σ ?	15 [RTN]
6	Read output. Use [RTN] to see	z = 1.9379	[RTN]
	next output. Use [BACK] to	T = 3.5781	[RTN]
	see last output	Mean = 113	[RTN]
		St. dev. = 8.124	[RTN]
7	End program	<u>R</u> un, <u>V</u> iew, <u>E</u> nd, or <u>C</u> ontinue?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "ONESAM"	One Sample Test For The Mean	
		<u>E</u> to end input, <u>C</u> to correct	
	Do steps 1-2 N times		
1	Enter value of indicated datum	Enter datum k?	Xk [RTN]
2	If an error was made:	Enter datum k?	C [RTN]
	This will be displayed:	Datum k deleted = Xk	
	If not finished with input,		
	goto 1		
3	Indicate the end of input:	Enter datum k?	E [RTN]
4	Enter μ naught:	μ_0 ?	μ_0 [RTN]
5	Enter σ :	σ ?	σ [RTN]
6	Read output - [RTN] to see	z =	[RTN]
	next output, [BACK] to see	T =	[RTN]/[BACK]
	last result	Mean =	[RTN]/[BACK]
		St. dev =	[RTN]/[BACK]
7	Review routine	Run, View, End, or Continue?	
	R = rerun the program - step 1		R [RTN]
	V = review results - step 6		V [RTN]
	E = end the program		E [RTN]
	C = goto step number 4		C [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
A()	Data storage	K\$	General utility string
N	Sample size	S1	Sum X = ΣX
S2	Sum X-squared $\Sigma(x^2)$	M	Mean
S3	Standard deviation (n-1)	Z	Z-value
T	t-value	U	Delay flag, = 1 if [BACK]

NOTES AND REFERENCES

Notes: 1. Both t and Z are computed. The user is reminded to use z only when the population standard deviation is known.

2. This program is limited to a maximum of 300 data points. To change this limit, change the dimension statement in line 80.

References: The formula for this program came from the HP-41C Users' Library Solutions book TEST STATISTICS.

PROGRAM LISTING

```

10 ! ONESAM - One sample
20 ! test statistics for
30 ! the mean
40 ! REV 11/01/82
50 !
60 DELAY .5
70 DISP "One Sample Test for the Mean"
80 DIM A(300),K$(100)
90 DEF FNI(X) = INT(X*10000+.5)/10000
100 !
110 ! Delay routine
120 !
130 DEF FND

140 K$=KEY$ @ IF K$(<>CHR$(8) AND K$(<>CH
    R$(13) THEN 140
150 FND=K$=CHR$(8) @ END DEF
160 !
170 ! Error correction
180 !
190 DEF FNE

200 IF N<1 THEN DISP "Must have data to
    delete" @ BEEP 440 @ GOTO 230
210 DISP "Datum";N;"deleted =";A(N)
220 S2=S2-A(N)^2 @ S1=S1-A(N) @ N=N-1
230 FNE=0 @ END DEF
240 !
250 ! Initialize
260 !
270 N,S1,S2=0
280 DISP CHR$(197);" to end input, ";CH
    R$(195);" to correct" @ WAIT 1
290 !
300 ! Input loop
310 !
320 DISP "Enter datum";N+1; @ INPUT K$
330 IF UPRC$(K$)="E" AND N>1 THEN 410

340 IF UPRC$(K$)="E" THEN BEEP 220 @ DI
    SP "Must have more than 1 datum" @
    WAIT 1 @ GOTO 320
350 IF UPRC$(K$)="C" THEN U=FNE @ GOTO
    320
360 ON ERROR BEEP 220 @ DISP "Enter num
    eric, [ "E" ], or [ "C" ]" @ WAIT 1 @ G
    OTO 320
370 A(N+1)=VAL(K$) @ N=N+1 @ S1=S1+A(N)
    @ S2=S2+A(N)^2 @ GOTO 320
380 !
390 ! Enter sigma, mu0
400 !
410 ON ERROR BEEP 220 @ DISP "Please en
    ter numeric data" @ GOTO 420

```

-Define precision of output

-Wait for 'RTN' or 'BACK' key.
Return 1 if 'BACK' key

-Delete incorrect input from
the counters

-Goto end-of-data routine upon
entry of 'E'

-Display error if 'E' entered
and there is no data

-Call error correction routine
if 'C' is entered

-Error trap

-Increment counters and
continue adding data

-End-of-data routine, second
error trap

PROGRAM LISTING

```

420 DISP "Enter ";CHR$(12);"o"; @ INPUT
    U0
430 DISP "Enter ";CHR$(9); @ INPUT S
440 !
450 ! Computation
460 !
470 OFF ERROR
480 M=S1/N @ S3=SQR((S2-S1^2/N)/N*(N/(N
    -1)))
490 Z=SQR(N)*(M-U0)/S
500 T=SQR(N)*(M-U0)/S3
510 PRINT "z=";FNI(Z) @ U=FND @ IF U TH
    EN 510
520 PRINT "T=";FNI(T) @ U=FND @ IF U TH
    EN 510
530 PRINT "Mean =";FNI(M) @ U=FND @ IF
    U THEN 520
540 PRINT "St.dev. =";FNI(S3) @ U=FND @
    IF U THEN 530
550 !
560 ! Review routine
570 !
580 DISP CHR$(210);"on, ";CHR$(214);"ie
    w, ";CHR$(197);"nd, or ";CHR$(195);
    "ontinue ";
590 INPUT K$ @ K$=UPRC$(K$&" ")
600 ON POS("RVEC",K$[1,1])+1 GOTO 580,2
    70,510,610,410
610 STOP

```

-Mean and standard
 deviation(n-1)
 -Z-value and T-value
 -Display the results
 -Review module

PROGRAM DESCRIPTION

KENDALL'S COEFFICIENT OF CONCORDANCE

Kendall's Coefficient of Concordance is used to test the communality of preference among observers who have assigned n individuals ranks ranging from 1 to n according to some specified characteristic. The coefficient (W) varies from 0 (no community of preference) to 1 (perfect agreement), and is an extension of those rank-based measures used to test the degree of association in the two-variable case. This test is frequently considered a reliability measure of ranks.

$$W = \frac{12 \sum_{i=1}^n \left(\sum_{j=1}^K R_{ij} \right)^2}{(K^2)(n)(n^2-1)} - \frac{3(n+1)}{n-1}$$

$$\chi^2 = K(n-1)W$$

degrees of freedom = $n-1$

where: K is the number of observers

n is the number of individuals

R_{ij} is the rank assigned to the i th individual
by the j th observer

SAMPLE PROBLEM

"Suppose three company executives are asked to interview six job applicants and to rank them separately in their order of suitability for a job opening. The three independent sets of ranks given by executives X, Y, and Z to applicants a through f might be those shown . . . " (Siegel, NON-PARAMETRIC STATISTICS, p. 230).

Find the degree of agreement among the three executives whose rankings of six job applicants are shown below. (Artificial data).

	<u>Applicant</u>					
	<u>a</u>	<u>b</u>	<u>c</u>	<u>d</u>	<u>e</u>	<u>f</u>
Executive X	1	6	3	2	5	4
Executive Y	1	5	6	4	2	3
Executive Z	6	3	2	5	4	1
R_i (not computed)	8	14	11	11	11	8

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "KENDALL"	Kendall's Coeff. of Concordance	
2	Enter the # of executives	How many observers (K)?	3 [RTN]
	Enter the # of applicants	How many subjects (N)?	6 [RTN]
		Type <u>C</u> to delete error	
3	Enter Appl.1, Exec.1	Subject 1 Observer 1?	1 [RTN]
	Enter Appl.1, Exec.2	Subject 1 Observer 2?	1 [RTN]
	Enter Appl.1, Exec.3	Subject 1 Observer 3?	6 [RTN]
	Enter Appl.2, Exec.1	Subject 2 Observer 1?	6 [RTN]
		Subject 2 Observer 2?	5 [RTN]
		Subject 2 Observer 3?	3 [RTN]
	Enter Applicant 3	Subject 3 Observer 1?	3 [RTN]

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
		Subject 3 Observer 2?	6 [RTN]
		Subject 3 Observer 3?	2 [RTN]
	Enter Applicant 4	Subject 4 Observer 1?	2 [RTN]
		Subject 4 Observer 2?	4 [RTN]
		Subject 4 Observer 3?	5 [RTN]
	Enter Applicant 5	Subject 5 Observer 1?	5 [RTN]
		Subject 5 Observer 2?	2 [RTN]
		Subject 5 Observer 3?	4 [RTN]
	Enter Applicant 6	Subject 6 Observer 1?	4 [RTN]
	Error	Subject 6 Observer 2?	334 [RTN]
	Call correction	Subject 6 Observer 3?	C [RTN]
	Correction displayed	6,2 deleted = 334	
	Enter correct value	Subject 6 Observer 2?	3 [RTN]
	Continue	Subject 6 Observer 3?	1 [RTN]
4	Coefficient of Concordance	W = .1619	[RTN]
5	Chi-square value	Chi-square = 2.4286	[RTN]
6	Degrees of freedom	Df = 5	[RTN]
7	End program	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "KENDALL"	Kendall's Coeff. of Concordance	
2	Enter the # of observers	How many observers (K)?	k [RTN]
	Enter the # of subjects	How many subjects (n)?	n [RTN]
		Type C to delete error	
3	Enter data as prompted	Subject i Observer j?	R _{i,j} [RTN]
	If an error was made:	Subject i Observer j?	C [RTN]
	Deleted datum displayed	i,j deleted = R _{ij}	
	Goto 3 until done		
4	Real output. Use [RTN] key	W =	[RTN]
	to see next, [BACK] to see	Chi-square =	[RTN]/[BACK]
	last result.	Df =	[RTN]/[BACK]
5	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun program - step 2		R [RTN] or
	V = review results = step 4		V [RTN] or
	E = end program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
K\$	General input string	A()	Temporary data storage
S0	Grand sum of data	N	Grand N of data
S1	ΣX_{ij}	S2	$\Sigma (\Sigma X_{ij})^2$
M	Mean of data	Z	Z statistic
E	ETA η		

NOTES AND REFERENCES

Notes: The value of the Coefficient of Concordance must be in the range of zero to 1 ($0 \leq W \leq 1$). If it is not within that range, the program will display a warning message. If you get the message "W is illegal. Check data", make sure that you have entered the data by subject (see sample problem), and that the observer's ranks are in the range 1 to n (the number of subjects). Tied ranks are each assigned the average of the ranks they would have been assigned had no ties occurred (see reference to Siegel).

- References:
1. Siegel, Sidney, NONPARAMETRIC STATISTICS FOR THE BEHAVIORAL SCIENCES, (McGraw-Hill, 1956), p. 231-232.
 2. Gibbond, J.D., NONPARAMETRIC STATISTICAL INFERENCE, (McGraw-Hill, 1971).
 3. Conover, W.J., PRACTICAL NONPARAMETRIC STATISTICS (John Wiley, New York, 1971).
 4. Formulae found in HP-41C Users' Library solutions TEST STATISTICS.

PROGRAM LISTING

```

10 ! KENDALL - Kendall's
20 ! Coefficient of
30 ! Concordance
40 ! Rev 11/01/82
50 !
60 !
70 !
80 DELAY .5
90 DISP "Kendall's Coeff. of Concordan
ce"
100 DIM A(100),K$(100)
110 !
120 ! Delay routine
130 !
140 DEF FND
150 K$=KEY$ @ IF K$(<>CHR$(8) AND K$(<>CH
R$(13) THEN 150
160 FND=K$=CHR$(8) @ END DEF
170 !
180 ! Error correction
190 !
200 DEF FNE
210 IF J<2 THEN BEEP 220 @ DISP "Must h
ave data to delete" @ GOTO 240
220 DISP STR$(I);",";STR$(J-1);" delete
d =" ;A(J-1) @ WAIT 1
230 J=J-1 @ S0=S0-A(J)
240 FNE=0 @ END DEF
250 DEF FNI(X) = INT(X*10000+.5)/10000
260 !
270 ! Initialize
280 !
290 X0,X,S=0
300 INPUT "How many observers (K) ?";K
310 IF K<2 OR K>100 THEN BEEP 220 @ DIS
P "Please enter 1<k<100" @ GOTO 300
320 INPUT "How many subjects (n) ?";N
330 IF N<2 THEN BEEP 220 @ DISP "Please
enter n>1" @ GOTO 320
340 DISP "Type ";CHR$(195);" to delete
error" @ WAIT 1
350 ON ERROR BEEP 220 @ DISP 'Enter num
eric data or ["C"]' @ WAIT 1 @ GOTO
400
360 !
370 ! Data input
380 !
390 FOR I=1 TO N @ S0=0 @ FOR J=1 TO K
400 DISP "Subject";I;"Observer";J;
410 INPUT K$ @ IF UPRC$(K$)="C" THEN U=
FNE @ GOTO 400

```

-Wait for 'RTN' or 'BACK' keys.
Return 1 if 'BACK' key

-Error correction routine,
decrement counters

-Define precision of output

-Input dialogue and
initialization

-Error trap- display warning if
invalid entry

-Call correction routine if
user enters 'C'

PROGRAM LISTING

<pre> 420 A(J)=VAL(K\$) @ S0=S0+A(J) 430 NEXT J @ S=S+S0^2 @ NEXT I 440 ! 450 ! Calculate W,chi2,df 460 ! 470 W=12*S/(K^2*N*(N^2-1))-3*(N+1)/(N-1) 480 C2=K*(N-1)*W @ D=N-1 490 ! 500 ! Output routine 510 ! 520 DISP "W=";FNI(W) @ U=FND @ IF U THE N 520 530 IF W>1 OR W<0 THEN DISP W;"is illeg al. Check data." @ BEEP 440,1.5 @ U =FND 540 DISP "Chi-square=";FNI(C2) @ U=FND @ IF U THEN 520 550 DISP "Df=";D @ U=FND @ IF U THEN 54 0 560 DISP CHR\$(210);"un again, ";CHR\$(21 4);"iew again, or ";CHR\$(197);"nd"; 570 INPUT K\$ @ K\$=UPRC\$(K\$&" ") 580 ON POS("RVE",K\$[1,1])+1 GOTO 560,29 0,520,590 590 STOP </pre>	<pre> -Increment subject counter -End loop and increment total counter -Compute W -Compute chi-square -Printout routine -Display warning if W<0 or W>1 -Review routine </pre>
--	--

PROGRAM DESCRIPTION

CORRELATION COEFFICIENT TEST

Under the assumptions of rank-order correlation analysis, the t statistic, which has the t distribution with $n-2$ degrees of freedom, may be used to test the null hypothesis (the true correlation coefficient $\rho=0$).

To test the null hypothesis $\rho = \rho_0$, where ρ_0 is a given number, the z statistic is used. z has approximately the normal distribution.

Equations:

$$t = \frac{r \sqrt{n-2}}{\sqrt{1-r^2}}$$

$$z = \frac{\sqrt{n-3}}{2} \ln \left[\frac{(1+r)(1-\rho_0)}{(1-r)(1+\rho_0)} \right]$$

Where r is an estimate (based on a sample of size n) of the correlation coefficient ρ .

SAMPLE PROBLEM

Given a sample size (N) of 31, and correlation coefficient of .12, test that the null hypothesis $\rho_0 = 0$.

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "CORRTEST"	Correlation Coefficient Test	
1	Enter the sample size	Enter the sample size (n)?	31 [RTN]
2	Enter r	Correlation coefficient (r)?	.12 [RTN]
3	Enter ρ_0	Enter RHO-naught?	0 [RTN]
4	Read t	t = .650923	[RTN]
5	Read Z	Z = .638055	[RTN]
6	End program	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "CORRTEST"	Correlation Coefficient Test	
1	Enter N	Enter the sample size (n)?	N [RTN]
2	Enter r	Correlation coefficient?	r [RTN]
3	Enter ρ_0	Enter RHO-naught?	ρ_0 [RTN]
4	Read t value	t = t	[RTN]
5	Read Z value	Z = z	[RTN]/[BACK]
	Use [BACK] to review t-value		
6	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun the program - step 1		R [RTN] or
	V = review results - step 4		V [RTN] or
	E = end the program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
K\$	Input string	N	Sample size
R	Correlation	R0	P_0
T	t-score	Z	Z-score
U	Delay flag		

NOTES AND REFERENCES

- Notes:
1. This program will check that $N > 3$, $\rho \leq 31$, and $\rho_0 < 1$, and will display a warning if an error is found.
 2. Usually, the z statistic is used when the sample size is large.
 3. Note that both t and z are returned. If the test being made is that ρ is not equal to zero then use z. Choice of the appropriate statistic is left to the user.

- References:
1. Hogg and Craig, INTRODUCTION TO MATHEMATICAL STATISTICS, (Macmillan and Co., 1970).
 2. J. Freund, MATHEMATICAL STATISTICS, (Prentice-Hall, 1971).
 3. The formulae for this program come from the HP-41C Users' Library solutions TEST STATISTICS, "Test statistics for the correlation coefficient", p. 5.

PROGRAM LISTING

```

10 ! CORRTEST - Test
20 ! statistics for the
30 ! Correlation Coeff.
40 ! REV 11/01/82
50 !
60 DELAY .5
70 DISP "Correlation Coefficient Test"
80 DIM K$(100)
90 !
100 ! Delay function
110 !
120 DEF FND

130 K$=KEY$ @ IF K$(<>CHR$(8) AND K$(<>CHR$(13) THEN 130
140 FND=K$=CHR$(8) @ END DEF
150 DEF FNI(X) = INT(X*10^6+.5)/10^6
160 !
170 ! Input
180 !
190 ON ERROR BEEP 220 @ DISP "Please enter numeric data" @ WAIT 1 @ GOTO 190
200 INPUT "Enter the sample size (n) ?" ;N
210 IF N<3 THEN BEEP 220 @ DISP "Data error - n<3" @ WAIT 1 @ GOTO 200
220 INPUT "Correlation coefficient (r) ?";R
230 IF ABS(R)>=1 THEN BEEP 220 @ DISP "Impossible correlation" @ GOTO 220
240 INPUT "Enter RHO-naught ?";R0
250 IF ABS(R0)>=1 THEN DISP "Data error ";CHR$(12);"o illegal." @ GOTO 240
260 !
270 ! Computation
280 !
290 T=R*SQR(N-2)/SQR(1-R^2)
300 Z=SQR(N-3)/2*LOG(((1+R)*(1-R0)/((1-R)*(1+R0)))
310 !
320 ! Print-out
330 !
340 DISP "t=";FNI(T) @ U=FND @ IF U THEN N 340
350 DISP "Z=";FNI(Z) @ U=FND @ IF U THEN N 340
360 !
370 ! Review routine
380 !
390 DISP CHR$(210);"un again, ";CHR$(214);"iew again, or ";CHR$(197);"nd";
400 INPUT K$ @ K$=UPRC$(K$&" ")

```

-Wait for 'RTN' or 'BACK' keys-
return 1 if 'BACK' key

-Define output precision

-Error trap- display warning if
non-numeric entry

-Enter N

-Verify that N>2

-Enter correlation (r)

-Verify that the absolute value
of (r) is less than one

-Enter rho-naught

-Verify that the absolute value
of rho is less than one

-Compute the t-value

-Compute the z-value

-Print the results

-Review module

PROGRAM LISTING

```
410 ON POS("RVE",K#11,11)+1 GOTO 390,19  
    0,340,420  
420 END
```

PROGRAM DESCRIPTION

INTRACLASS CORRELATION COEFFICIENT

The intraclass correlation coefficient r_I measures the degree of association among individuals within classes or groups. The coefficient is most easily calculated using the analysis of variance techniques. r_I is the sample estimate of the population intraclass correlation coefficient ρ_I . If we can assume that the individuals within groups are random samples from normal populations with the same variance, then the hypothesis $\rho_I=0$ can be tested using the F statistic. This program also calculates the R-squared statistic, which is a measure of the relationship between the sample independent and dependent variables in the fixed effect case, and Omega-square, which is an estimate measure of the independent-dependent variable association in the population in the fixed effect case.

Mean of subjects in the i^{th} sample

$$\bar{x}_i = \frac{\sum x_i}{n_i}$$

Standard deviation $\sigma_I = \sqrt{\frac{\sum (x_i^2)}{n_i} - (\bar{x}_i)^2}$

$$SS \text{ total} = \sum \left(\frac{\sum x_j^2}{n_j} \right) - \left(\frac{\sum \sum x}{n} \right)^2$$

$$SS \text{ treatment} = \sum \left(\frac{T_i^2}{n_i} \right) - \frac{(\sum T)^2}{n} \quad T \text{ is the column sum}$$

$$SS \text{ error} = \sum \left(\frac{\sum x_j^2}{n_j} \right) - \sum \left(\frac{T_j^2}{n_j} \right)$$

$$Df \text{ total} = n-1$$

K = the number of sets

$$Df \text{ treatment} = K-1$$

n = the total n

$$Df \text{ error} = n-k$$

J = the number of subjects

PROGRAM DESCRIPTION

INTRACLAS CORRELATION COEFFICIENT (continued)

MS treatment = SS treatment/df treatment

MS error = SS error/df error

F = MS treat/MS error

R^2 = SS treat/SS total

Ω^2 = (SS treat - (MS error)(K-1)) / (SS total + MS error)

Intraclass r = $\left[\frac{SS \text{ treat}}{K-1} - \frac{SS \text{ error}}{K(J-1)} \right] / \left[\frac{SS \text{ treat}}{K-1} + \frac{SS \text{ error}}{K} \right]$

SAMPLE PROBLEM

Find the degree of association between individuals (A-B) within the following set of groups:

		Subjects	
		A	B
Groups (sets)	1	71	71
	2	69	72
	3	59	65
	4	65	64
	5	66	60
	6	73	72
	7	68	67
	8	70	68

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "INTRA"	Intraclass Correlation Coeff.	
2	Enter the N of groups	How many sets?	8 [RTN]
3	Enter the N of subjects	How many subjects?	2 [RTN]
		C to correct error	
4	Enter set 1	Set 1 Subject 1?	71 [RTN]
		Set 1 Subject 2?	71 [RTN]
	Enter set 2	Set 2 Subject 1?	69 [RTN]
		Set 2 Subject 2?	72 [RTN]
	Enter set 3	Set 3 Subject 1?	59 [RTN]
		Set 3 Subject 2?	65 [RTN]
	Set 4: ERROR	Set 4 Subject 1?	666 [RTN]

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Call correction routine	Set 4 Subject 2?	C [RTN]
	Deleted value is displayed	(4,1) DELETED = 666	
	Enter correct value	Set 4 Subject 1?	65 [RTN]
		Set 4 Subject 2?	64 [RTN]
	Enter set 5	Set 5 Subject 1?	66 [RTN]
		Set 5 Subject 2?	60 [RTN]
	Enter set 6	Set 6 Subject 1?	73 [RTN]
		Set 6 Subject 2?	72 [RTN]
	Enter set 7	Set 7 Subject 1?	68 [RTN]
		Set 7 Subject 2?	67 [RTN]
	Enter set 8	Set 8 Subject 1?	70 [RTN]
		Set 2 Subject 2?	68 [RTN]
4	Read means	Set 1 Me = 71 Std = 0	[RTN]
		Set 2 Me = 70.5 Std = 1.5	[RTN]
		Set 3 Me = 62 Std = 3	[RTN]
		Set 4 Me = 64.5 Std = .5	[RTN]
		Set 5 Me = 63 Std = 3	[RTN]
		Set 6 Me = 72.5 Std = .5	[RTN]
		Set 7 Me = 67.5 Std = .5	[RTN]
		Set 8 Me = 69 Std = 1	[RTN]
5	Read output	Total Me = 67.5 Std = 4.031	[RTN]
		Treat DF = 7 SS = 216	[RTN]
		Treat MS = 30.857	[RTN]
		Error DF = 8 SS = 260	[RTN]
		Error MS = 5.5	[RTN]

SOLUTION	
-----------------	--

STEP	INSTRUCTIONS	DISPLAY	INPUT
		Total DF = 15 SS = 260	[RTN]
	F value	F = 5.61039	[RTN]
		R squared = .830769	[RTN]
		Omega squared = .66855	[RTN]
	Degree of association	Intraclass r = .697446	[RTN]
6	End program	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "INTRA"	Intraclass Correlation Coefficient	
2	Enter the N of groups	How many sets?	k [RTN]
3	Enter the N of subjects	How many subjects?	n [RTN]
		<u>C</u> to correct error	
4	Enter indicated datum	Set i Subject j?	Xij [RTN]
	If an error was made:	Set i Subject j?	C [RTN]
	This will be displayed:	(i,j) DELETED = Xij	
	Goto 4 until done		
5	View means	Set i Me = Std =	[RTN]
6	View results. [RTN] to see	Total Me = Std =	[RTN]
	next result, [BACK] to see	Treat DF = SS =	[RTN]/[BACK]
	last result.	Treat MS =	[RTN]/[BACK]
		Error DF = SS =	[RTN]/[BACK]
		Error MS =	[RTN]/[BACK]
		Total DF = SS =	[RTN]/[BACK]
		F =	[RTN]/[BACK]
		R squared =	[RTN]/[BACK]
		Omega squared =	[RTN]/[BACK]
		Intraclass r =	[RTN]/[BACK]
7	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun program - step 2		R [RTN]
	V = review results - step 6		V [RTN]
	E = end program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
T(i)	Σx_i	X2(i)	Σx_i^2
M(i)	Mean of treatment i	I0()	t_i^2/n
S9(i)	SD of treatment i	V(i)	Variance of i
R()	Temporary storage	E1	Value of deleted data
X\$	General input string	T	Grand sum of all data
N	Grand n of all data	X2	Σx_i^2 of treatment
I0	$\Sigma(T_i^2/n)$	I1	Intraclass correlation
S1	Treatment SS	M1	Treatment MS
S2	Error SS	M2	Error MS
S3	Total SS	F	F-value
D1	Treatment df	R2	R squared
D2	Error df	O2	Omega squared
D3	Total df		

NOTES AND REFERENCES

- Notes:
1. A maximum of 100 subjects per set may be used. To change this, change the dimension statements in line 70.
 2. A maximum of 20 sets may be used. To change this, change lines 370 and 420.
 3. Once a set has been finished, it may not be corrected.

- References:
1. Winer, B.J., STATISTICAL PRINCIPLES IN EXPERIMENTAL DESIGN, (McGraw-Hill, New York, 1971) pages 210-214.
 - 2.. Hays, W.L., STATISTICS FOR PSYCHOLOGISTS, (Holt, Rinehart and Winston, 1963) page 382.
 3. Ostle, B., STATISTICS, IN RESEARCH, Iowa State University Press, 1972.
 4. HP-41C Users' Library, TEST STATISTICS, p. 33-34.
 5. HP-75 STATISTICS SOLUTIONS BOOK, One-Way Analysis of Variance

PROGRAM LISTING

```

10 ! INTRAC-Intraclass
20 ! Correlation Coeff.
30 ! Rev 11/01/82
40 !
50 DELAY .5
60 DISP "Intraclass Correlation Coeff.
  "
70 DIM I(20),X2(20),I0(20),V(20),M(20)
  ,S9(20),R(100)
80 DIM X$(20)
90 !
100 ! Define variance
110 !
120 DEF FNS(S1,S2,N) = S2/N-(S1/N)^2
130 !
140 ! Delay routine
150 !
160 DEF FND
170 A$=KEY$ @ IF A$="" THEN 170
180 FND=0 @ IF A$=CHR$(8) THEN FND=1
190 END DEF
200 !
210 ! Precision routine
220 !
230 DEF FNI(X) = INT(X*10^3+.5)/10^3
240 DEF FNJ(X) = INT(X*10^6+.5)/10^6
250 !
260 ! Correction
270 !
280 DEF FNE(C)
290 IF I=1 THEN BEEP @ DISP "Must have
  data to delete" @ WAIT 1 @ GOTO 330
300 E1=R(I-1) @ DISP "(";C;",";I-1;") D
  ELETED =" ;R(I-1) @ WAIT 1
310 T(C)=T(C)-E1 @ T=T-E1 @ I=I-1 @ N=N
  -1
320 X2=X2-E1^2 @ X2(C)=X2(C)-E1^2
330 FNE=0 @ END DEF
340 !
350 ! Initialize
360 !
370 FOR Y=1 TO 20 @ T(Y)=0 @ X2(Y)=0 @
  I0(Y)=0 @ V(Y)=0 @ M(Y)=0 @ NEXT Y
380 N,T,X2,I0=0
390 !
400 ! Enter data
410 !
420 INPUT "How many sets ?"; K @ IF K<2
  OR K>20 THEN BEEP @ GOTO 420
430 INPUT "How many subjects? "; N0 @ I
  F N0<1 THEN BEEP @ GOTO 430

```

-Routine to calculate the
variance

-Wait for 'RTN' or 'BACK' key.
Return 1 if 'BACK' key

-Define precision of output

-Error correction routine-
decrement counters

-Set counters to zero

PROGRAM LISTING

```

440 ON ERROR BEEP @ DISP "Please enter
    numeric data" @ WAIT 1 @ GOTO 470
450 DISP CHR$(195); " to correct error."
    @ BEEP 440 @ WAIT 1
460 FOR J=1 TO K @ FOR I=1 TO N0
470 DISP 'Set';J;'Subject';I; @ INPUT X
    $
480 IF X$="" THEN 470
490 IF POS("Cc",X$) THEN U=FNE(J) @ GOT
    O 470
500 X=VAL(X$)
510 !
520 ! Loop counters
530 !
540 N=N+1 @ R(I)=X
550 T(J)=T(J)+X @ T=T+X @ X2(J)=X2(J)+X
    ^2 @ X2=X2+X^2
560 NEXT I
570 NEXT J
580 OFF ERROR
590 !
600 ! CALCULATION
610 ! Me,STD,Internal
620 !
630 FOR J=1 TO K
640 I0(J)=T(J)^2/N0 @ I0=I0+I0(J)
650 V(J)=FNS(T(J),X2(J),N0) @ S9(J)=SQR
    (V(J))
660 M(J)=T(J)/N0
670 DISP "Set";J;"Me=";FNI(M(J));"Std="
    ;FNI(S9(J)) @ U=FND
680 NEXT J @ V=FNS(T,X2,N) @ M=T/N @ S9
    =SQR(V)
690 DISP "Total Me=";FNI(M);"Std=";FNI
    (S9) @ U=FND
700 !
710 ! Int,SS,MS,DF
720 !
730 I1=T^2/N
740 S1=I0-I1 @ S2=X2-I0 @ S3=X2-I1
750 D1=K-1 @ D2=N-K @ D3=N-1
760 M1=S1/D1 @ M2=S2/D2
770 !
780 ! F,R^2,D^2
790 !
800 F=M1/M2 @ R2=S1/S3 @ D2=(S1-(K-1)*M
    2)/(S3+M2)
810 I1=(S1/(K-1)-S2/(K*(N0-1)))/(S1/(K-
    1)+S2/K)
820 !
830 ! Print Out
840 !
850 DISP "Treat DF=";D1;"SS=";FNI(S1)
    @ U=FND

```

-Error trap- return warning if
illegal data is entered

-Input loop
-Call error correction

-Decrement counters

-Intermediate calculation
-Variance and SD(n)

-Mean

-Calculate sum-squares
-Calculate degrees of freedom
-Calculate mean-squares

	PROGRAM LISTING	
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```

860 DISP "Treat MS=";FNI(M1) @ U=FND @
    IF U THEN 850
870 DISP "Error DF=";D2;"SS=";FNI(S2)
    @ U=FND @ IF U THEN 860
880 DISP "Error MS=";FNI(M2) @ U=FND @
    IF U THEN 870
890 DISP "Total DF=";D3;"SS=";FNI(S3)
    @ U=FND @ IF U THEN 880
900 DISP "F=";FNJ(F) @ U=FND @ IF U THE
    N 890
910 DISP "R squared=";FNJ(R2) @ U=FND @
    IF U THEN 900
920 DISP "Omega squared=";FNJ(O2) @ U=F
    ND @ IF U THEN 910
930 DISP "Intraclass r =" ;FNJ(I1) @ U=F
    ND @ IF U THEN 920
940 DISP CHR$(210);"un again, ";CHR$(21
    4);"iew again, or ";CHR$(197);"nd";
950 INPUT X$ @ ON POS("RVE",UPRC$(X$))+
    1 GOTO 940,370,690,960
960 STOP

```

-Review module

PROGRAM DESCRIPTION

KRUSKAL-WALLIS STATISTIC

Suppose we want to test the null hypothesis that k independent random samples of sizes $n_1, n_2, \dots, n_{k-1}, n_k$ come from identical continuous populations.

This program will arrange all values from k samples jointly (as if they were one sample) in an increasing order of magnitude. Values that have equal ranks will be assigned the average of the ranks that they cover. Let R_{ij} be the rank of the j th value in the i th sample.

The Kruskal-Wallis statistic H can be used to test the null hypothesis that each observer has identical ranking preference.

When all sample sizes are large (>5), H is distributed approximately at the chi-square with $k-1$ degrees of freedom. For small samples, the test is based on special tables (not computed). This program will accept a maximum of 254 TOTAL observations, due to a restriction in the sorting routine.

Equation: $df = K-1$

$$H = \left(\frac{12}{n(n+1)} \right) \left(\sum_{i=1}^K \frac{\left(\sum_{j=1}^{n_i} R_{ij} \right)^2}{n_i} \right) - 3(N+1)$$

Where: $N = \sum_{i=1}^K n_i$

R_{ij} = Rank of observation (i, j)

K = number of samples

n_i = number of observations in the i^{th} sample

SAMPLE PROBLEM

Compute the H-statistic for the following data: (data from Conover, p. 258).

1		2		3		4	
Obs.	Rank	Obs.	Rank	Obs.	Rank	Obs.	Rank
83	11	91	23	101	34	78	2
91	23	90	19.5	100	33	82	9
94	28.5	81	6.5	91	23	81	6.5
89	17	83	11	93	27	77	1
89	17	84	13.5	96	31.5	79	3
96	31.5	83	11	95	30	81	6.5
91	23	88	15	94	28.5	80	4
92	26	91	23			81	6.5
90	19.5	89	17				
		84	13.5				

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "KRUSKA"	Kruskal-Wallis Statistic	
1	Enter the N of treatments	How many treatments?	4 [RTN]
		<u>E</u> to end treat., <u>C</u> to change	
2	Begin treatment 1	Treat. 1 Subject 1?	83 [RTN]
		Treat. 1 Subject 2?	91 [RTN]
		Treat. 1 Subject 3?	94 [RTN]
		Treat. 1 Subject 4?	89 [RTN]
		Treat. 1 Subject 5?	89 [RTN]
		Treat. 1 Subject 6?	96 [RTN]
		Treat. 1 Subject 7?	91 [RTN]
		Treat. 1 Subject 8?	92 [RTN]

	SOLUTION	
--	----------	--

STEP	INSTRUCTIONS	DISPLAY	INPUT
		Treat. 1 Subject 9?	90 [RTN]
4	End treatment 1	Treat. 1 Subject 10?	E [RTN]
2	Begin treatment 2	Treat. 2 Subject 1?	91 [RTN]
		Treat. 2 Subject 2?	90 [RTN]
		Treat. 2 Subject 3?	81 [RTN]
		Treat. 2 Subject 4?	83 [RTN]
		Treat. 2 Subject 5?	84 [RTN]
		Treat. 2 Subject 6?	83 [RTN]
		Treat. 2 Subject 7?	88 [RTN]
		Treat. 2 Subject 8?	91 [RTN]
		Treat. 2 Subject 9?	89 [RTN]
		Treat. 2 Subject 10?	84 [RTN]
4	End treatment 2	Treat. 2 Subject 11?	E [RTN]
2	Begin treatment 3	Treat. 3 Subject 1?	101 [RTN]
		Treat. 3 Subject 2?	100 [RTN]
		Treat. 3 Subject 3?	91 [RTN]
	Error	Treat. 3 Subject 4?	9333 [RTN]
3	Call correction routine	Treat. 3 Subject 5?	C [RTN]
	This will be displayed:	(3,4) DELETED = 9333	
2	Enter correct value	Treat. 3 Subject 4?	93 [RTN]
	Continue	Treat. 3 Subject 5?	96 [RTN]
		Treat. 3 Subject 6?	95 [RTN]
		Treat. 3 Subject 7?	94 [RTN]
4	End treatment 3	Treat. 3 Subject 8?	E [RTN]
2	Begin treatment 4	Treat. 4 Subject 1?	93 [RTN]

	SOLUTION	
--	----------	--

STEP	INSTRUCTIONS	DISPLAY	INPUT
		Treat. 4 Subject 2?	82 [RTN]
		Treat. 4 Subject 3?	81 [RTN]
		Treat. 4 Subject 4?	77 [RTN]
		Treat. 4 Subject 5?	79 [RTN]
		Treat. 4 Subject 6?	81 [RTN]
		Treat. 4 Subject 7?	80 [RTN]
		Treat. 4 Subject 8?	81 [RTN]
4	End treatment 4	Treat. 4 Subject 9?	E [RTN]
5	Skip the ranks	View the ranks (Y/N)?	N [RTN]
6	View printout	H = 25.46437	[RTN]
		df = 3	[RTN]
		Total n = 34	[RTN]
7	End program	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "KRUSKA"	Kruskal-Wallis Statistic	
1	Enter the number of treatments	How many treatments?	k [RTN]
		<u>E</u> to end treat., <u>C</u> to correct	
	do steps 2-5 k times		
2	Enter data as prompted	Treat. i Subject j?	X _{ij} [RTN]
3	If an error was made:	Treat. i Subject j?	C [RTN]
	Deleted datum displayed:	(i,j) DELETED = A _{ij}	
	Goto 2 until treatment done		
4	Depress E to end treatment	Treat. i Subject j	E [RTN]
	Goto 2 until all treatments		
	have been entered		
5	Depress Y to see ranks	View the ranks (Y/N)?	Y or N [RTN]
	To view the ranks:	i,j S = R =	[RTN]/[BACK]
6	Read the printout. Use	H =	[RTN]/[BACK]
	[RTN] key to see next result,	df =	[RTN]/[BACK]
	[BACK] key to see last result.	Total n =	[RTN]/[BACK]
7	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun program - step 1		R [RTN]
	V = review results - step 5		V [RTN]
	E = end program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
A()	Data storage	N	Total N
X\$	General use string	A1()	Storage of ranks
N(j)	N of column j	N1	Internal: total N
NO	Grand sum	K	Number of treatments
X	Temporary input value	H	H-value
R2	$\Sigma(R,j)^2$	R1	Temporary sum of rank
D	Degrees of freedom	U*	Delay flag, = 1 if [BACK]
VARIABLES USED IN THE INDEX SORTING ROUTINE			
L	Lower parameter of search	U*	Upper parameter of search
I	Middle of binary search	K1	Value to "search" for
T\$	Upper part of index string	B\$	Lower part of index string
A\$	Index string		
VARIABLES USED IN THE RANKING AND TIED-VALUE CORRECTION ROUTINE			
L1	Last discrete rank value	C1	Index (position) of L1
C0	Number of ranks that = L1	C2	Sum of indexes after C1
T	"Current" rank value	R	Value to replace "current" tied ranks
* Some variables used for more than one purpose			

NOTES AND REFERENCES

- Notes:
1. The program is presently limited to a maximum of 20 treatments. To change this limit, change lines 70 and 320.
 2. The program is limited to a maximum of 254 total data items. To change this would require a major reprogramming effort, and would slow down the ranking routine.

- References:
1. Conover, W.J., PRACTICAL NONPARAMETRIC STATISTICS (John Wiley and sons. 1971), p. 257-259.
 2. Knuth, Donald E., THE ART OF COMPUTER PROGRAMMING, Volume 3, Sorting and Searching, (Addison-Wesley, 1972).
 3. HP-41C Users' Library solutions, TEST STATISTICS, Kruskal-Wallis statistic.

PROGRAM LISTING

```

10 ! KRUSKAL: Kruskal-
20 ! Wallis statistic
30 ! REV 11/01/82
40 !
50 DELAY .5
60 DISP "      Kruskal-Wallis Statistic"
70 DIM A(255),A$(255),T$(255),B$(255),
   A1(255),X$(20),N(20)
80 DEF FNC(X) = NUM(A$(X,X))

90 !
100 ! Delay routine
110 !
120 DEF FND

130 A$=KEY$ @ IF A$="" THEN 130
140 FND=0 @ IF A$=CHR$(8) THEN FND=1
150 END DEF
160 !
170 ! Correction
180 !
190 DEF FNE(C)
200 IF N(C)<1 THEN BEEP @ DISP "Must ha
   ve data to delete" @ GOTO 230
210 DISP "(";C;",";N(C);") DELETED =";A
   (N) @ WAIT 1
220 N(C)=N(C)-1 @ N=N-1 @ N0=N0-A(C)
230 FNE=0 @ END DEF
240 DEF FNI(X) = INT(X*10^5+.5)/10^5
250 !
260 ! Initialize
270 !
280 N1,R1,R2,N,N0=0
290 !
300 ! Enter data
310 !
320 INPUT "How many Treatments ?"; K @
   IF K<2 OR K>20 THEN BEEP @ GOTO 320
330 DISP CHR$(197);" to end treat., ";C
   HR$(195);" to correct" @ WAIT 1
340 FOR J=1 TO K @ N(J)=0
350 DISP 'Treat.';J;'Subject';N(J)+1; @
   INPUT X$
360 IF UPRC$(X$)="E" THEN 490

370 IF UPRC$(X$)="C" THEN U=FNE(J) @ GO
   TO 350
380 ON ERROR BEEP 220 @ DISP 'Enter num
   eric, ["E"], or ["C"]' @ WAIT 1 @ G
   OTO 350
390 X=VAL(X$)
400 !
410 ! Loop counters
420 !

```

-Conversion function for
ranking routine

-Wait for 'RTN' or 'BACK' keys-
return 1 if 'BACK' key

-Correction routine

-Define precision of output

-Enter and verify the number of
treatments

-Goto the end of the treatment
if 'E' is entered

-Call error correction routine
if 'C' is entered

-Error trap

PROGRAM LISTING

```

430 N(J)=N(J)+1 @ N=N+1 @ A(N)=X @ N0=N0+X -Increment counters
440 IF N>=254 THEN BEEP @ DISP "Can't Enter any more" @ WAIT 1 @ GOTO 490 -Check number of data items
450 GOTO 350
460 !
470 ! End of treatment
480 !
490 IF N(J)<2 THEN BEEP @ DISP "Must have more than one subject" @ GOTO 350
500 NEXT J
510 OFF ERROR
520 !
530 ! Rank data by
540 ! "Binary" sort
550 !
560 L1,A(N+1),A(0)=-INF @ C0=1 @ C1,C2=0 -Binary index sort
570 A$=CHR$(1)
580 FOR X=2 TO N -Binary search
590 L=1 @ U=X-1
600 I=INT((L+U)/2)
610 K1=A(NUM(A$(I,I)))
620 IF A(X)=K1 THEN GOTO 650
630 IF A(X)<K1 THEN U=I-1 ELSE L=I+1
640 IF U>=L THEN GOTO 600
650 IF L>1 THEN B$=A$(I,I-1) ELSE B$=""
660 IF L<X-1 THEN T$=A$(I+1,LEN(A$)) ELSE T$="" -Insert present index into A$
670 IF A(X)<K1 THEN A$=B$&CHR$(X)&A$(I,LEN(A$)) ELSE A$=A$(I,I)&CHR$(X)&T$
680 NEXT X
690 A$=A$&CHR$(0)
700 !
710 ! Compute & store
720 ! ranks
730 !
740 FOR X=1 TO N -Store ranks in A()
750 T=A(FNC(X)) @ IF T<>L1 AND C0=1 THEN L1=T @ A1(FNC(X))=X @ C1,C2=X @ GOTO 800
760 IF T=L1 THEN C0=C0+1 @ C2=C2+X -Replace tied ranks
770 IF X<>N AND T=L1 THEN GOTO 800
780 R=C2/C0 @ FOR Q=C1 TO C1+C0-1 @ A1(FNC(Q))=R @ NEXT Q
790 C0=1 @ L1=T @ A1(FNC(X))=X @ C1,C2=X
800 NEXT X
810 !
820 ! Compute r2/n
830 !
840 FOR X=1 TO K
850 R1=0 @ FOR Y=1 TO N(X)

```

PROGRAM LISTING

```

860 N1=N1+1 @ R1=R1+A1(N1) @ NEXT Y
870 R2=R2+R1^2/N(X) @ NEXT X
880 D=K-1

890 H=12/(N*(N+1))*R2-3*(N+1)
900 !
910 ! Print-out
920 !
930 DISP "View the ranks? (";CHR$(217);
    "/" ;CHR$(206);")";
940 INPUT A$ @ A$=UPRC$(A$&" ")
950 IF POS("NY",A$[1,1])=0 THEN 930
960 IF A$="N " THEN 1050
970 X1,X=0 @ Y=1
980 PRINT "Sample";Y

990 X=X+1 @ X1=X1+1 @ IF X>N THEN 1050
1000 IF X1>N(Y) THEN Y=Y+1 @ X1=0 @ X=X-
    1 @ GOTO 980
1010 PRINT STR$(Y);"," ;STR$(X1);" S=" ;A(
    X);"R=" ;A1(X) @ U=FND
1020 IF U AND X1>1 THEN X=X-1 @ X1=X1-1
    @ GOTO 1010
1030 IF U AND Y>1 THEN Y=Y-1 @ X1=N(Y) @
    X=X-1 @ GOTO 1010
1040 GOTO 990
1050 PRINT "H =" ;FNI(H) @ U=FND @ IF U T
    HEN X1=N(K) @ X=N @ Y=K @ GOTO 1010
1060 PRINT "df=" ;D @ U=FND @ IF U THEN 1
    050
1070 PRINT "Total n=" ;N @ U=FND @ IF U T
    HEN 1060
1080 !
1090 ! Review routine
1100 !
1110 DISP CHR$(210);"un again, " ;CHR$(21
    4);"iew again, or " ;CHR$(197);"nd "
    ;
1120 INPUT A$ @ A$=UPRC$(A$&" ")
1130 ON POS("RVE",A$[1,1])+1 GOTO 1110,2
    80,930,1140
1140 STOP

```

-Compute H and degrees of freedom

-Routine to allow user to view the ranks

-Printout

-Review module

PROGRAM DESCRIPTION

MANN-WHITNEY U-TEST

This program calculates the Mann-Whitney test statistic on two independent samples of equal or unequal sizes. The Mann-Whitney test will test the null hypothesis that there is no difference between the two samples. The program will rank all values from both samples as if they were one sample, assigning tied ranks the mean of the positions that they occupy. This program will also accept, as input, data that has already been ranked in the preceding manner. The smaller of the two U-statistics will be displayed, as according to statistical convention. The Z-value that is displayed is approximately a random variable having the standard normal distribution.

For small samples (less than or equal to 8) the specially constructed tables should be used. For example: HANDBOOK OF STATISTICAL TABLES, D. B. Owen, Addison-Wesley, 1962.

Formula:

$$U = n_1 n_2 + \frac{n_1(n_1+1)}{2} - \sum_{i=1}^{n_1} R_i$$

$$z = \frac{U - \frac{n_1 n_2}{2}}{\sqrt{n_1 n_2 (n_1 + n_2 + 1) / 12}}$$

Where: n_1 = Size of sample 1

n_2 = Size of sample 2

R_i = Rank assigned to item i of the sample with the smallest U .

Note: Both of the two possible U's are computed.

The smallest U is displayed, as is conventional.

SAMPLE PROBLEM

The two-sample case is one in which the investigator has obtained two samples from possibly different populations. The null hypothesis tests the rejection of the assumption that the samples come from two different populations.

Consider two independent samples of students trained in a series of athletic events under two different conditions. The null hypothesis is that there are no differences between the training methods. Use the program MANN to calculate the ranks, U-statistic and z-statistic of these students.

	Score
Method A	18 15 13 21 11
Method B	13 6 2 5

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "MANN"	Mann-Whitney U-Test Statistic	
		Sample 1 C=change E=end	
1	Enter sample 1	Sample 1 Item 1?	18 [RTN]
		Sample 1 Item 2?	15 [RTN]
		Sample 1 Item 3?	13 [RTN]
		Sample 1 Item 4?	21 [RTN]
		Sample 1 Item 5?	11 [RTN]
4	End sample 1	Sample 1 Item 6?	E [RTN]
		Sample 2 C=change E=end	
2	Enter sample 2	Sample 2 Item 1?	13 [RTN]
		Sample 2 Item 2?	6 [RTN]
	ERROR	Sample 2 Item 3?	299 [RTN]
3	Call error correction	Sample 2 Item 4?	C [RTN]
	This will be displayed	Item 3 deleted = 299	

	SOLUTION	
--	----------	--

STEP	INSTRUCTIONS	DISPLAY	INPUT
2	Enter the correct value	Sample 2 Item 3?	2 [RTN]
	Continue	Sample 2 Item 4?	5 [RTN]
4	End sample 2	Sample 2 Item 5?	E [RTN]
5	View the rank scores?	View the ranks? (Y/N)?	Y [RTN]
6	View the ranks. Use [RTN]	Sample 1	
	to see the next rank.	1,1 S = 18 R = 8	[RTN]
		1,2 S = 15 R = 7	[RTN]
		1,3 S = 13 R = 5.5	[RTN]
		1,4 S = 21 R = 9	[RTN]
		1,5 S = 11 R = 4	[RTN]
		Sample 2	
		2,1 S = 13 R = 5.5	[RTN]
		2,2 S = 6 R = 3	[RTN]
		2,3 S = 2 R = 1	[RTN]
		2,4 S = 5 R = 2	[RTN]
7	View results, using [RTN] as	U = 1.5	[RTN]
	above	Z = -2.08207	[RTN]
8	End program	Run again, View again, or End?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "MANN"	Mann-Whitney U-Test Statistic	
		Sample 1 C = change, E = end	
1	Enter items of sample 1	Sample 1 Item i?	A(1,i) [RTN]
	If an error was made:	Sample 1 Item i?	C [RTN]
	This will be displayed:	Item i deleted = A(1,i)	
	Goto 1 until done		
	End sample 1	Sample 1 Item i?	E [RTN]
		Sample 2 C = change, E = end	
2	Enter items of sample 2	Sample 2 Item i?	A(2,i) [RTN]
	If an error was made:	Sample 2 Item i?	C [RTN]
	Will not correct sample 1	Item i deleted = A(2,i)	
	Goto 2 until done		
	End sample 2	Sample 2 Item i?	E [RTN]
3	Do you wish to view the	View the ranks? (Y/N)?	Y [RTN] or
	ranks? If not, goto 5		N [RTN]
4	View the ranks. Use the	Sample 1	
	[RTN] key to see the next	1,1 S = sample R = rank	[RTN]
	rank, [BACK] to see previous	1,i S = sample R = rank	[RTN]/[BACK]
	rank	Sample 2	
5	View U and Z. Use [RTN] and	U = u value	[RTN]/[BACK]
	[BACK] as above	Z = z value	[RTN]/[BACK]
6	Review routine	Run again, View again, or End?	
	R = rerun the program - step 1		R [RTN] or
	V = review results - step 3		V [RTN] or
	E = end the program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
A()	Data storage	A1()	Storage of ranks
N(j)	N of column j	N	Total N
X9	Temporary input data value	Z	Z-statistic
U1,U2	Large and small U statistic	K\$	General use string
R1,R2	Sum of ranks in var. 1,2	U*	Delay flag, = 1 if [BACK]
D	Degrees of freedom		used
VARIABLES USED IN THE INDEX SORTING ROUTINE			
L	Lower parameter of search	U*	Upper parameter of search
I	Middle of binary search	K1	Value to "search" for
T\$	Upper part of index string	B\$	Lower part of index
A\$	Index string		
VARIABLES USED IN THE RANKING AND TIED-VALUE CORRECTION ROUTINE			
L1	Last discrete rank value	C1	Index (position) of L1
C0	Number of ranks that = L1	C2	Sum of indexes after C1
T	"Current" rank value	R	Value to replace "current" tied ranks
* Some variables used for more than one purpose			

NOTES AND REFERENCES

- Notes:
1. A maximum of 254 items (TOTAL) may be entered. This is due to the design of the ranking program, and can't be changed easily. See the Notes and References to Kruskal-Wallis statistic.
 2. In accordance with statistical convention, the smaller of the two possible U-statistics is displayed. Variables U1 and U2 contain, respectively, the U-statistic computed using item 1 and the U-statistic computed using item 2.

- References:
1. J.E. Freund, MATHEMATICAL STATISTICS, (Prentice-Hall, 1962).
 2. S. Siegel, NON-PARAMETRIC STATISTICS, (McGraw-Hill, New York, 1956).
 3. TEST STATISTICS, HP-41C Users' Library solutions, (MANN-WHITNEY STATISTIC).

PROGRAM LISTING

```

10 ! Mann-Whitney test statistic
20 ! REV 11/01/82
30 !
40 DIM A(255),A$(255),I$(255),B$(255),
   A1(255),N(2)
50 DELAY .5
60 !
70 ! Rank conversion
80 !
90 DEF FNC(X) = NUM(A$(X,X))

100 !
110 ! Error correction
120 !
130 DEF FNI(X) = INT(X*10^5+.5)/10^5
140 DEF FNE

150 DISP "Item";N(S);"deleted =";A(N(S)
   +N0)
160 N=N-1 @ N(S)=N(S)-1 @ FNE=0
170 END DEF
180 !
190 ! Delay routine
200 !
210 DEF FND

220 K$=KEY$ @ IF K$(<>CHR$(13) AND K$(<>C
   HR$(8) THEN 220
230 FND=K$=CHR$(8) @ END DEF
240 !
250 ! Initialize
260 !
270 DISP "Mann-Whitney U-test statistic
   "
280 ON ERROR BEEP 440 @ DISP 'Enter num
   eric, ["E"], or ["C"]' @ GOTO 350
290 L1,A(0)=-INF @ C0=1 @ N,N0,N(1),N(2
   ),R,C1,C2=0
300 !
310 ! Input loop
320 !
330 FOR S=1 TO 2
340 DISP "Sample ";S;" ";CHR$(195);"=
   change, ";CHR$(197);"=end" @ WAIT 1
350 B$="" @ DISP "Sample";S;"Item";N(S)
   +1; @ INPUT B$
360 IF UPRC$(B$)="E" THEN 410
370 IF UPRC$(B$)="C" AND N(S)>0 THEN U=
   FNE @ GOTO 350
380 IF UPRC$(B$)="C" THEN DISP "Must ha
   ve data to delete" @ BEEP 220 @ GOT
   O 350
390 IF N>250 THEN BEEP @ DISP "WARNING-
   Can't accept n>254" @ WAIT 1.5

```

-Conversion function for
ranking routine

-Define precision of output
-Delete user's input error and
decrement counters

-Wait for 'RTN' or 'BACK' keys.
Return 1 if 'BACK' key

-Error trap

-Enter sample value

-End data entry if E is entered
-Call correction routine if C
is entered
-Return error if attempting to
delete non-existent data

-Return error if more than 254
data items entered

PROGRAM LISTING

```

400 X9=VAL(B$) @ N=N+1 @ N(S)=N(S)+1 @
    A(N(S)+N0)=X9 @ GOTO 350
410 IF N(S)<2 THEN BEEP 220 @ DISP "Must
    have more than one item" @ GOTO 3
    50
420 N0=N @ NEXT S
430 OFF ERROR
440 !
450 ! Binary sort
460 !
470 A$=CHR$(1) @ A(N+1)=-INF
480 FOR X=2 TO N
490 L=1 @ U=X-1
500 I=INT((L+U)/2)
510 K1=A(NUM(A$(I,I)))
520 IF A(X)=K1 THEN 550
530 IF A(X)<K1 THEN U=I-1 ELSE L=I+1
540 IF U>=L THEN 500
550 IF I>1 THEN B$=A$(I,I-1) ELSE B$=""
560 IF I<X-1 THEN T$=A$(I+1,LEN(A$)) EL
    SE T$=""
570 IF A(X)<K1 THEN A$=B$&CHR$(X)&A$(I,
    LEN(A$)) ELSE A$=A$(I,I)&CHR$(X)&T$
580 NEXT X
590 A$=A$&CHR$(0)
600 !
610 ! Paired ranks
620 !
630 FOR X=1 TO N
640 T=A(FNC(X)) @ IF T<>L1 AND C0=1 THE
    N L1=T @ A1(FNC(X))=X @ C1,C2=X @ G
    OTO 690
650 IF T=L1 THEN C0=C0+1 @ C2=C2+X
660 IF X<>N AND T=L1 THEN 690
670 R=C2/C0 @ FOR Q=C1 TO C1+C0-1 @ A1(
    FNC(Q))=R @ NEXT Q
680 C0=1 @ L1=T @ A1(FNC(X))=X @ C1,C2=
    X
690 NEXT X
700 !
710 ! Compute U and Z
720 !
730 R1,R2=0 @ FOR X=1 TO N(1) @ R1=R1+A
    1(X) @ NEXT X
740 FOR X=N(1)+1 TO N(1)+N(2) @ R2=R2+A
    1(X) @ NEXT X
750 U2=N(1)*N(2)+N(2)*(N(2)+1)/2-R2
760 U1=N(1)*N(2)+N(1)*(N(1)+1)/2-R1
770 U=U1 @ IF U2<U1 THEN U=U2
780 Z=(U-N(1)*N(2)/2)/SQR(N(1)*N(2)*(N(
    1)+N(2)+1)/12)
790 !
800 ! View ranks
810 !

```

-Increment counters, store value, and continue

-Binary index sort

-Binary search

-Insert preset index into A\$

-Store ranks in A1()

-Replace tied ranks

-Compute sum of ranks in variable 1 and 2

-Compute U using variable 2

-Compute U using variable 1

-Choose smallest U

-Compute z-score

PROGRAM LISTING

```

820 DISP "View the ranks? (";CHR$(217);
    "/" ;CHR$(206);")";
830 INPUT K$ @ K$=UPRC$(K$&" ")
840 IF POS("NY",K$[1,1])=0 THEN 820
850 IF K$="N " THEN 970
860 X1,X=0 @ Y=1
870 DISP "Sample";Y
880 X=X+1 @ X1=X1+1 @ IF X>N THEN 970
890 IF X1>N(Y) THEN Y=Y+1 @ X1=0 @ X=X-
    1 @ GOTO 870
900 DISP STR$(Y);", ";STR$(X1);" S=";A(
    X);"R=";A1(X) @ V=FND
910 IF V AND X1>1 THEN X=X-1 @ X1=X1-1
    @ GOTO 900
920 IF V AND Y>1 THEN Y=1 @ X1,X=N(1) @
    GOTO 900
930 GOTO 880
940 !
950 ! View U,V
960 !
970 DISP "U = ";FNI(U) @ V=FND
980 IF V THEN X=N @ X1=N(2) @ Y=2 @ GOT
    O 900
990 DISP "Z=";FNI(Z) @ V=FND @ IF V THE
    N 970
1000 DISP CHR$(210);"un again, ";CHR$(21
    4);"iew again, or ";CHR$(197);"nd";
1010 INPUT B$ @ B$=UPRC$(B$&" ")
1020 ON POS("RVE",B$[1,1])+1 GOTO 1000,2
    80,820,1030
1030 STOP

```

-Routine to view the ranks

-Printout/display routine

-Review module

PROGRAM DESCRIPTION

FISHER'S EXACT PROBABILITY

Fisher's exact probability test is used for analyzing a 2 x 2 contingency table when the two independent samples are small in size.

a (I-)	b (I+)
c (II-)	d (II+)

Given frequencies a, b, c, d, with a as the smallest frequency, this program calculates:

- 1) the exact probability of observing the given frequencies in a 2 x 2 table, when the marginal totals are regarded as fixed, and
- 2) the exact probability P_i ($i=1, 2, \dots, a$) of each more extreme table having the same marginal totals.

Formula:

$$\text{Exact probability } P_0 = \frac{(a+b)!(c+d)!(a+c)!(b+d)!}{N!a!b!c!d!}$$

Where: $N = a+b+c+d$

Each more extreme table (with the same margins)

$$P_i = \frac{(a+b)!(c+d)!(a+c)!(b+d)!}{N!(a-i)!(b+i)!(c+i)!(d-i)!}$$

Where: $P_i \in \{1, 2, \dots, a-1, a\}$

$$X! = (1)(2)\dots(X-1)(X)$$

SAMPLE PROBLEM

Calculate P_0 , P_2 , P_3 , and P_4 for the following table:

Frequency:	7	10
	8	5

NOTE: The table must be arranged as:

Frequency	5	8
	10	7

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "FISHER"	Fisher Exact Probability Test	
2	Enter frequency A	Enter Group I- (A)?	5 [RTN]
3	Enter frequency B	Enter Group I+ (B)?	8 [RTN]
4	Enter frequency C	Enter Group II- (C)?	10 [RTN]
5	Enter frequency D	Enter Group II+ (D)?	7 [RTN]
6	Read probabilities, Use	Exact probability = .01467	[RTN]
	[RTN] to see the next	Prob.(1) = .05705	[RTN]
	probability	Prob.(2) = .13691	[RTN]
		Prob.(3) = .1867	[RTN]
		Prob.(4) = .12446	[RTN]
		Prob.(5) = .02872	[RTN]
7	End program	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Arrange table so that a is		
	the smallest frequency		
1	Run "FISHER"	Fisher Exact Probability	
2	Enter frequency A	Enter group I- (A)?	a [RTN]
3	Enter frequency B	Enter group I+ (B)?	b [RTN]
4	Enter frequency C	Enter group II- (C)?	c [RTN]
5	Enter frequency D	Enter group II+ (D)?	d [RTN]
6	View probabilities. Use [RTN]	Exact probability =	[RTN]
	to see next display, [BACK]	Prob. (1) =	[RTN]
	to see previous one	Prob. (2) =	[RTN]/[BACK]
		Prob. (3) =	[RTN]/[BACK]
		Prob. (4) =	[RTN]/[BACK]
		Prob. (5) =	[RTN]/[BACK]
7	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun the program - step 2		R [RTN]
	V = review results - step 6		V [RTN]
	E = end program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
P()	Probability storage	K\$	General input string
F	Factorial function	A	Group I- (A)
B	Group I+ (B)	C	Group II- (C)
D	Group II+ (D)	N	A+B+C+D
I,X	Index values	U	Delay flag, = 1 if [BACK]

NOTES AND REFERENCES

- Notes:
1. a must be the smallest among the frequencies. Rearrange the table if necessary.
 2. This program requires that $a \leq 50$. To change this limit, change the dimension statement in line 70.
 3. This program contains a routine for calculating the factorial of a number in lines 170-230. You can use it in your own program as follows:

```

1000 DEF FNF(N)
1010 F=1
1020 FOR X=2 to N
1030 F=F*X
1040 NEXT X
1050 FNF=F @ END DEF
.....
2300 A=FNF(B)/C (Sample formula)
.....

```

- References:
1. Sidney Siegel, NONPARAMETRIC STATISTICS, (McGraw-Hill, 1956).
 2. Sir R.A. Fisher, STATISTICAL METHODS FOR RESEARCH WORKERS, (Oliver and Boyd, 1950).
 3. Hewlett-Packard, HP-41C Users' Library Solutions TEST STATISTICS, formula from program FISHER'S EXACT TEST FOR A 2 x 2 CONTINGENCY TABLE, p. 39.

PROGRAM LISTING

```

10 ! FISHER - Fisher's exact
20 ! test for a 2*2 contingency
30 ! table
40 ! REV 11/01/82
50 !
60 DISP " Fisher Exact Probability Te
  st"
70 DIM P(50),K$(20)
80 !
90 ! Delay routine
100 !
110 DEF FND

120 K$=KEY$ @ IF K$(<>CHR$(13) AND K$(<>C
  HR$(8) THEN 120
130 FND=K$=CHR$(8) @ END DEF
140 !
150 ! Calculate factorial
160 !
170 DEF FNF(N)
180 F=1
190 FOR X=2 TO N
200 F=F*X
210 NEXT X
220 FNF=F
230 END DEF
240 !
250 ! Limit output precision
260 !
270 DEF FNI(X) = INT(X*100000+.5)/10000
  0
280 INPUT "Enter Group I- (A) ?";A
290 INPUT "Enter Group I+ (B) ?";B
300 INPUT "Enter Group II- (C) ?";C
310 INPUT "Enter group II+ (D) ?";D
320 IF (A<B)+(A<C)+(A<D)=3 THEN 340

330 BEEP 880 @ DISP "A must be the smal
  lest freq." @ WAIT 1 @ GOTO 140
340 N=A+B+C+D
350 !
360 ! Calculate prob.
370 !
380 FOR I=0 TO A

390 P(1)=FNF(A+B)*FNF(C+D)*FNF(A+C)*FNF
  (B+D)
400 P(I)=P(I)/(FNF(N)*FNF(A-I)*FNF(B+I)
  *FNF(C+1)*FNF(D-I))
410 NEXT I
420 !
430 ! Printout
440 !
450 DISP "Exact probability =" ;FNI(P(0)
  ) @ U=FND @ IF U THEN 450

```

-Wait for 'RTN' or 'BACK' keys.
Return 1 if 'BACK' key

-Function to compute factorial

-Function to define output
precision
-Enter the frequencies

-Verify that A is the smallest
frequency

-Calculate the probabilities.
Store exact prob. in A(0)

-Display the probabilities

	PROGRAM LISTING	
--	-----------------	--

```

460 X=0
470 X=X+1 @ IF X>A THEN 540
480 DISP "Prob.(";X;") =";FNI(P(X)) @ U
    =FND
490 IF U THEN X=X-(X>1) @ GOTO 480
500 GOTO 470
510 !
520 ! Review routine
530 !
540 DISP CHR$(210);"un again, ";CHR$(21
    4);"iew again, or ";CHR$(197);"nd "
    ;
550 INPUT K$ @ K$=UPRC$(K$&" ")
560 ON POS("RVE",K$[1,1])+1 GOTO 540,28
    0,450,570
570 STOP

```

-Review module

PROGRAM DESCRIPTION

2-FACTOR ANALYSIS OF VARIANCE

A two way analysis of variance allows the user to test the null hypothesis against columns, (condition a), rows (condition b), and the interaction of rows and columns, (a*b). This program can be generalized to any sized p*q 2-factor experiment, depending upon memory size. Unequal cell sizes are handled by considering each cell as though it contained the same number of subjects as all the other cells, with an adjustment based upon the harmonic mean. If the cell sizes are equal, the harmonic mean will have no effect.

RESTRICTIONS: If the cell sizes are relevant to the experimental manipulation, then other methods should be used. Severe variations in cell size (greater than 2:1) should be avoided. A negative Sum Square for the interaction term is cause for the immediate use of other methods.

p = number of rows

q = number of columns

	Cell means				Total
	$\bar{X}_{11}$	$\bar{X}_{12}$		$\bar{X}_{1q}$	a_1
	$\bar{X}_{21}$	$\bar{X}_{22}$		$\bar{X}_{2q}$	a_2
	$\bar{X}_{31}$	$\bar{X}_{32}$		$\bar{X}_{3q}$	a_3
	$\vdots$	$\vdots$		$\vdots$	$\vdots$
	$\bar{X}_{p1}$	$\bar{X}_{p2}$		$\bar{X}_{pq}$	a_p
Total	B_1	B_2		B_q	G

Intermediate formulas:

$$(1) = G^2/pq$$

$$(2) = (\sum a_i^2)/q$$

$$(3) = (\sum B_j^2)/p$$

$$(4) = (\sum \bar{X}_{ij})^2$$

$$\text{Harmonic mean } \bar{n}_h = \frac{pq}{\sum \sum (1/n_{ij})}$$

PROGRAM DESCRIPTION

2-FACTOR ANALYSIS OF VARIANCE (continued)

$$SS_{\text{within}} = \sum \sum \left(\sum_c X_{cij}^2 - \left(\frac{\sum X_{cij}}{n_{ij}} \right)^2 \right) \quad df_w = \sum \sum n_{ij} - pq \quad MS_w = SS_w / df_w$$

$$SS_a = \bar{n}_h [(2) - (1)] \quad df_a = p - 1 \quad MS_a = SS_a / df_a \quad F_a = MS_a / MS_w$$

$$SS_b = \bar{n}_h [(3) - (1)] \quad df_b = q - 1 \quad MS_b = SS_b / df_b \quad F_b = MS_b / MS_w$$

$$SS_{ab} = \bar{n}_h [(4) - (2) - (3) + (1)] \quad df_{ab} = (q-1)(p-1)$$

$$MS_{ab} = SS_{ab} / df_{ab} \quad F_{ab} = MS_{ab} / MS_w$$

SAMPLE PROBLEM

An experimenter wishes to study the effects of standard vs. reverse polish calculation under 3 conditions of instruction by scoring the number of errors per 100 calculations.

		Conditions (B)		
Calculators (A)	RPN	1	2	3
	STANDARD	3,3,2	2,2,1	3,1,2
		9,6,7	8,6,6	9,5

(artificial data)

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "AOV2F"	2-Factor Analysis of Variance	
1	Enter the row dimensions	How many rows (p)?	2 [RTN]
2	Enter the column dimensions	How many columns (q)?	3 [RTN]
3	Display the means	Print the means (Y/N)?	Y [RTN]
		<u>C</u> to correct, <u>E</u> to end cell	
6	Enter column (1,1)	Row 1 Clm. 1 Item 1?	3 [RTN]
		Row 1 Clm. 1 Item 2?	3 [RTN]
		Row 1 Clm. 1 Item 3?	2 [RTN]
6b	End column (1,1)	Row 1 Clm. 1 Item 4?	E [RTN]
7	Read mean and SD (n-1)	[1,1] Mean = 2.66667 N = 3	[RTN]
7	Use [BACK] to review mean	[1,1] Std. = .4714	[RTN]
6	Enter column (1,2)	Row 1 Clm. 2 Item 1?	2 [RTN]
		Row 1 Clm. 2 Item 2?	2 [RTN]
		Row 1 Clm. 2 Item 3?	1 [RTN]
6b	End column (1,2)	Row 1 Clm. 2 Item 4?	E [RTN]
7		[1,2] Mean = 1.66667 N = 3	[RTN]

	SOLUTION	
--	----------	--

STEP	INSTRUCTIONS	DISPLAY	INPUT
		[1,2] Std. = .4714	[RTN]
6	Enter column (1,3)	Row 1 Clm. 3 Item 1?	3 [RTN]
		Row 1 Clm. 3 Item 2?	1 [RTN]
		Row 1 Clm. 3 Item 3?	2 [RTN]
6b	End column (1,3)	Row 1 Clm. 3 Item 4?	E [RTN]
7		[1,3] Mean = 2 N = 3	[RTN]
		[1,3] Std. = .8165	[RTN]
6	Enter column (2,1)	Row 2 Clm. 1 Item 1?	9 [RTN]
		Row 2 Clm. 1 Item 2?	6 [RTN]
		Row 2 Clm. 1 Item 3?	7 [RTN]
6b	End column (2,1)	Row 2 Clm. 1 Item 4?	E [RTN]
7		[2,1] Mean = 7.3333 N = 3	[RTN]
		[2,1] Std. = 1.24722	[RTN]
6	Enter column (2,2)	Row 2 Clm. 2 Item 1?	8 [RTN]
		Row 2 Clm. 2 Item 2?	6 [RTN]
		Row 2 Clm. 2 Item 3?	6 [RTN]
6b	End column (2,2)	Row 2 Clm. 2 Item 4?	E [RTN]
7		[2,2] Mean = 6.66667 N = 3	[RTN]
		[2,2] Std. = .94281	[RTN]
6	Enter column (2,3)	Row 2 Clm. 3 Item 1?	9 [RTN]
	Error	Row 2 Clm. 3 Item 2?	95 [RTN]
6a	Call error correction	Row 2 Clm. 3 Item 3?	C [RTN]
	This will be displayed:	2,3,2 deleted = 95	
6	Enter correct value	Row 2 Clm. 3 Item 2?	5 [RTN]
6b	End column (2,3)	Row 2 Clm. 3 Item 3?	E [RTN]

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
7		[2,3] Mean = 7 N = 2	[RTN]
		[2,3] Std. = 2	[RTN]
9	Read output using [RTN] key	A SS = 99.28205 df = 1	[RTN]
	to see next result.	A MS = 99.28205 F = 58.50549	[RTN]
		B SS = 1.94872 df = 2	[RTN]
		B MS = .97436 F = .57418	[RTN]
		AB SS = .10256 df = 2	[RTN]
		AB MS = .05128 F = .03022	[RTN]
		Within SS = 18.66667 df = 11	[RTN]
		Within MS = 1.69697	[RTN]
10	End program	Run again, View again, or End?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "AOV2F"	2-Factor Analysis of Variance	
1	Enter row dimensions	How many rows (p)?	p [RTN]
2	Enter column dimensions	How many columns (q)?	q [RTN]
3	Display cell means?	Print the means (Y/N)?	Y or N [RTN]
		<u>C</u> to correct, <u>E</u> to end cell	
4	Enter cell value	Row i Clm. j Item c?	Xijc [RTN]
5a	If error, call correction	Row i Clm. j Item c?	C [RTN]
	This will be displayed:	i,j,c deleted = Xijc	
	If not done, goto 4 else		
5b	If cell is finished	Row i Clm. j Item c?	E [RTN]
6	If you answered Y to #3:	[i,j] Mean = N=	[RTN]
		[i,j] Std. =	[RTN]/[BACK]
7	Goto 6 until all rows and columns are done.		
8	Read output. Use [RTN] key	A SS = df =	[RTN]
	to see next result, [BACK]	A MS = F =	[RTN]/[BACK]
	key to see previous result.	B SS = df =	[RTN]/[BACK]
		B MS = F =	[RTN]/[BACK]
		AB SS = df =	[RTN]/[BACK]
		AB MS = F =	[RTN]/[BACK]
		Within SS = df =	[RTN]/[BACK]
		Within MS =	[RTN]/[BACK]
9	Review routine	Run again, View again, or End?	
	R = rerun the program - step 2		R [RTN]
	V = review results - step 8		V [RTN]
	E = End the program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
P	Number of rows (p)	Q	Number of columns (q)
A()	Sum of cell means (row)	X()	Temporary cell storage
B()	Sum of cell means (clm)	N0	Temporary n per cell
X\$,A\$	General input strings	N1	Grand total n
X1	Temporary Σx per cell	X2	Temporary Σx^2 per cell
G1	Grand sum of cell means	S0	Temporary SD(x) of cell
A2	Sum of A-squared	B2	Sum of B-squared
H1	Harmonic mean	M	Temporary mean of cell
E1	Computation formula #1	E3	Computation formula #3
E4	Computation formula #4	E5	Computation formula #5
S1	Sum-Squared of A (SSa)	M1	Mean-Squared of A (MSa)
S2	Sum-Squared of B (SSb)	M2	Mean-Squared of B (MSb)
S3	Sum-Squared of AB (SSab)	M3	Mean-Squared of AB (MSab)
S4	Sum-Squared within cell	M4	Mean-Squared within cell
D1	Df. of A (p-1)	D2	Df. of B (q-1)
D3	Df. of AB (q-1)	D4	Df. within (G-P*Q)
F1	F-ratio of A	F3	F-ratio within
F2	F-ratio of B	P1	Flag 1=display cell means

NOTES AND REFERENCES

Notes: This program is limited to 20 rows, 20 columns, and 50 items per cell. To change this, change the dimensions in line 80.

References: Winer, B.J., STATISTICAL PRINCIPLES IN EXPERIMENTAL DESIGN, 2nd ED., (McGraw-Hill, New York, 1971), p. 446-447.

PROGRAM LISTING

```

10 ! ANOVA2F - 2-factor
20 ! Analysis of variance
30 ! (equal or unequal cell size)
40 ! Unweighted (NON least-squares) method
50 ! REV 11/01/82
60 !
70 DISP "2-Factor Analysis of Variance" @ WAIT 1
80 DIM A(20),B(20),X$(50),X(50),A$(20)
90 !
100 ! Precision
110 !
120 DEF FNI(X) = INT(X*10^5+.5)/10^5
130 !
140 ! Correction
150 !
160 DEF FNE
170 IF N0<1 THEN BEEP 880 @ DISP "Must
    Have data to delete" @ GOTO 200
180 DISP I;",";J;",";N0;"Deleted =";X(N0) @ WAIT 1
190 X1=X1-X(N0) @ X2=X2-X(N0)^2 @ N0=N0-1 @ N1=N1-1
200 FNE=0 @ END DEF
210 !
220 ! Delay
230 !
240 DEF FND
250 X$=KEY$ @ IF X$(<>CHR$(13) AND X$(<>CHR$(8) THEN 250
260 FND=X$=CHR$(8) @ END DEF
270 !
280 ! Initialize
290 !
300 INPUT "How many rows (p) ?";P
310 INPUT "How many columns (q) ?";Q
320 INPUT "Print the means (Y/N) ?"; X$
    @ P1=POS(UPRC$(X$),"Y")
330 FOR X=1 TO P @ A(X)=0 @ NEXT X
340 FOR Y=1 TO Q @ B(Y)=0 @ NEXT Y
350 N1,G1,S4,E5,A2,B2,M1,N1,H1=0
360 DISP CHR$(195);" to correct, ";CHR$(197);" to end cell." @ WAIT 1
370 !
380 ! Error trapping
390 !
400 ON ERROR BEEP 880 @ DISP "Please enter IEL,ICL,or numeric" @ WAIT 1 @ GOTO 460
410 !

```

-Function to define output precision

-Error correction routine to delete data from counters

-Wait for 'RTN' or 'BACK' keys. Returns 1 if 'BACK' key

-Starting prompts

-Initialize counters

-Error message for data entry routines

PROGRAM LISTING

```

420 ! Input routine
430 !
440 FOR I=1 TO P @ FOR J=1 TO Q
450 N0=0 @ X1=0 @ X2=0
460 DISP "Row";I;"Clm.";J;"Item";N0+1;
470 X$="" @ INPUT X$
480 IF POS(UPRC$(X$),"C") THEN U=FNE @
    GOTO 460
490 IF POS(UPRC$(X$),"E") THEN 550

500 X=VAL(X$) @ X1=X1+X @ X2=X2+X^2 @ N
    0=N0+1 @ X(N0)=X @ N1=N1+1
510 GOTO 460
520 !
530 ! End cell
540 !
550 IF N0<2 THEN BEEP 880 @ DISP "Must
    have >1 datum per cell." @ WAIT 1 @
    GOTO 460
560 M=X1/N0 @ S4=S4+X2-X1^2/N0
570 H1=H1+1/N0 @ A(I)=A(I)+M @ B(J)=B(J)
    +M
580 E5=E5+M^2 @ G1=G1+M @ S0=SQR((X2-X1
    ^2/N0)/N0)
590 IF P1=0 THEN BEEP 440 @ GOTO 620
600 DISP "I";I;",";J;"I Mean =";FNI(M);
    "N=";N0 @ U=FND @ IF U THEN 600
610 DISP "I";I;",";J;"I Std.=";FNI(S0)
    @ U=FND @ IF U THEN 600
620 NEXT J @ NEXT I
630 H1=P*Q/H1
640 FOR I=1 TO P @ A2=A2+A(I)^2 @ NEXT
    I
650 FOR J=1 TO Q @ B2=B2+B(J)^2 @ NEXT
    J
660 !
670 ! Sub-equations
680 !
690 E1=G1^2/(P*Q)
700 E3=A2/Q @ E4=B2/P
710 !
720 ! Compute SS,MS,df,F
730 !
740 D1=P-1 @ S1=H1*(E3-E1) @ M1=S1/D1
750 D2=Q-1 @ S2=H1*(E4-E1) @ M2=S2/D2
760 D3=(Q-1)*(P-1) @ S3=H1*(E5-E3-E4+E1
    ) @ M3=S3/D3
770 D4=N1-P*Q @ M4=S4/D4
780 F1=M1/M4 @ F2=M2/M4 @ F3=M3/M4
790 !
800 ! Display the results
810 !
820 DISP "A SS=";FNI(S1);"df=";D1 @ U=
    FND @ IF U THEN 820

```

-Data entry

-Call error correction if 'C' is entered

-Goto end of cell if 'E' is entered

-Increment cell counters and total N

-Cell mean

-Harmonic mean counter, grand total

-Cell standard deviation (n)

-Display mean if P1 is set

-Compute sum of A-squared, sum of B-squared

-Computation

-Display results

PROGRAM LISTING

```

830 DISP "A  MS=";FNI(M1);"F=";FNI(F1)
    @ U=FND @ IF U THEN 820
840 DISP "B  SS=";FNI(S2);" df=";D2 @
    U=FND @ IF U THEN 830
850 DISP "B  MS=";FNI(M2);" F=";FNI(F2
    ) @ U=FND @ IF U THEN 840
860 DISP "AB SS=";FNI(S3);" df=";D3 @
    U=FND @ IF U THEN 850
870 DISP "AB MS=";FNI(M3);" F=";FNI(F3
    ) @ U=FND @ IF U THEN 860
880 DISP "Within SS=";FNI(S4);"df=";D4
    @ U=FND @ IF U THEN 870
890 DISP "Within MS=";FNI(M4) @ U=FND @
    IF U THEN 880
900 DISP CHR$(210);"un again, ";CHR$(21
    4);"iew again, or ";CHR$(197);"nd";
910 INPUT A$ @ A$=UPRC$(A$&" ")
920 ON POS("RVE",A$(1,1))+1 GOTO 900,30
    0,820,930
930 STOP

```

-Review module

PROGRAM DESCRIPTION

BARTLETT'S CHI-SQUARE STATISTIC

Bartlett's Chi-square has a distribution (approximately) with $k-1$ degrees of freedom which can be used to test the null hypothesis that the variances are all estimates of the same population variance.

F max tests the hypothesis that the largest and the smallest variance come from the same population of variances.

Formula: (Note: $\chi = \text{CHI}$)

$$\chi^2 = \frac{f \ln(S^2) - \sum_{i=1}^K f_i \ln(s_i^2)}{1 + \left(\frac{1}{3(K-1)}\right) \left[\left(\sum_{i=1}^K \frac{1}{f_i}\right) - \frac{1}{f} \right]}$$

Where: s_i^2 = Sample variance of the i^{th} sample

f_i = Degrees of freedom ($n_i - 1$) of the i^{th} sample

$$s^2 = \frac{\sum_{i=1}^K f_i s_i^2}{f}$$

$$f = \sum_{i=1}^K f_i$$

$$F_{\text{max}} = \max(s^2) / \min(s^2)$$

SAMPLE PROBLEM

Determine whether the variances of the groups shown below differ significantly across the groups. The obtained chi-square of 1.04 shows that the differences are not significant.

Group	N (not used)	Variance (σ)	Degrees of freedom (df)
1	21	12.20	20
2	13	13.50	12
3	15	7.86	14
4	10	10.89	9

Df is based upon N-1

Data comes from Edwards, EXPERIMENTAL DESIGN IN PSYCHOLOGICAL RESEARCH.

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "BARTLETT"	Bartlett's Chi-square Statistic	
		E,E to end, C,C to correct	
1	Enter sample 1	Sample 1 enter var., df?	12.2, 20 [RTN]
	Enter sample 2	Sample 2 enter var., df?	13.5, 12 [RTN]
	Error	Sample 3 enter var., df?	12,3 [RTN]
2	Call error correction	Sample 4 enter var., df?	C C [RTN]
	This will be displayed:	Sample 3 deleted = 12,3	
1	Enter correct values	Sample 3 enter var., df?	7.86, 14 [RTN]
	Enter sample 4	Sample 4 enter var., df?	10.89, 9 [RTN]
3	End data input	Sample 5 enter var., df?	E,E [RTN]
4	Real results. Use [RTN] to	Chi-square = 1.04955	[RTN]
	see next item.	Fmax = 1.71756	[RTN]
		df = 3	[RTN]
5	End program	Run again, View again, or End?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "BARTLETT"	Bartlett's Chi-square Statistic	
		E,E to end, C,C to correct	
2	Enter value of sample	Sample i enter var, df?	σ ,df. [RTN]
3	If an error was made:	Sample i enter var, df?	C,C [RTN]
	this will be displayed	Sample i deleted = Si,DFi	
	Goto 2 until all samples have		
	been entered		
4	To end data input:	Sample i enter var, df?	E,E [RTN]
5	Read display. Use [RTN] to	Chi-square =	[RTN]
	see next item, [BACK] to	F max =	[RTN]/[BACK]
	see previous item	df =	[RTN]/[BACK]
6	Review routine	Run again, View again, or End?	
	R = rerun the program - step 2		R [RTN]
	V = review results - step 5		V [RTN]
	E = end the program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
S2()	Variance storage	F()	Storage of df.
A\$	Variance input, general use	B\$	Df. input
K	Total number of sample	U	Delay flag, = 1 if [BACK] used
S4	Sum of inverse df	M1	Minimum variance
A1	Maximum variance	M0	F max
C0	Chi-square value	D	Total df. (degrees of freedom)

NOTES AND REFERENCES

Notes: 1. This program is presently limited to a maximum of 50 samples.
To change this limit, change the dimension statement in line 70.

2. Because a different method was used, the solution to the sample problem is slightly different from the solution in Edwards EXPERIMENTAL DESIGN IN PSYCHOLOGICAL RESEARCH, p. 198.

- References: 1. Hald, A., STATISTICAL THEORY WITH ENGINEERING APPLICATIONS, (John Wiley and Sons, 1960).
2. Edwards, A., EXPERIMENTAL DESIGN IN PSYCHOLOGICAL RESEARCH, (Rinehart & Co., 1950), p. 198.
3. Hewlett-Packard, HP-41C Users' Library solutions TEST STATISTICS, Procedure from Bartlett's Chi-square Statistic, p. 46.

PROGRAM LISTING

```

10 ! BARTLETT - Bartlett's Chi-
20 ! square statistic (test for
30 ! homogeneity of variance)
40 !
50 ! REV 11/01/82
60 DISP "Bartlett's Chi-square Statist
ic" @ WAIT 1
70 DIM S2(50),F(50),A$(10),B$(10)
80 !
90 ! Correction routine
100 !
110 DEF FNE
120 IF K<1 THEN BEEP 440 @ DISP "Must h
ave data to delete" @ GOTO 150
130 DISP "Sample";K;"deleted =";S2(K);"
";F(K)
140 S2=S2-S2(K)*F(K) @ F=F-F(K) @ S3=S3
-F(K)*LOG10(S2(K)) @ S4=S4-1/F(K) @
K=K-1
150 FNE=0 @ END DEF
160 !
170 ! Delay routine
180 !
190 DEF FND

200 K$=KEY$ @ IF K$(>)CHR$(8) AND K$(>)CH
R$(13) THEN 200
210 FND=K$=CHR$(8) @ END DEF
220 DEF FNI(X) = INT(X*10^5+.5)/10^5

230 S2,S3,S4,F,K=0 @ A1=-INF @ M1=INF
240 DISP "E,E to end, C,C to correct" @
WAIT 1
250 ON ERROR BEEP 220 @ DISP "Enter [E]
[RTN],[C][RTN] or S2,F" @ WAIT 1 @
GOTO 260
260 DISP "Sample";K+1;"enter var., df";
270 INPUT A$,B$
280 IF POS(UPRC$(A$(1,1)),"E") THEN 360
290 IF POS(UPRC$(A$(1,1)),"C") THEN U=F
NE @ GOTO 260
300 S2(K+1)=VAL(A$) @ F(K+1)=VAL(B$)
310 S3=S3+VAL(B$)*LOG10(VAL(A$)) @ S4=S
4+1/VAL(B$)
320 F=F+VAL(B$) @ S2=S2+VAL(A$)*VAL(B$)
@ K=K+1 @ GOTO 250
330 !
340 ! End of data
350 !
360 S2=S2/F @ C0=(F*LOG10(S2)-S3)*2.302
6/((1+1/(3*(K-1)))*(S4-1/F))
370 FOR I=1 TO K @ IF S2(I)>A1 THEN A1=
S2(I)

```

-Correct user's output

-Delete incorrect value from the counters

-Wait for 'RTN' or 'BACK' keys. Return 1 if 'BACK' key

-Function to define the output precision

-Initialize counters

-Error trap

-Goto end-of-data if 'E' is entered

-Call error correction if 'C' is entered

-Increment counters and enter next sample

-End of data- compute chi-square value

-Determine maximum/minimum variance

PROGRAM LISTING

```

380 IF S2(I)<M1 THEN M1=S2(I)
390 NEXT I
400 M0=A1/M1 @ D=K-1

410 PRINT "Chi-square =",FNI(C0) @ U=FN
    D @ IF U THEN 410
420 PRINT "Fmax =",FNI(M0) @ U=FND @ IF
    U THEN 410
430 PRINT "df=";D @ U=FND @ IF U THEN 4
    20
440 DISP CHR$(210);"un again, ";CHR$(21
    4);"iew again, or ";CHR$(197);"nd "
    ;
450 INPUT "?"; A$ @ A$=UPRC$(A$&" ")
460 ON POS("RVE",A$[1,1])+1 GOTO 440,23
    0,410,470
470 STOP

```

-Compute F max, total degrees
of freedom

-Display the results

-Review module

PROGRAM DESCRIPTION

DIFFERENCES AMONG PROPORTIONS

This program tests proportions in independent sets of data to determine if each could have been randomly drawn from the same population of proportions. A chi-square statistic with k-1 degrees of freedom is computed. Theta is a measure of association between the independent (groups) and dependent (proportions) variables.

Equations:

$$\chi^2 = \sum_{i=1}^K \frac{(C_{1,i} - n_i \hat{\theta})^2}{n_i \hat{\theta} (1 - \hat{\theta})}$$

Where:

$$\hat{\theta} = \sum C_{1,i} / \sum n_i$$

$$n_i = C_{1,i} + C_{2,i}$$

K = number of samples

SAMPLE PROBLEM

Suppose that a simple test of mechanical ability is given to 4 groups of school children under the conditions found below. Determine whether there is a difference among the effectiveness of the 4 experimental conditions by testing the null hypothesis, which is that the proportion of successes in the 4 groups should not be significantly different.

Condition	C_1	C_2
	Failure	Success
Extensive training before lunch	8	42
Extensive training after lunch	12	18
Minimal training before lunch	50	170
Minimal training after lunch	9	90

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "DIFF"	Differences Among Proportions	
		E,E to end input, C,C to correct	
2	Enter case 1 fail, success	Sample 1 enter C1,C2?	8,42 [RTN]
	Enter case 2	Sample 2 enter C1,C2?	12,18 [RTN]
	Enter case 3	Sample 3 enter C1,C2?	50,170 [RTN]
	Error	Sample 4 enter C1,C2?	19,19 [RTN]
	Call correction routine	Sample 5 enter C1,C2?	C,C [RTN]
	This will be displayed:	Sample 4 deleted = 19,19	
		Sample 4 enter C1,C2?	9,90 [RTN]
3	End data input	Sample 5 enter C1,C2?	E,E [RTN]
4	Real display, use [RTN] to	Chi-square = 16,50082	[RTN]
	see next output.	df = 3	[RTN]
		Theta = .19799	[RTN]
5	End program	Run again, View again, or End?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
1	Run "DIFF"	Differences Among Proportions	
		E,E to end input, C,C to correct	
2	Enter indicated case:	Sample i enter C1,C2?	C1i,C2i[RTN]
	If you made an error:	Sample i enter C1,C2?	C,C [RTN]
	This will be displayed:	Sample i deleted = C1i,C2i	
	Goto 2 until all data has		
	been entered.		
3	End data input	Sample i enter C1,C2?	E,E [RTN]
4	Read output. User [RTN] to	Chi-square = χ^2	[RTN]
	see next output, [BACK] to	df = df	[RTN]/[BACK]
	see previous output.	Theta = $\hat{\theta}$	[RTN]/[BACK]
5	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun the program step 2		R [RTN]
	V = review results - step 4		V [RTN]
	E = end program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
C1()	Storage of condition 1	C2()	Storage of condition 2
A\$	General use, input C1()	B\$	Input C2() (Condition 2)
X1	Sum of condition 1	N1	Sum of N(i)
N	Total N	T	Theta
D	Degrees of freedom	C2	Chi-square value
NO	Temporary N(i)		

NOTES AND REFERENCES

Notes: 1. A maximum of 300 samples may be entered. To change this limit, change the dimension statement in line 70.

References: 1. J. Freund, MATHEMATICAL STATISTICS, (Prentice-Hall, 1971).

2. Allen L. Edwards, EXPERIMENTAL DESIGN IN PSYCHOLOGICAL RESEARCH (Rinehart & Co., 1950), p. 74.

This program was derived from the HP-41 Users' Library Solutions Book, "Test Statistics", program DIFFERENCES AMONG PROPORTIONS, p. 9.

PROGRAM LISTING

```

10 ! DIFF- Differences
20 ! among proportions
30 ! REV 11/01/82
40 !
50 DELAY .5
60 DISP "Differences among proportions
"
70 DIM C1(300),C2(300),A$(50),B$(50)
80 !
90 ! Correction
100 !
110 DEF FNE

120 IF N<1 THEN BEEP 220 @ DISP "Must h
ave data to delete" @ WAIT 1 @ GOTO
150
130 DISP "Sample";N;"deleted =";C1(N);"
,";C2(N) @ WAIT 1
140 X1=X1-C1(N) @ N1=N1-C1(N)-C2(N) @ N
=N-1
150 FNE=0 @ END DEF
160 !
170 ! Delay routine
180 !
190 DEF FND

200 A$=KEY$ @ IF A$(>CHR$(8) AND A$(>CH
R$(13) THEN 200
210 FND=A$=CHR$(8) @ END DEF
220 DEF FNI(X) = INT(X*10^5+.5)/10^5

230 !
240 ! Input routine
250 !
260 X1,N1,N=0
270 DISP CHR$(197);" to end input, ";CH
R$(195);" to correct" @ WAIT 1
280 ON ERROR BEEP 220 @ DISP 'Enter I"E
"1,["C"1,or ["C1,C21' @ WAIT 1.5 @ G
OTO 290
290 DISP "Sample";N+1;" enter C1,C2 ";
@ INPUT A$,B$
300 IF UPRC$(A$)="E" THEN 340

310 IF UPRC$(A$)="C" THEN U=FNE @ GOTO
290
320 C1(N+1)=VAL(A$) @ C2(N+1)=VAL(B$) @
N=N+1
330 X1=X1+C1(N) @ N1=N1+C1(N)+C2(N) @ G
OTO 290
340 IF N<2 THEN BEEP 220 @ DISP "Please
enter more than 1 sample" @ WAIT 1
@ GOTO 290
350 !

```

-Routine to correct error and decrement counters

-Wait for 'RTN' or 'BACK' key. Return 1 for 'BACK' key

-Function to define output precision

-Error trap- returns warning if illegal data is entered

-End data entry if 'E' is entered

-Call correction routine if 'C' is entered

-Increment counters, store condition values, and cont.

-End routine- verify that N>1

PROGRAM LISTING

360 ! Computation

370 !

380 T=X1/N1

390 D=N-1

400 C2=0

410 FOR I=1 TO N

420 N0=C1(I)+C2(I)

430 C2=C2+(C1(I)-N0*T)^2/(N0*T*(1-T))

440 NEXT I

450 !

460 ! Print out

470 !

480 PRINT "Chi-square=";FNI(C2) @ U=FN
D @ IF U THEN 480

490 PRINT "df=";D @ U=FND @ IF U THEN 4
80

500 PRINT "Theta=";FNI(T) @ U=FND @ IF
U THEN 490

510 !

520 ! Review routine

530 !

540 DISP CHR\$(210);"on again, ";CHR\$(21
4);"iew again, or ";CHR\$(197);"nd "
;

550 INPUT A\$ @ A\$=UPRC\$(A\$&" ")

560 ON POS("RVE",A\$(1,1))+1 GOSUB 540,2
60,480,570

570 STOP

-Compute Theta

-Loop to compute chi-square
value

-Routine to display data

-Review module

PROGRAM DESCRIPTION

DATA TRANSFORMATIONS

This program will either transform or standardize data sets. The square-root transformation is appropriate in analysis of variance when cell variances tend to be functions of the cell means. The log transformation is useful when normalizing distributions with positive skew.

The standard score (z score) manipulation converts distributions into standard score form, with a mean of zero and unit standard deviation. The T transformation changes data into a distribution with a mean and standard deviation defined by the user.

Formula:

$$\text{mean} = \bar{X} = \frac{\sum X}{n}$$

$$\text{Standard deviation } \sigma_x = \sqrt{\left(\frac{\sum X^2}{n}\right) - \left(\frac{\sum X}{n}\right)^2}$$

$$\text{Log transformation} = \log_e X$$

$$\text{Square root transformation} = \sqrt{X}$$

$$\text{Standard score } s = \frac{X - \bar{X}}{\sigma_x}$$

$$\text{T transform } t = s(\sigma_c) - \bar{X}_c$$

Where: σ_c is the constant standard deviation.

$\bar{X}_c$ is the constant mean.

SAMPLE PROBLEM

The following data represents the time (in minutes) that it took 8 new HP-75 owners to build a short, working BASIC program on their new computers. Convert these scores to:

- 1) standard scores, and
- 2) t-scores with a mean of 75 and a standard deviation of 12.

	<u>Owner</u>							
	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>	<u>6</u>	<u>7</u>	<u>8</u>
Time (minutes)	27	15	26	17	12	9	8	27
(Artificial data)								

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "TRANS"	Transformations	
		E to end input, C to correct	
1	Enter datum 1	Item 1 Score?	27 [RTN]
	Enter datum 2	Item 2 Score?	15 [RTN]
	Enter datum 3	Item 3 Score?	26 [RTN]
	ERROR	Item 4 Score?	177 [RTN]
2	Call error correction	Item 5 Score?	C [RTN]
	This will be displayed	Item 4 deleted = 177	
1	Enter correct value	Item 4 Score?	17 [RTN]
	Enter datum 5	Item 5 Score?	12 [RTN]
	Enter datum 6	Item 6 Score?	9 [RTN]
	Enter datum 7	Item 7 Score?	8 [RTN]
	Enter datum 8	Item 8 Score?	27 [RTN]
3	End data input	Item 9 Score?	E [RTN]
4	Read value of mean and SD.	Mean = 17.625 Std. = 7.51561	[RTN]
5		Enter type of transformation:	

SOLUTION

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Enter transformation type	Log, SStandard, SQr, or T?	ST [RTN]
5b		Std. score transformation	[RTN]
6	Read transofrmations. Use	Item 1 Raw = 27 Trn = 1.2474	[RTN]
	[RTN] key to read the next	Item 2 Raw = 15 Trn = -.34927	[RTN]
	transformation.	Item 3 Raw = 26 Trn = 1.11435	[RTN]
		Item 4 Raw = 17 Trn = -.08316	[RTN]
		Item 5 Raw = 12 Trn = -.74844	[RTN]
		Item 6 Raw = 9 Trn = -1.14761	[RTN]
		Item 7 Raw = 8 Trn = -1.28067	[RTN]
		Item 8 Raw = 27 Trn = 1.2474	[RTN]
7	Options: Select 'view'	Run again, View again, or End?	V [RTN]
4	Read the mean again	Mean = 17.625 Std. = 7.51561	[RTN]
5		Enter type of transformation:	
	Enter transformation t	Log, SStandard, SQr, or T?	T [RTN]
5a	Enter constant μ, σ	Enter μ, σ ?	75,12 [RTN]
5b		T score transformation	[RTN]
6	Read the transformations	Item 1 Raw = 27 Trn = 89.96885	[RTN]
		Item 2 Raw = 15 Trn = 70.80872	[RTN]
		Item 3 Raw = 26 Trn = 88.37217	[RTN]
		Item 4 Raw = 17 Trn = 74.00208	[RTN]
		Item 5 Raw = 12 Trn = 66.01869	[RTN]
		Item 6 Raw = 9 Trn = 61.22866	[RTN]
		Item 7 Raw = 8 Trn = 59.63198	[RTN]
		Item 8 Raw = 27 Trn = 89.96885	[RTN]
7	End program	Run again, View again, or End?	E [RTN]

USER INSTRUCTIONS

STEP	INSTRUCTIONS	DISPLAY	INPUT
	Run "TRANS"	Transformations	
		<u>E</u> to end, <u>C</u> to correct	
1	Enter value of item #i	Item i Score?	A _i [RTN]
2	If you made an error:	Item i Score?	C [RTN]
	This will be displayed	Item i Deleted = A _i	
	Goto 1 until all data is in		
3	End data input	Item i Score?	E [RTN]
4	Read mean and std. deviation	Mean = Std. =	[RTN]
5	Enter transformation type:	Enter type of transformation:	
		Log, S _T andard, S _Q r, or T?	
	L = Log (base e) transformation		L [RTN] or
	ST = Standard score transformation		ST [RTN] or
	SQ = Square root transformation		SQ [RTN] or
	T = t-transformation		T [RTN]
5a	If t was chosen:	Enter μ, σ ?	μ, σ [RTN]
5b	Transformation type is displayed	transformation	[RTN]
6	Read transformations	Item i Raw = R _i Trn = T _i	[RTN]/[BACK]
7	Review routine	<u>R</u> un again, <u>V</u> iew again, or <u>E</u> nd?	
	R = rerun the program - step 1		R [RTN]
	V = review the answers and		V [RTN]
	select new transformation		
	type - step 4		
	E = exit the program		E [RTN]

VARIABLE NAMES

NAME	DESCRIPTION	NAME	DESCRIPTION
A()	Data storage	A\$	General use input string
T	Type of transformation	N	Total N of data
S1	Sum of all data $\sum X_i$	S2	Sum of all data-squared $\sum (X_i^2)$
K\$	Delay function string	M	Mean of data
S	Standard deviation (N)	D	Value of displayed trans.
MO	Constant μ for T	SO	Constant σ
U	Delay, = 1 if [BACK] used	X	Increment for output

NOTES AND REFERENCES

Note: 1. The program is limited to a maximum of 500 items. To change this alter the dimension statement in line 80.

- References: 1. B.J. Winer, STATISTICAL PRINCIPLES in Experimental Design (2nd ED), (McGraw-Hill, New York, 1971).
2. G.A. Ferguson, STATISTICAL ANALYSIS in Psychology and Education (2nd ED), (McGraw-Hill, New York, 1966), p. 109.

PROGRAM LISTING

```

10 ! TRANS - Data transformation
20 ! Log base e, square root,
30 ! standard score, & t score
40 !
50 ! REV 11/01/82
60 !
70 DISP "          Transformations" @ W
  AIT 1
80 DIM A(500),A$(160)
90 INTEGER T
100 DEF FNI(X) = INT(X*10^5+.5)/10^5
110 DEF FNE
120 IF N<1 THEN BEEP 220 @ DISP "Must h
    ave data to delete" @ WAIT 1 @ GOTO
    150
130 DISP "Item";N;"deleted =";A(N)
140 S1=S1-A(N) @ S2=S2-A(N)^2 @ N=N-1
150 FNE=0 @ END DEF
160 !
170 ! Delay function
180 !
190 DEF FND
200 K$=KEY$ @ IF K$(<>CHR$(13) AND K$(<>C
    HR$(8) THEN 200
210 FND=K$=CHR$(8) @ END DEF
220 N,S1,S2=0
230 DISP CHR$(197);" to end input, ";CH
    R$(195);" to correct" @ WAIT 1
240 ON ERROR BEEP 220 @ DISP "Enter IEI
    [RTN],[C]IRTN],or data" @ WAIT 1 @
    GOTO 250
250 DISP "Item";N+1;" Score"; @ INPUT A
    $
260 IF POS(UPRC$(A$),"E") THEN 330
270 IF POS(UPRC$(A$),"C") THEN U=FNE @
    GOTO 250
280 S1=S1+VAL(A$) @ S2=S2+VAL(A$)^2 @ N
    =N+1
290 A(N)=VAL(A$) @ GOTO 250
300 !
310 ! End data input
320 !
330 IF N<2 THEN BEEP 220 @ DISP "Must h
    ave more than 1 item" @ WAIT 1 @ GO
    TO 250
340 M=S1/N @ S=SQR(S2/N-(S1/N)^2)
350 PRINT "Mean= ";FNI(M);"SD.= ";FNI(S
    )
360 U=FND @ IF U THEN 350
370 DISP "Enter type of transformation:
    "

```

-Function to define output precision

-Function to handle error

-Decrement counters

-Delay function. Wait for 'RTN' or 'BACK' keys.

-Beginning of user dialogue

-Error trap

-Check to see if user wishes to end data entry

-Check to see if user wishes to correct data

-Increment counters

-Check validity of sample size

-Compute mean and standard deviation

-Prompt user to select transformation type

PROGRAM LISTING

```

380 DISP CHR$(204);"og, ";CHR$(211);CHR
   $(212);"andard, ";CHR$(211);CHR$(20
   9);"r, or ";
390 DISP CHR$(212); @ INPUT A$
400 A$=UPRC$(A$&" ") @ A$=A$[1,2]
410 IF POS("L LOSQSTT ",A$)=0 THEN 370
420 T=POS("L LOSQSIT ",A$) @ IF T>1 THE
   N T=T-1
430 IF T>1 THEN T=T/2
440 IF T=4 THEN DISP "Enter ";CHR$(12);
   ", ";CHR$(9); @ INPUT M0,S0
450 A$="Log(e)      Square-rootStd.score
   T-score      "
460 PRINT A$[T*11-10,T*11];" transforma
   tion"
470 U=FND
480 OFF ERROR
490 X=0
500 X=X+1 @ IF X>N THEN 610

510 IF T=1 THEN D=LOG(A(X))
520 IF T=2 THEN D=SQR(A(X))

530 IF T=3 OR T=4 THEN D=(A(X)-M)/S
540 IF T=4 THEN D=D*S0+M0

550 PRINT "Item";X;"Raw=";A(X);"Trn=";F
   NI(D)
560 U=FND @ IF U THEN X=X-1*(X>1) @ GOT
   O 510
570 GOTO 500
580 !
590 ! Review routine
600 !
610 DISP CHR$(210);"un again, ";CHR$(21
   4);"iew again, or ";CHR$(197);"nd";
620 INPUT A$ @ A$=UPRC$(A$&" ")
630 ON POS("RVE",A$[1,1])+1 GOTO 610,22
   0,350,640
640 STOP

```

-Enter mean and SD for
t-transformation

-Display name of transformation
type

-Increment counter and check
for end of data

-Compute log transformation

-Compute square-root
transformation

-Compute t and standard score
transformation

-Transform mean and SD for
t-transformation

-Display transformed data

-Program options

TEST STATISTICS

ONE SAMPLE TEST STATISTICS FOR THE MEAN
KENDALL'S COEFFICIENT OF CONCORDANCE
CORRELATION COEFFICIENT TEST
INTRAClass CORRELATION COEFFICIENT
KRUSKAL-WALLIS STATISTIC
MANN-WHITNEY U-TEST
FISHER'S EXACT PROBABILITY
2-FACTOR ANALYSIS OF VARIANCE
BARTLETT'S CHI-SQUARE STATISTIC
DIFFERENCES AMONG PROPORTIONS
DATA TRANSFORMATIONS

ALL HP-75 SOLUTIONS BOOKS ARE AVAILABLE RECORDED ON MINI-DATA CASSETTES
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